

# SHURLAND HALL GATEHOUSE, EASTCHURCH, ISLE OF SHEPPEY, KENT TREE-RING ANALYSIS OF TIMBERS

SCIENTIFIC DATING REPORT

Alison Arnold and Robert Howard



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**SHURLAND HALL GATEHOUSE  
EASTCHURCH  
ISLE OF SHEPPEY, KENT**

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Alison Arnold and Robert Howard

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## **SUMMARY**

Dendrochronological analysis of 30 samples from the gatehouse of Shurland Hall has resulted in the production of three site chronologies. The first comprises eight samples of overall length of 122 rings, the second comprises 14 samples with an overall length of 192 rings, whilst the third comprises three samples of overall length 96 rings. Only the 122 rings of the first site chronology can be dated, these spanning the years AD 1405–1526. Interpretation of the sapwood on the dated samples indicates that they probably represent timbers cut as part of a single programme of felling sometime between AD 1536–61. As such they represent neither the early-sixteenth century rebuild of Shurland Hall by Sir Thomas Cheney in the period AD 1510–18, nor the enlargement of the site completed in time for the visit of Henry VIII in AD 1532. It is possible, however, that the dated timbers were cut at different times from as early as AD 1523 to as late as AD 1566.

## **CONTRIBUTORS**

Alison Arnold and Robert Howard

## **ACKNOWLEDGEMENTS**

The Nottingham Tree-ring Dating Laboratory would like to take this opportunity to thank Tim Whittaker and the Spitalfields Historic Building Trust, now owners of Shurland Hall, not only for their enthusiasm in restoring this building but also for their helpful cooperation with this programme of tree-ring analysis, particularly in identifying the original location of removed timbers. We would also like to thank Peter Kendall, Inspector of Ancient Monuments of English Heritage's Guildford Office for his help in arranging site access. The Nottingham Laboratory would also like to thank Keevill Heritage Consultancy for the use of sections of their report in the introduction below (Keevill 2006).

## **ARCHIVE LOCATION**

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## INTRODUCTION

The remains of Shurland Hall stand on the Isle of Sheppey, in Eastchurch, Kent (TQ 992 715, Fig 1). It was once one of Kent's most important Tudor mansions, having been rebuilt by Sir Thomas Cheney (AD 1482–1558), Lord Warden of the Cinque Ports and Treasurer of the Household, on the site of an earlier medieval castle. Sir Thomas Cheney is supposed to have demolished the original buildings and built a new mansion in AD 1510–18. However, it is thought more likely that he extended and revamped at least some of the earlier structures, eg, the hall, and the original gate tower. The house was later enlarged, this work being completed by the time Henry VIII visited in AD 1532.

The house of Sir Thomas Cheney consisted of a gatehouse, in front of which, to the west, was a walled courtyard. There was a single gate in the front wall of this courtyard, and two entrances in each side wall. The gatehouse had gable-ended buildings to either side which extended east, or rearwards, towards the main hall, and formed the side ranges of an inner courtyard (the probable guest ranges). Another series of courtyards, to the rear of the main hall, consisted of pentice-type cloister buildings linking the hall to the chapel in the south-east corner and a possible kitchen/brew house range at the back of the group of buildings. The stable courtyards and ancillary courtyards were to one side and exit to the park would have been possible through a large courtyard to the rear.

The house was supposed to have been enlarged before the royal visit, with wings added from the gateway, a banqueting hall built to the east side of the inner courtyard, and dormitories on either side. In its final form it is believed that there were not less than nine quadrangles enclosed within high stone walls, the complex spreading over several acres, and presumably presenting an impressive sight (Fig 2). Sir Thomas Cheney died in December AD 1558 and the estate passed to his son Henry. From that time on, Shurland Hall gradually went into decline.

The house remained in residential use into the twentieth century, but was used by the military during World Wars I and II. Subsequently it was abandoned, and gradually began to fall into ruination (Fig 3). This process has accelerated markedly over the last decade, despite local and national concern for the future of this exceptionally important building.

The present gatehouse at Shurland, to the west of where the main buildings once were, is the most intact surviving part of the buildings, all other elements of the site now being lost. The tower forms the central portion of the gatehouse, with the twin turrets on the west front flanking the entrance. The northern and southern rooms of the extended gatehouse clearly butt against the tower, with straight joints being visible internally and externally on both the east and west facades. It is unclear whether the tower was originally wholly free-standing, or whether it may have had attached flanking courtyard walls. The tower was extended, probably quite soon after its original construction, to become a continuous range as an integral element of a multiple-courtyard house.

The building is currently a Scheduled Ancient Monument and is on the English Heritage Buildings at Risk Register.

## THE TIMBERS

The timbers found within the gatehouse comprise lintels to doors and windows, bridging beams of the first-floor frame, and common joists of the ground-floor frame to both the northern and southern parts of the gatehouse (there are none in the central gateway itself), these being set directly on the earth beneath, and almost certainly reused here. There are no roof, partition wall, or other structural timbers of any sort to be seen.

Given the extensive nature of the conservation and repair work being undertaken here, and particularly the decayed and unstable nature of the timbers (Fig 4a/b), the majority of these beams, particularly the bridging beams and common joists, had been removed from this structure and stored *ex-situ* before sampling was undertaken (Fig 5). In most instances, as with the bridging beams for example, the precise location of these timbers was recorded prior to removal. In some cases, however, as with the common joists, only the general original location was noted. Only door and window lintels remained undisturbed and *in-situ*. The other parts of Shurland Hall are now represented by partial wall remains and footing, and there are no timbers to these areas.

## SAMPLING

Sampling and analysis by tree-ring dating of the timbers within the gatehouse of Shurland Hall (there being no other timbers elsewhere to this site) were commissioned by English Heritage. The purpose of this programme of analysis was to inform urgent repair work on this Building at Risk. It was hoped that tree-ring analysis of the timbers would not only establish the construction date of the gatehouse, confirming whether or not it is part of Sir Thomas' programme of works, but also identify possible later phases of alteration, and establish how much, if any, older material from the original gate tower might have been reused.

The usual procedure in tree-ring dating is to obtain samples by coring. In this instance, however, having been long exposed to the elements, the timbers were often of a delicate nature and the cores would simply have fragmented. This method was, therefore, rejected and, from those timbers which were deemed beyond conservation or reuse, a total of 31 samples was obtained by the removal of cross-sectional slices with a chainsaw. These slices then being reduced to smaller radial sections.

Each sample was given the code SRL-A (for Shurland site "A") and numbered 01–31. Where possible, the original location of these samples was recorded at the time of sampling on a simple plan, reproduced here as Figure 6. Where the exact original location is not known, the general location only is given. Details of the samples are also given in Table 1.

It will be seen from Table 1 that none of the timbers which remain *in-situ* have been sampled. Such timbers were not only few in number, but sometimes buried within the walls and not easily accessible; like their floor-frame counterparts, they too were often badly rotted at their outer edges. Under these circumstances, given that such timbers appeared to be derived from moderately fast-grown trees, it was felt that they were unlikely to provide satisfactory samples for tree-ring analysis.

## ANALYSIS AND RESULTS

Each of the 31 samples obtained was prepared by sanding and polishing. It was seen at this point that one sample, SRL-A22, had less than 54 rings, the usual minimum required for reliable dating, and so it was rejected from this programme of analysis. The annual growth rings of the remaining 30 samples were, however, measured, the data of these measurements being given at the end of this report. The data of these 30 samples were then compared with each other by the Litton/Zainodin grouping procedure (see Appendix), allowing three site chronologies to be formed at a minimum  $t$ -value of  $t=4.5$ .

The first site chronology, SRLASQ01 (Fig 7), comprises eight samples with an overall length of 122 rings. Site chronology SRLASQ01 was compared to an extensive corpus of reference material for oak, this indicating consistent and repeated cross-matches with several of them when the first ring date of the site chronology is AD 1405 and the last measured ring date is AD 1526. The evidence for this dating is given in Table 2 where an indicative selection is listed.

The second site chronology, SRLASQ02 (Fig 8), comprises 14 samples with an overall length of 192 rings. Site chronology SRLASQ02 was also compared to an extensive range of reference material for oak, not only that held by the Nottingham Laboratory, but also with the reference material held by other dendrochronology laboratories. There was, however, no satisfactory cross-matching, and these 14 samples must remain undated.

The third and final site chronology, SRLASQ03 (Fig 9), comprises three samples with an overall length of 96 rings. Site chronology SRLASQ03 was likewise compared to an extensive range of reference material for oak by the Nottingham Laboratory and others, but again there was no satisfactory cross-matching, and these three samples must remain undated.

Each site chronology was then compared with the remaining five measured but ungrouped samples, but there was no further satisfactory cross-matching. Each of the remaining five ungrouped samples was then compared individually with the reference chronologies, but again, there was no satisfactory cross-matching and these samples must, therefore, also remain undated.

This analysis can be summarised as follows:

Site chronology	Number of samples	Number of rings	Date span (where dated)
SRLASQ01	8	122	AD 1405–1526
SRLASQ02	14	192	undated
SRLASQ03	3	96	undated
individuals	5	---	undated
	1	---	unmeasured

It was noticeable during this analysis that a number of samples within each group cross-match very well with each other, suggesting the possibility that the trees represented by each group were all growing close to each other. There are, for example, values in excess of  $t=6.0$  between the samples in site chronology SRLASQ03, and values in excess of  $t=8.0$  between the samples of site chronology SRLASQ01. However, the most similar samples are those of site chronology SRLASQ02, where values in excess of  $t=13.0$ ,  $t=14.0$ , and even  $t=15.0$  are seen. Indeed, values as high as these would suggest that some timbers have been derived from the same tree, which, given that most of these are small common joists formed of quartered trees, is a distinct possibility.

## DISCUSSION AND CONCLUSION

The tree-ring analysis undertaken here has produced three site chronologies, only one of which, SRLASQ01, can be dated, its 122 rings spanning the years AD 1405–1526. This site sequence includes main beams and common joists from the north and south ranges, as well as a bridging beam from the central range. None of the seven samples in this site chronology retains complete sapwood and it is thus not possible to determine their exact felling date with reliability. Several of them, however, do retain the heartwood/sapwood boundary.

The heartwood/sapwood boundary, where it exists, on the samples in site chronology SRLASQ01 varies from relative position/date 113/AD 1517 on sample SRL-A06 to relative position/date 122/AD 1526 on sample SRL-A08, a variation of only nine years; the overall average date of the boundary is AD 1521. Such a limited variation could be taken as evidence that the dated timbers were cut as part of a single felling operation. If this were the case, using a 95% confidence limit of 15–40 rings for the amount of sapwood the trees might have had, they would have an estimated felling date in the range AD 1536–61.

The view that the timbers were all felled at the same, or at a very similar time, is further supported by the degree of cross-match between some of the samples. The high levels of ' $t$ ' between some samples would certainly suggest that the timbers came from a single woodland source, a phenomenon more frequently seen amongst timbers of the same phase of felling than amongst timbers felled at different times.



This assumption, however, is not necessarily correct as the dated timbers are not part of a single, integral, framed structure, free of the evidence of reuse, but from loose timbers, many of which are clearly recycled in their present positions. It is thus quite possible that the dated timbers were felled at different times from possibly as early as 1523 to as late as 1566. The felling date range of each individual timber is given below, again using a 95% confidence limit of 15–40 rings for the amount of sapwood the trees might have had.

Sample	Felling date range
SRL-A01	AD 1533–58
SRL-A02	AD 1523–38
SRL-A03	AD 1534–59
SRL-A04	Unlikely to be before AD 1506
SRL-A05	Unlikely to be before AD 1526
SRL-A06	AD 1532–57
SRL-A08	AD 1541–66
SRL-A14	Unlikely to be before AD 1513

It is clear, therefore, that the timbers represented by the dated material do not belong with the supposed major rebuilding of Shurland Hall by Sir Thomas Cheney in the period AD 1510–18, and although there is a slight possibility that one or two timbers may have been felled for the enlargement of Shurland completed prior to the visit by Henry VIII in AD 1532, it is very unlikely that they all were. It would appear, therefore, that they represent a later phase of building works, despite there being no documented event in the period AD 1536–61 which would call for the further felling of timbers.

Although dendrochronology cannot be used to identify the precise source of timber (eg Bridge 2000), it would appear that the timbers in the gatehouse are likely to be from woodlands that were reasonably close to Shurland. As will be seen from Table 2, many of the highest *t*-values obtained during the dating of site sequence SRLASQ01, and thus the greatest degree of similarity, are with reference chronologies from sites elsewhere in Kent and south-east England.

In this respect, it is of interest to note the lack of cross-matching and dating of the other two site sequences, and the remaining single samples. Site chronology SRLASQ02, containing 14 samples, is certainly well replicated and, having in excess of 190 rings, is certainly long enough for reliable dating; site chronology SRLASQ03, comprising three samples and at less than 100 rings long, though still adequate, is perhaps less so. Neither site chronology, nor the single samples can be dated regardless of the fact they have been compared to an extensive corpus of reference material from Britain and elsewhere in Europe.

This lack of cross-matching might suggest two possibilities. Either there is some peculiarity with the annual growth rings of the undated samples, potentially reflecting highly localised growth conditions, which make cross-matching and dating difficult, though none is

apparent in the samples, or, alternatively, although less likely, the timber is from a time and/or a place for which no reference material is currently available. In this respect the unmatched data from Shurland may in due course be of considerable use.

The phenomenon of undated site chronologies and individual samples has, to a certain extent, been encountered previously in Kent, during the survey of that county by the Royal Commission on the Historical Monuments of England (Pearson 1994). During tree-ring analysis undertaken as part of that survey it was noted that amongst a number of buildings believed, on stylistic and architectural evidence, to date to the early- to mid-fourteenth century, a number produced no dates, despite having suitable chronologies or samples. Such buildings were not, however, confined to any particular area, but strung out from Eastry in the east to Fawkham in the west, although, interestingly, always in the north of the county. This does not of course prove that the undated timbers from the gatehouse at Shurland Hall are also of an early date, but it is a possibility and it does show that Shurland is not an isolated case.

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## TABLES

*Table 1: Details of tree-ring samples from Shurland Gatehouse, Eastchurch, Kent*

Sample number	Sample location	Total rings*	Sapwood rings**	First measured ring date (AD)	Last heartwood ring date (AD)	Last measured ring date (AD)
SRL-A01	Bridging beam, centre range	110	h/s	AD 1409	AD 1518	AD 1518
SRL-A02	Main beam 1, south range	105	h/s	AD 1419	AD 1523	AD 1523
SRL-A03	Main beam 2, south range	104	h/s	AD 1416	AD 1519	AD 1519
SRL-A04	Common joist, south range	80	no h/s	AD 1412	-----	AD 1491
SRL-A05	Main beam 1, north range	80	no h/s	AD 1432	-----	AD 1511
SRL-A06	Common joist, north range	107	h/s	AD 1411	AD 1517	AD 1517
SRL-A07	Common joist, north range	55	no h/s	-----	-----	-----
SRL-A08	Common joist, north range	76	h/s	AD 1451	AD 1526	AD 1526
SRL-A09	Common joist, north range	87	no h/s	-----	-----	-----
SRL-A10	Common joist, north range	65	no h/s	-----	-----	-----
SRL-A11	Common joist, north range	124	no h/s	-----	-----	-----
SRL-A12	Common joist, north range	94	no h/s	-----	-----	-----
SRL-A13	Common joist, north range	140	no h/s	-----	-----	-----
SRL-A14	Common joist, north range	94	no h/s	AD 1405	-----	1498
SRL-A15	Common joist, north range	163	no h/s	-----	-----	-----
SRL-A16	Common joist, north range	105	no h/s	-----	-----	-----
SRL-A17	Common joist, north range	101	no h/s	-----	-----	-----
SRL-A18	Common joist, north range	67	no h/s	-----	-----	-----
SRL-A19	Common joist, north range	66	no h/s	-----	-----	-----
SRL-A20	Common joist, north range	60	no h/s	-----	-----	-----
SRL-A21	Common joist, north range	95	no h/s	-----	-----	-----
SRL-A22	Common joist, north range	nm	no h/s	-----	-----	-----
SRL-A23	Common joist, north range	98	h/s	-----	-----	-----
SRL-A24	Common joist, north range	124	h/s	-----	-----	-----
SRL-A25	Common joist, north range	89	no h/s	-----	-----	-----

**Table 1: continued**

Sample number	Sample location	Total rings*	Sapwood rings**	First measured ring date (AD)	Last heartwood ring date (AD)	Last measured ring date (AD)
SRL-A26	Common joist, north range	63	no h/s	-----	-----	-----
SRL-A27	Common joist, north range	113	h/s	-----	-----	-----
SRL-A28	Common joist, north range	85	no h/s	-----	-----	-----
SRL-A29	Common joist, north range	160	no h/s	-----	-----	-----
SRL-A30	Common joist, north range	95	no h/s	-----	-----	-----
SRL-A31	Common joist, north range	76	no h/s	-----	-----	-----

\*NM = not measured

\*\*h/s = the heartwood/sapwood ring is the last ring on the sample

C = complete sapwood retained on sample, last measured ring is the felling date

**Table 2: Results of the cross-matching of site chronology SRLASQ01 and relevant reference chronologies when first ring date is AD 1405 and last ring date is AD 1526**

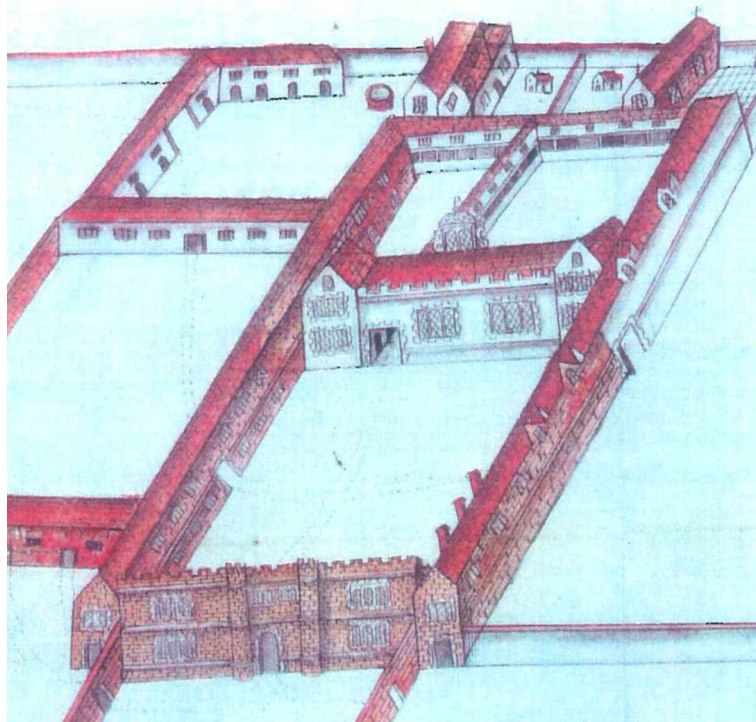
Reference chronology	Span of chronology	z-value	
Kent-88	AD 1158-1540	8.4	( Laxton and Litton 1989 )
Manor House, High Street, Fordwich, Kent	AD 1264-1556	7.8	( Arnold <i>et al</i> 2003 )
China Court, Petham, Kent	AD 1375-1491	6.9	( Howard <i>et al</i> 1988 )
Walmer Castle, Kent	AD 1396-1523	6.9	( Howard <i>et al</i> 1997 )
Chilton Manor, Sittingbourne, Kent	AD 1368-1520	6.6	( Howard <i>et al</i> 1988 )
Abbey Farm Barns, Faversham, Kent	AD 1344-1471	6.4	( Howard <i>et al</i> 1998 )
England, London	AD 413-1728	6.2	( Tyers and Groves 1999 unpubl )
Ightham Mote (billiards room), Ivy Hatch, Kent	AD 1405-1521	6.2	( Howard <i>et al</i> 1996 )

# FIGURES

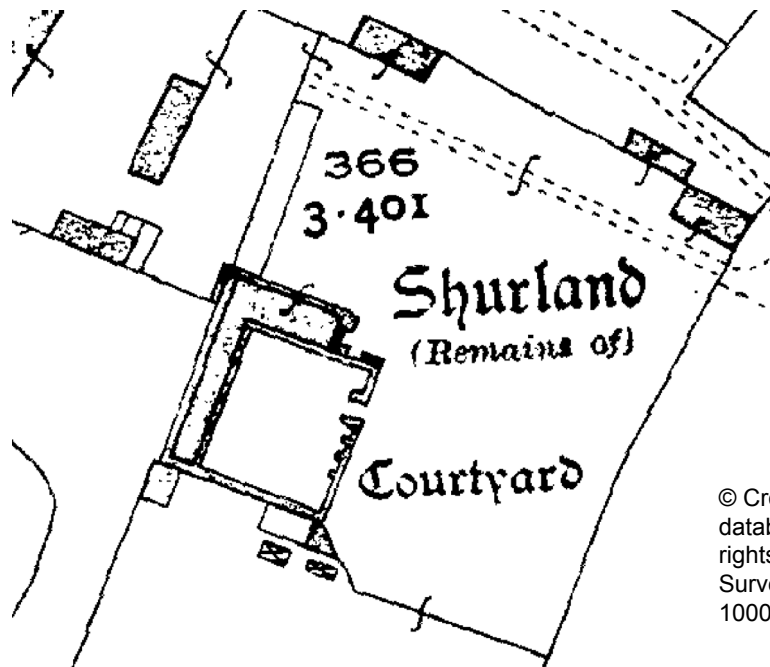


Figure 1: Map to show the location of Shurland Hall

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*Figure 2: Shurland Hall in 1572 from the west, with the gatehouse in the foreground (detail from Map of the Isle of Sheppey...., Elizabethan State Papers, SP12/87, The National Archives, © Crown Copyright)*



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*Figure 3: Map to show the surviving ruins of Shurland Hall in 1933*

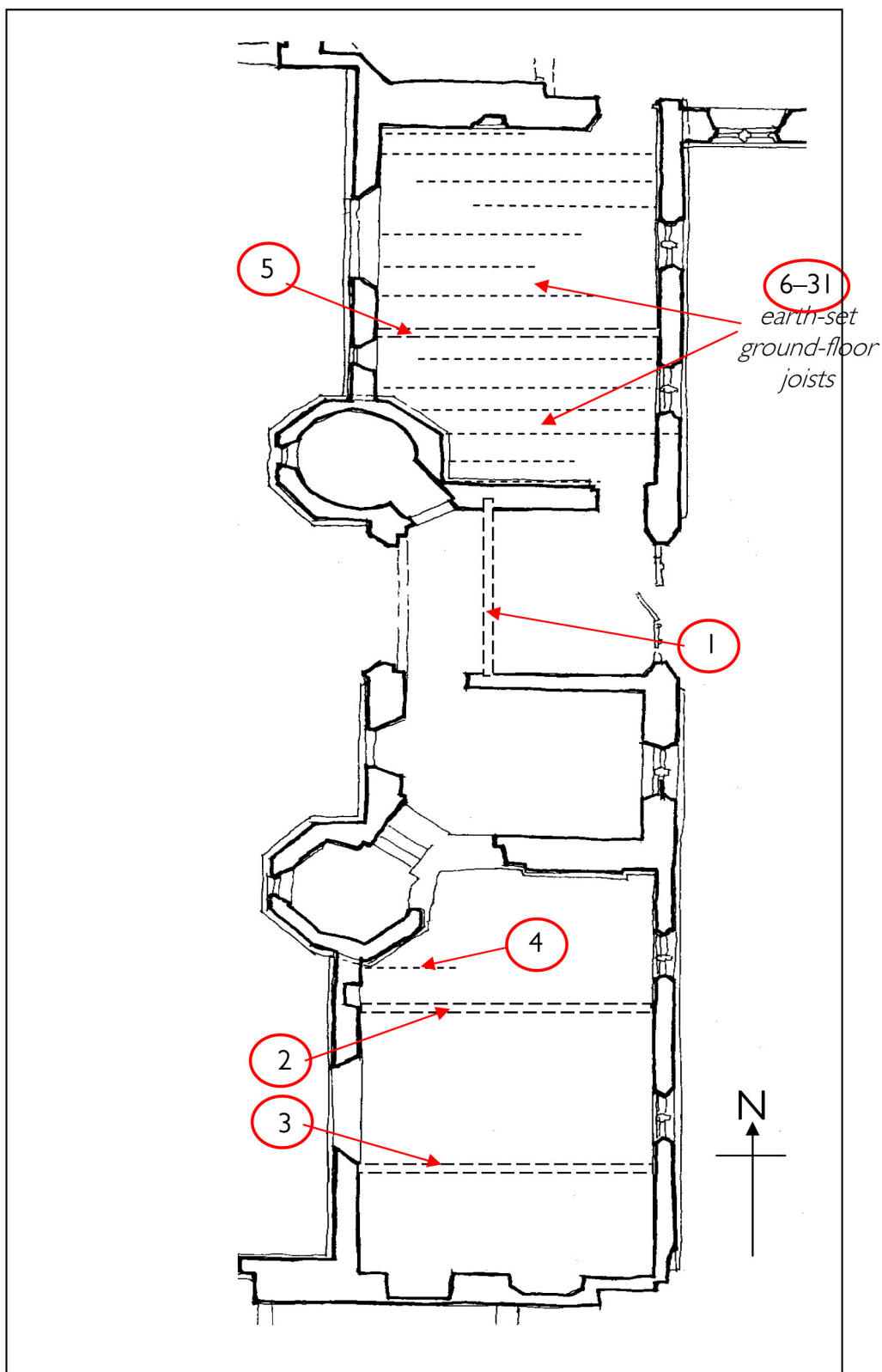


*Figure 4a/b: Photographs to show derelict and dangerous nature of the building before room clearance and stabilisation (photos by Peter Rumley consulting archaeologist)*

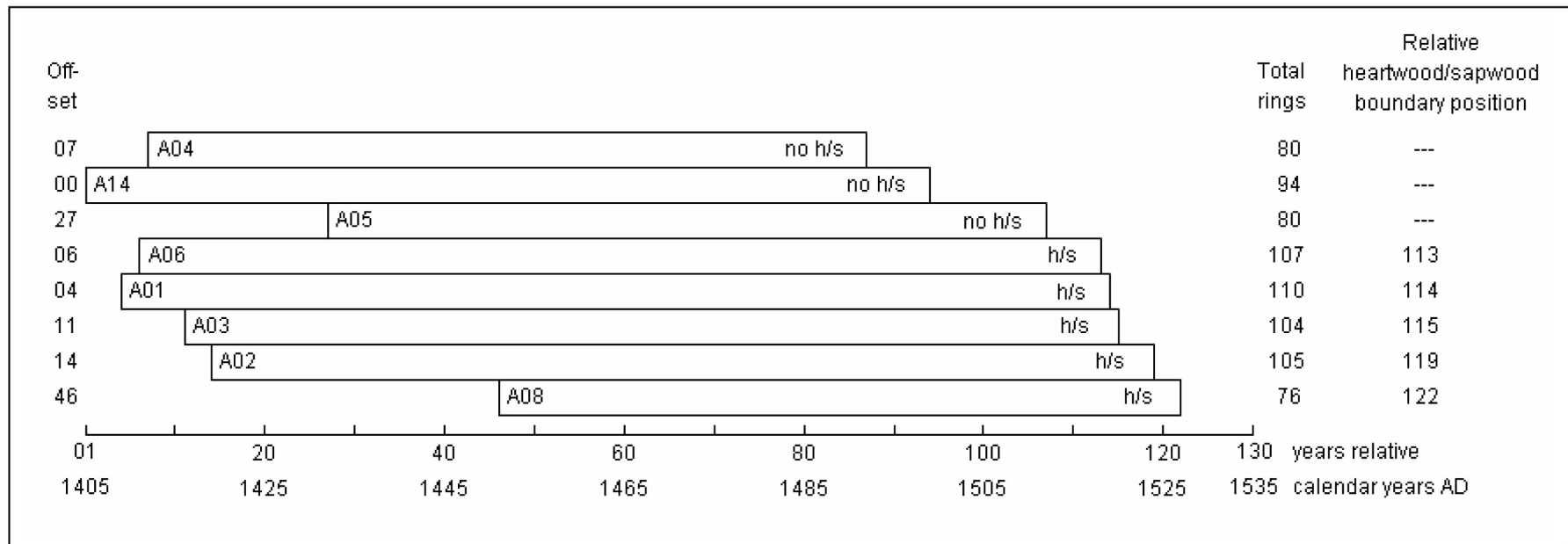




*Figure 5: Photograph to show two of the removed bridging beams*



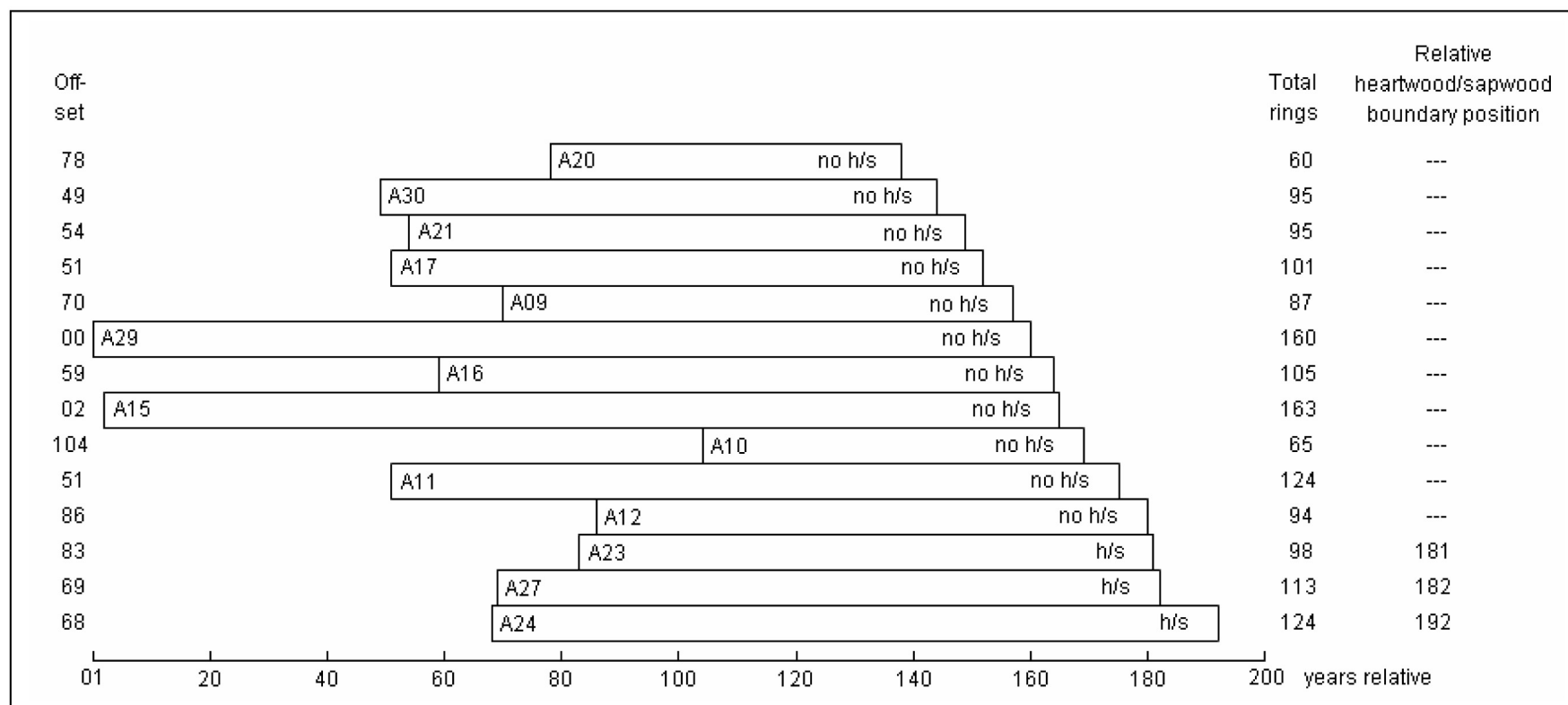
*Figure 6: Plan of the gatehouse to show position of sampled timbers where known, or general location where not recorded before removal*




Empty bars  = heartwood rings

h/s = the last ring on the sample is at the heartwood/sapwood boundary, only the sapwood rings are missing

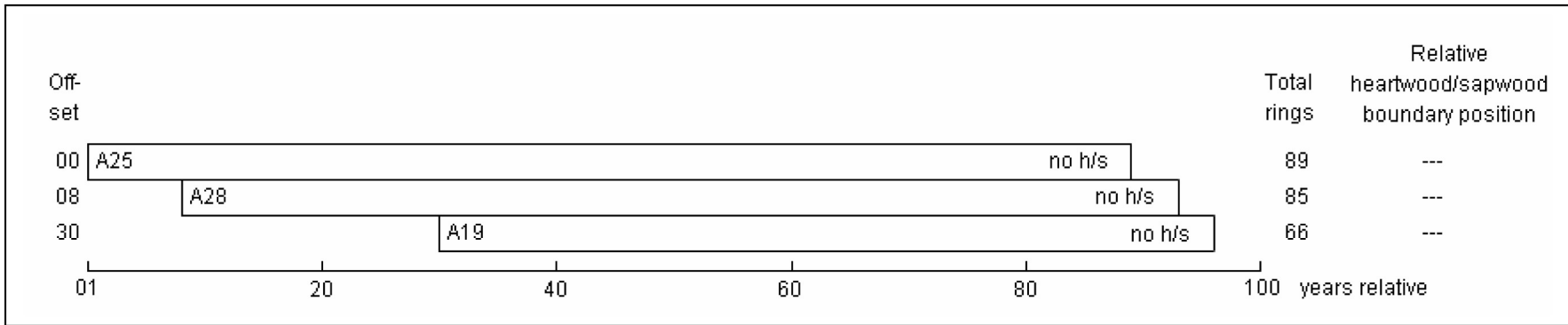
**Figure 7: Bar diagram of the samples in site chronology SRLASQ01**



Empty bars  = heartwood rings

h/s = the last ring on the sample is at the heartwood/sapwood boundary, only the sapwood rings are

*Figure 8: Bar diagram of the samples in site chronology SRLASQ02*



Empty bars  = heartwood rings

h/s = the last ring on the sample is at the heartwood/sapwood boundary, only the sapwood rings are

**Figure 9: Bar diagram of the samples in site chronology SRLASQ03**

## DATA OF MEASURED SAMPLES

Measurements in 0.01 mm units

### SRL-A01A 110

179 138 229 200 169 191 275 198 183 270 251 410 346 328 466 352 360 375 280 355  
409 417 342 421 314 257 370 312 285 270 230 251 288 245 276 272 249 250 243 195  
291 160 219 198 203 225 278 262 236 252 194 214 214 159 207 131 144 155 138 205  
173 184 166 121 162 149 153 140 93 102 100 99 239 151 140 157 183 168 145 142  
157 148 141 102 121 128 135 212 167 162 126 119 139 107 91 125 151 228 178 140  
184 150 123 111 84 91 98 128 103 116

### SRL-A01B 110

172 121 224 177 166 182 276 213 200 275 240 409 370 385 515 324 381 367 275 372  
379 412 394 415 331 264 359 324 302 235 213 247 296 252 258 276 274 275 278 239  
274 152 231 199 195 240 285 285 235 248 188 251 196 194 199 149 154 165 178 188  
175 183 165 111 133 124 192 159 101 118 100 115 237 146 155 159 175 196 155 123  
174 153 138 102 139 132 146 254 145 141 141 141 120 121 96 126 134 228 171 141  
182 132 137 98 108 107 112 129 105 113

### SRL-A02A 105

129 144 145 143 229 162 151 153 133 128 137 174 256 204 150 157 212 204 169 193  
116 173 155 193 139 105 120 127 140 156 203 103 130 114 88 106 127 172 148 117  
116 152 159 157 149 123 146 104 104 141 140 94 93 107 101 131 156 137 130 91  
114 146 208 188 128 210 216 166 181 141 140 209 126 114 129 152 131 214 184 143  
160 96 94 118 61 57 88 86 90 92 108 100 45 57 73 90 112 70 90 103  
116 101 77 100 175

### SRL-A02B 80

102 139 126 108 117 126 150 167 111 125 131 92 109 109 145 157 140 154 129 169  
167 148 106 122 108 97 144 120 96 110 104 141 163 169 114 106 113 158 180 233  
136 153 154 160 138 153 130 135 129 98 75 106 150 122 195 119 98 112 82 116  
97 61 88 93 104 95 92 97 84 61 60 69 89 90 88 81 109 93 110 107

### SRL-A03A 97

113 182 380 176 200 209 252 243 225 167 130 150 188 223 134 124 194 142 105 134  
110 135 104 141 102 113 108 156 142 124 149 101 135 122 95 102 130 148 128 117  
117 123 156 181 171 128 156 145 163 230 177 104 156 216 150 150 247 155 145 146  
193 232 281 224 221 255 227 185 186 159 162 228 155 131 153 163 169 228 221 146  
144 112 95 103 57 60 80 117 93 107 103 89 58 72 126 92 136

### SRL-A03B 104

156 177 162 163 230 201 184 230 192 290 257 191 128 158 177 192 209 148 150 257  
195 186 167 151 199 171 189 193 177 145 146 168 179 205 125 145 126 122 115 186  
184 134 159 144 172 155 198 153 96 118 127 102 132 137 103 103 103 111 108 134  
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152 146 106 106 85 102 107 65 69 113 126 119 86 107 116 68 81 80 77 93  
120 122 72 124

### SRL-A04A 80

188 231 174 208 174 201 230 288 229 193 244 218 200 211 173 119 114 114 127 123  
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113 85 79 70 52 46 54 64 74 59 48 39 59 51 66 56 41 41 68 60

### SRL-A04B 80

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110 92 81 80 51 47 60 61 72 64 50 41 71 50 66 53 45 53 67 57  
 SRL-A05A 80  
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 200 157 223 195 244 239 210 159 151 231 233 254 170 153 177 273 327 252 205 171  
 1 207 177 217 181 327 286 138 139 137 168 135 99 98 151 176 180 129 140 146 235  
 SRL-A05B 80  
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 SRL-A06A 107  
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 77 73 88 81 93 73 108  
 SRL-A06B 107  
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 583 353 345 422 465 373 414 320 356 365 244 287 241 210  
 263 148 115 166 184 198 177 186 133 154 116 115 114 93 133 108 91 119 80 79  
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 163 118 124 133 134 177 124 99 109 95 81 77 78 74 89 89 105 71 96 83  
 41 73 73 96 92 91 117  
 SRL-A07A 55  
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 99 118 136 122  
 SRL-A07B 55  
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 SRL-A08A 76  
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 SRL-A08B 76  
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 552 431 511 408  
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 94 119 106 143 88 135 95 133 112 130 116 125 108 97 114 114 165 133 123 129 121 178  
 SRL-A09B 87  
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 83 72 75 68 77 85 116 54 83 86 131 89 123 125 97 106 88 117 117 86  
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 107 154 115 138  
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 SRL-A10A 65  
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 123 107 122 83 131

SRL-A10B 65

177 148 126 157 110 113 119 151 108 131 83 88 90 117 110 109 113 116 100 121 105 94 122 88  
107 109 120 126 92 95 108 115 98 100 134 125  
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114 107 131 99 120

SRL-A11A 124

75 79 76 86 89 59 60 46 69 84 79 77 82 86 93 91 78 85 80 102 94 105 93 113 99 88  
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84 105 69 80 107 120 126 127 132 109  
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123 170 107 118

SRL-A11B 124

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84 88 126 124 90 118 107 129 124 97 147 119 124 108 102 128 96 131 80 110 114 118 121 96  
107 70 80 106 114 134 134 118 98  
144 131 116 104 143 121 132 105 108 118 114 155 103 145 108 149 128 168 105 148  
142 152 104 117

SRL-A12A 94

178 152 82 119 96 71 106 83 78 66 84 72 66 73 79 84 78 99 62 62 94 92 82 70 51 78  
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90 122 89 66 77 87 64 80 72 102 76 74 94 97 80 94 108 88 103 111  
117 128 99 93 77 82 129 103 74 90 79 76 109 128 84 99 114 149 108 124  
207 98 59 87 68 81 79 88 116 75 96 92 90 125

SRL-A12B 94

166 127 90 131 111 78 92 94 75 119 149 88 91 119 124 97 109 120 104 74  
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80 122 94 71 82 81 66 76 76 95 66 73 92 111 76 94 106 90 104 98  
111 129 103 100 72 87 122 108 74 78 69 81 112 116 85 115 94 87 102 94  
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SRL-A13A 140

115 144 155 231 220 294 262 444 251 132 215 368 166 183 204 173 163 194 99 163  
182 258 68 106 122 76 72 79 95 129 201 111 178 129 113 137 154 141 112 109  
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64 99 64 99 82 114 97 110 77 76 49 84 77 112 63 80 66 53 111 85  
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SRL-A13B 140

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129 144 71 94 66 93 182 127 127 66 74 106 69 107 91 95 95 90 83 95  
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86 68 91 67 92 92 55 54 67 99 112 114 98 94 80 92 94 89 91 102  
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SRL-A14A 94

339 288 192 248 216 273 270 239 214 256 240 159 136 150 149 178 124 103 166 158  
139 120 122 105 117 126 143 139 108 102 178 129 112 123 140 140 122 174 113 103  
84 117 107 109 173 132 162 131 90 128 136 185 176 136 131 139 168 173 137 116



113 110 87 158 130 84 115 124 117 186 211 103 130 126 232 247 327 215 139 178  
158 158 135 111 121 145 87 99 148 142 135 224 178 232

SRL-A14B 94

314 290 191 244 212 273 272 241 203 269 255 155 132 157 155 176 122 119 163 153  
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91 111 112 121 151 119 141 118 97 128 152 190 184 142 121 150 193 173 144 110  
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178 165 132 113 117 147 77 99 142 160 145 238 203 132

SRL-A15A 163

115 123 82 94 73 91 90 112 91 125 128 99 115 117 93 112 144 98 108 129  
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62 60 57 58 65 61 72 66 52 76 66 77 75 101 110 84 98 76 63 68  
72 62 101

SRL-A15B 163

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60 65 100

SRL-A16A 105

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76 88 115 93 92

SRL-A16B 105

93 92 104 64 101 99 88 80 74 90 82 99 94 80 96 88 102 65 82 76  
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80 120 115 104 131 114 93 96 115 95 85 101 79 83 114 116 88 99 116 125  
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75 82 98 92 91

SRL-A17A 88

99 118 65 80 87 76 86 88 77 88 76 89 65 82 67 85 106 94 68 86  
82 83 87 91 62 65 86 72 95 68 68 84 116 63 73 87 120 106 121 126  
90 95 83 98 99 88 91 75 94 132 107 83 118 130 136 138 118 152 132 135  
113 143 103 139 119 98 86 94 100 112 89 109 77 105 86 94 80 73 89 68  
67 78 84 105 96 91 84 88

SRL-A17B 97

65 65 64 77 82 66 65 43 63 89 91 65 89 100 133 63 85 75 92 91  
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90 84 76 74 98 104 72 76 95 120 120 116 124 86 109 91 100 98 77 99  
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90 95 114 110 130 89 113 87 97 109 95 80 65 79 84 77 113  
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 178 233 274 275 302 276 243  
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 137 276 205 143 150 163  
 SRL-A19B 66  
 120 208 175 186 207 216 187 163 166 136 138 161 164 113 59 106 95 172 241 180  
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 131 124 109 130 120 125 94 125 92 115 92 95 82 111 84 133 122 137 93 93  
 SRL-A20B 60  
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 127 121 103 131 126 126 96 124 84 114 92 94 82 107 99 127 119 132 93 98  
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 106 96 111 115 132 156 107 109 128 132 122 104 143 131 128 123 100 95 123 99  
 103 103 81 94 94 101 108 77 86 72 74 96 83 120 133  
 SRL-A21B 95  
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 76 87 106 69 75 91 109 98 125 125 94 97 86 103 85 89 102 82 84 116  
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 130 112 94 148 111 142 126 154 96 128 137 108 92 110 95 111 130 102 136 126  
 SRL-A23B 85  
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 SRL-A24A 124

131 185 169 147 108 143 193 202 119 97 139 174 172 190 117 157 144 183 180 184  
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105 104 115 130 98 93 95 115 80 96 109 103 106 114 130 90 129 109 112 131  
134 117 88 115 123 104 101 89 95 102 125 121 84 116 91 83 130 101 109 108  
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71 81 92 90

SRL-A24B 124

131 217 174 155 111 130 175 192 126 98 150 174 176 197 121 162 141 185 175 184  
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86 75 95 146 96 97 90 75 90 143 145 130 101 111 120 125 103 132 109 142  
108 102 121 119 108 101 97 107 85 88 100 114 103 115 122 96 130 111 111 127  
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109 75 94 85 92 108 102 91 90 113 128 85 86 99 78 86 87 116 85 81  
75 84 90 89

SRL-A25A 85

192 186 215 177 97 112 131 173 169 173 95 99 97 112 89 77 98 75 75 109  
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94 124 134 163 108 118 86 63 60 81 111 98 119 150 144 147 140 106 83 95  
88 131 128 192 245

SRL-A25B 74

134 110 74 116 144 112 135 121 163 155 96 94 100 146 182 166 168 121 161 171  
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SRL-A26A 63

155 169 182 197 189 199 207 259 200 180 134 146 206 235 236 227 164 198 143 235  
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124 155 136

SRL-A26B 63

158 177 175 193 192 202 206 257 196 184 138 158 187 222 238 196 165 184 145 220  
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133 150 155

SRL-A27A 113

98 168 161 139 163 180 203 116 101 127 116 135 182 101 160 121 161 150 164 118  
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112 139 165 89 81 89 81 88 140 138 148 140 95 108 124 135 146 135 150 97  
98 104 115 105 117 111 110 75 91 112 118 117 116 140 86 135 115 112 118 123  
113 93 95 126 116 97 82 86 106 142 136 112 137 124 89 118 99 114 109 107  
101 92 91 79 90 113 100 103 113 107 82 80 91

SRL-A27B 113

108 174 157 139 182 171 191 127 95 117 129 129 187 97 148 134 159 163 161 105  
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101 152 159 89 89 98 78 93 135 141 136 137 101 107 125 127 146 135 156 93  
105 103 111 103 111 105 118 80 101 103 125 112 113 143 96 138 111 112 120 121  
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SRL-A28A 85

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158 152 148 188 212

SRL-A28B 85

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134 163 140 248 272

SRL-A29A 160

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SRL-A29B 160

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81 61 72 63 41 59 63 53 47 85 60 58 71 69 79 76 64 68 69 93  
72 86 63 95 98 101 50 79 81 70 74 83 65 64 66 92 84 83 93 90  
101 91 72 97 69 86 94 121 113 151 130 155 160 123 155 136 205 135 119 163  
183 220 161 181 157 159 109 162 96 108 113 124 96 89 81 71 65 59 81 90  
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SRL-A30A 94

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58 103 66 95 113 109 90 91 113 121 131 92 110 109 115 102 114 112 120 92  
90 83 93 94 119 96 124 78 96 97 116 103 103 91

SRL-A30B 95

51 65 76 62 68 61 71 65 49 36 61 61 79 71 75 111 86 74 53 89  
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69 76 75 88 87 83 86 99 68 71 71 99 121 125 120 86 103 96 91 96  
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SRL-A31A 76

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SRL-A31B 76

122 108 117 99 106 112 144 121 99 133 98 132 111 91 140 123 133 95 118 88  
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75 77 127 98 113 143 86 111 102 80 85 94 80 90 130 123 138 126 149 134  
51 62 49 75 64 98 83 76 82 73 60 71 68 58 57 75

## APPENDIX: TREE-RING DATING

### The Principles of Tree-Ring Dating

Tree-ring dating, or dendrochronology as it is known, is discussed in some detail in the Laboratory's Monograph, *An East Midlands Master Tree-Ring Chronology and its uses for dating Vernacular Building* (Laxton and Litton 1988) and *Dendrochronology: Guidelines on Producing and Interpreting Dendrochronological Dates* (English Heritage 1988). Here we will give the bare outlines. Each year an oak tree grows an extra ring on the outside of its trunk and all its branches just inside its bark. The width of this annual ring depends largely on the weather during the growing season, about April to October, and possibly also on the weather during the previous year. Good growing seasons give rise to relatively wide rings, poor ones to very narrow rings and average ones to relatively average ring widths. Since the climate is so variable from year to year, almost random-like, the widths of these rings will also appear random-like in sequence, reflecting the seasons. This is illustrated in Figure A1 where, for example, the widest rings appear at irregular intervals. This is the key to dating by tree rings, or rather, by their widths. Records of the average ring widths for oaks, one for each year for the last 1000 years or more, are available for different areas. These are called master chronologies. Because of the random-like nature of these sequences of widths, there is usually only one position at which a sequence of ring widths from a sample of oak timber with at least 70 rings will match a master. This will date the timber and, in particular, the last ring.

If the bark is still on the sample, as in Figure A1, then the date of the last ring will be the date of felling of the oak from which it was cut. There is much evidence that in medieval times oaks cut down for building purposes were used almost immediately, usually within the year or so (Rackham 1976). Hence if bark is present on several main timbers in a building, none of which appear reused or are later insertions, and if they all have the same date for their last ring, then we can be quite confident that this is the date of construction or soon after. If there is no bark on the sample, then we have to make an estimate of the felling date; how this is done is explained below.

### The Practice of Tree-Ring Dating at the Nottingham Tree-Ring Dating Laboratory

**1. Inspecting the Building and Sampling the Timbers.** Together with a building historian the timbers in a building are inspected to try to ensure that those sampled are not reused or later insertions. Sampling is almost always done by coring into the timber, which has the great advantage that we can sample *in situ* timbers and those judged best to give the date of construction, or phase of construction if there is more than one in the building. The timbers to be sampled are also inspected to see how many rings they have. We normally look for timbers with at least 70 rings, and preferably more. With fewer rings than this, 50 for example, sequences of widths become difficult to match to a unique

position within a master sequence of ring widths and so are difficult to date (Litton and Zainodin 1991). The cross-section of the rafter shown in Figure A2 has about 120 rings; about 20 of which are sapwood rings – the lighter rings on the outside. Similarly the core has just over 100 rings with a few sapwood rings.

To ensure that we are getting the date of the building as a whole, or the whole of a phase of construction if there is more than one, about 8–10 samples per phase are usually taken. Sometimes we take many more, especially if the construction is complicated. One reason for taking so many samples is that, in general, some will fail to give a date. There may be many reasons why a particular sequence of ring widths from a sample of timber fails to give a date even though others from the same building do. For example, a particular tree may have grown in an odd ecological niche, so odd indeed that the widths of its rings were determined by factors other than the local climate! In such circumstances it will be impossible to date a timber from this tree using the master sequence whose widths, we can assume, were predominantly determined by the local climate at the time.

Sampling is done by coring into the timber with a hollow corer attached to an electric drill and usually from its outer rings inwards towards where the centre of the tree, the pith, is judged to be. An illustration of a core is shown in Figure A2; it is about 150mm long and 10mm diameter. Great care has to be taken to ensure that as few as possible of the outer rings are lost in coring. This can be difficult as these outer rings are often very soft (see below on sapwood). Each sample is given a code which identifies uniquely which timber it comes from, which building it is from and where the building is located. For example, CRO-A06 is the sixth core taken from the first building (A) sampled by the Laboratory in Cropwell Bishop. Where it came from in that building will be shown in the sampling records and drawings. No structural damage is done to any timbers by coring, nor does it weaken them.

During the initial inspection of the building and its timbers the dendrochronologist may come to the conclusion that, as far as can be judged, none of the timbers have sufficient rings in them for dating purposes and may advise against sampling to save further unwarranted expense.

All sampling by the Laboratory is undertaken according to current Health and Safety Standards. The Laboratory's dendrochronologists are insured.



*Figure A1: A wedge of oak from a tree felled in 1976. It shows the annual growth rings, one for each year from the innermost ring to the last ring on the outside just inside the bark. The year of each ring can be determined by counting back from the outside ring, which grew in 1976*



*Figure A2: Cross-section of a rafter, showing sapwood rings in the left-hand corner, the arrow points to the heartwood/sapwood boundary (H/S); and a core with sapwood; again the arrow is pointing to the H/S. The core is about the size of a pencil*



*Figure A3: Measuring ring widths under a microscope. The microscope is fixed while the sample is on a moving platform. The total sequence of widths is measured twice to ensure that an error has not been made. This type of apparatus is needed to process a large number of samples on a regular basis*





*Figure A4: Three cores from timbers in a building. They come from trees growing at the same time. Notice that, although the sequences of widths look similar, they are not identical. This is typical*

**2. Measuring Ring Widths.** Each core is sanded down with a belt sander using medium-grit paper and then finished by hand with flourgrade-grit paper. The rings are then clearly visible and differentiated from each other with a result very much like that shown in Figure A2. The core is then mounted on a movable table below a microscope and the ring-widths measured individually from the innermost ring to the outermost. The widths are automatically recorded in a computer file as they are measured (see Fig A3).

**3. Cross-Matching and Dating the Samples.** Because of the factors besides the local climate which may determine the annual widths of a tree's rings, no two sequences of ring widths from different oaks growing at the same time are exactly alike (Fig A4). Indeed, the sequences may not be exactly alike even when the trees are growing near to each other. Consequently, in the Laboratory we do not attempt to match two sequences of ring widths by eye, or graphically, or by any other subjective method. Instead, it is done objectively (ie statistically) on a computer by a process called cross-matching. The output from the computer tells us the extent of correlation between two sample sequences of widths or, if we are dating, between a sample sequence of widths and the master, at each relative position of one to the other (offsets). The extent of the correlation at an offset is determined by the *t*-value (defined in almost any introductory book on statistics). That offset with the maximum *t*-value among the *t*-values at all the offsets will be the best candidate for dating one sequence relative to the other. If one of these is a master chronology, then this will date the other. Experiments carried out in the past with sequences from oaks of known date suggest that a *t*-value of at least 4.5, and preferably at least 5.0, is usually adequate for the dating to be accepted with reasonable confidence (Laxton and Litton 1988; Laxton *et al* 1988; Howard *et al* 1984–1995).

This is illustrated in Figure A5 with timbers from one of the roofs of Lincoln Cathedral. Here four sequences of ring widths, LIN-C04, 05, 08, and 45, have been cross-matched with each other. The ring widths themselves have been omitted in the bar diagram, as is usual, but the offsets at which they best cross-match each other are shown; eg the sequence of ring widths of C08 matches the sequence of ring widths of C45 best when it is at a position starting 20 rings after the first ring of C45, and similarly for the others. The actual *t*-values between the four at these offsets of best correlations are in the matrix. Thus at the offset of +20 rings, the *t*-value between C45 and C08 is 5.6 and is the maximum found between these two among all the positions of one sequence relative to the other.

It is standard practice in our Laboratory first to cross-match as many as possible of the ring-width sequences of the samples in a building and then to form an average from them. This average is called a site sequence of the building being dated and is illustrated in Figure A5. The fifth bar at the bottom is a site sequence for a roof at Lincoln Cathedral and is constructed from the matching sequences of the four timbers. The site sequence width for each year is the average of the widths in each of the sample sequences which has a width for that year. Thus in Fig A5 if the widths shown are 0.8mm for C45, 0.2mm for C08, 0.7mm for C05, and 0.3mm for C04, then the corresponding width of the site

sequence is the average of these, 0.55mm. The actual sequence of widths of this site sequence is stored on the computer. The reason for creating site sequences is that it is usually easier to date an average sequence of ring widths with a master sequence than it is to date the individual component sample sequences separately.

The straightforward method of cross-matching several sample sequences with each other one at a time is called the 'maximal *t*-value' method. The actual method of cross-matching a group of sequences of ring-widths used in the Laboratory involves grouping and averaging the ring-width sequences and is called the 'Litton-Zainodin Grouping Procedure'. It is a modification of the straightforward method and was successfully developed and tested in the Laboratory and has been published (Litton and Zainodin 1991; Laxton *et al* 1988).

**4. Estimating the Felling Date.** As mentioned above, if the bark is present on a sample, then the date of its last ring is the date of the felling of its tree (or the last full year before felling, if it was felled in the first three months of the following calendar year, before any new growth had started, but this is not too important a consideration in most cases). The actual bark may not be present on a timber in a building, though the dendrochronologist who is sampling can often see from its surface that only the bark is missing. In these cases the date of the last ring is still the date of felling.

Quite often some, though not all, of the original outer rings are missing on a timber. The outer rings on an oak, called sapwood rings, are usually lighter than the inner rings, the heartwood, and so are relatively easy to identify. For example, sapwood can be seen in the corner of the rafter and at the outer end of the core in Figure A2, both indicated by arrows. More importantly for dendrochronology, the sapwood is relatively soft and so liable to insect attack and wear and tear. The builder, therefore, may remove some of the sapwood for precisely these reasons. Nevertheless, if at least some of the sapwood rings are left on a sample, we will know that not too many rings have been lost since felling so that the date of the last ring on the sample is only a few years before the date of the original last ring on the tree, and so to the date of felling.

Various estimates have been made and used for the average number of sapwood rings in mature oak trees (English Heritage 1998). A fairly conservative range is between 15 and 50 and that this holds for 95% of mature oaks. This means, of course, that in a small number of cases there could be fewer than 15 and more than 50 sapwood rings. For example, the core CRO-A06 has only 9 sapwood rings and some have obviously been lost over time – either they were removed originally by the carpenter and/or they rotted away in the building and/or they were lost in the coring. It is not known exactly how many sapwood rings are missing, but using the above range the Laboratory would estimate between a minimum of 6 (=15-9) and a maximum of 41 (=50-9). If the last ring of CRO-A06 has been dated to 1500, say, then the estimated felling-date range for the tree from which it came originally would be between 1506 and 1541. The Laboratory uses this estimate for sapwood in areas of England where it has no prior information. It

also uses it when dealing with samples with very many rings, about 120 to the last heartwood ring. But in other areas of England where the Laboratory has accumulated a number of samples with complete sapwood, that is, no sapwood lost since felling, other estimates in place of the conservative range of 15 to 35 are used. In the East Midlands (Laxton *et al*/2001) and the east to the south down to Kent (Pearson 1995) where it has sampled extensively in the past, the Laboratory uses the shorter estimate of 15 to 35 sapwood rings in 95% of mature oaks growing in these parts. Since the sample CRO-A06 comes from a house in Cropwell Bishop in the East Midlands, a better estimate of sapwood rings lost since felling is between a minimum of 6 (=15-9) and 26 (=35-9) and the felling would be estimated to have taken place between 1506 and 1526, a shorter period than before. Oak boards quite often come from the Baltic region and in these cases the 95% confidence limits for sapwood are 9 to 36 (Howard *et al* 1992, 56).

Even more precise estimates of the felling date and range can often be obtained using knowledge of a particular case and information gathered at the time of sampling. For example, at the time of sampling the dendrochronologist may have noted that the timber from which the core of Figure A2 was taken still had complete sapwood but that some of the soft sapwood rings were lost in coring. By measuring into the timber the depth of sapwood lost, say 20mm, a reasonable estimate can be made of the number of sapwood rings lost, say 12 to 15 rings in this case. By adding on 12 to 15 years to the date of the last ring on the sample a good tight estimate for the range of the felling date can be obtained, which is often better than the 15 to 35 years later we would have estimated without this observation. In the example, the felling is now estimated to have taken place between AD 1512 and 1515, which is much more precise than without this extra information.

Even if all the sapwood rings are missing on a sample, but none of the heartwood rings are, then an estimate of the felling-date range is possible by adding on the full complement of, say, 15 to 35 years to the date of the last heartwood ring (called the heartwood/sapwood boundary or transition ring and denoted H/S). Fortunately it is often easy for a trained dendrochronologist to identify this boundary on a timber. If a timber does not have its heartwood/sapwood boundary, then only a *post quem* date for felling is possible.

**5. Estimating the Date of Construction.** There is a considerable body of evidence collected by dendrochronologists over the years that oak timbers used in buildings were not seasoned in medieval or early modern times (English Heritage 1998; Miles 1997, 50–5). Hence, provided that all the samples in a building have estimated felling-date ranges broadly in agreement with each other, so that they appear to have been felled as a group, then this should give an accurate estimate of the period when the structure was built, or soon after (Laxton *et al*/2001, fig 8; 34–5, where ‘associated groups of fellings’ are discussed in detail). However, if there is any evidence of storage before use, or if there is evidence the oak came from abroad (eg Baltic boards), then some allowance has to be made for this.

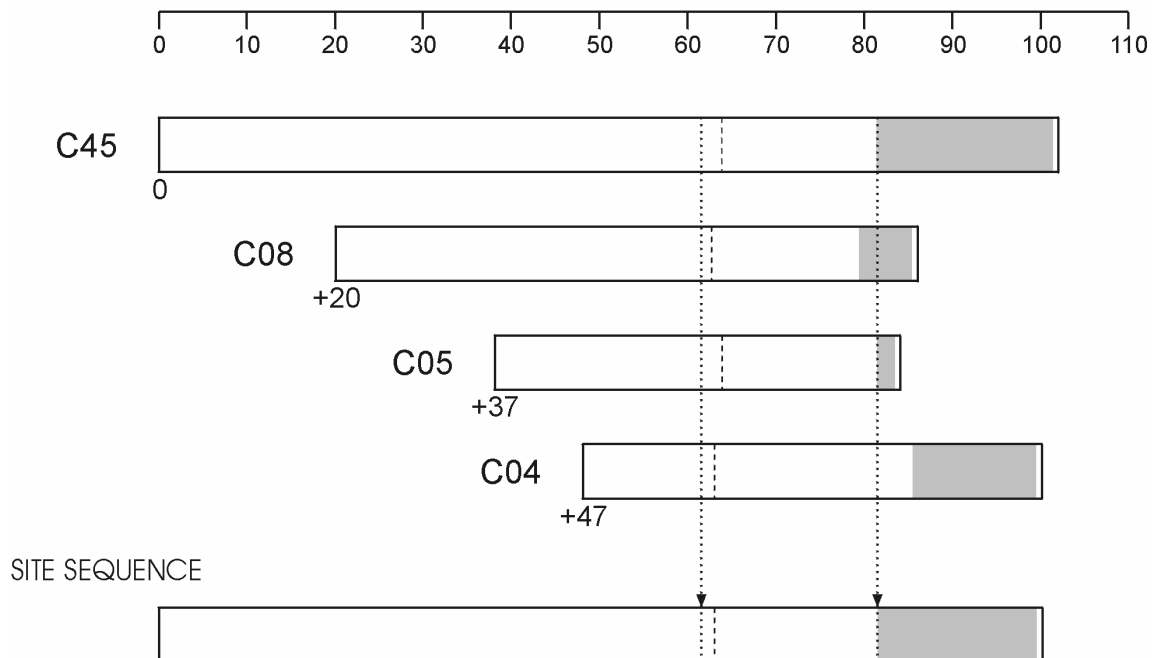
**6. Master Chronological Sequences.** Ultimately, to date a sequence of ring widths, or a site sequence, we need a master sequence of dated ring widths with which to cross-match it, a Master Chronology. To construct such a sequence we have to start with a sequence of widths whose dates are known and this means beginning with a sequence from an oak tree whose date of felling is known. In Figure A6 such a sequence is SHE-T, which came from a tree in Sherwood Forest which was blown down in a recent gale. After this other sequences which cross-match with it are added and gradually the sequence is 'pushed back in time' as far as the age of samples will allow. This process is illustrated in Figure A6. We have a master chronological sequence of widths for Nottinghamshire and East Midlands oak for each year from AD 882 to 1981. It is described in great detail in Laxton and Litton (1988), but the components it contains are shown here in the form of a bar diagram. As can be seen, it is well replicated in that for each year in this period there are several sample sequences having widths for that year. The master is the average of these. This master can now be used to date oak from this area and from the surrounding areas where the climate is very similar to that in the East Midlands. The Laboratory has also constructed a master for Kent (Laxton and Litton 1989). The method the Laboratory uses to construct a master sequence, such as the East Midlands and Kent, is completely objective and uses the Litton-Zainodin grouping procedure (Laxton *et al* 1988). Other laboratories and individuals have constructed masters for other areas and have made them available. As well as these masters, local (dated) site chronologies can be used to date other buildings from nearby. The Laboratory has hundreds of these site sequences from many parts of England and Wales covering many short periods.

**7. Ring-Width Indices.** Tree-ring dating can be done by cross-matching the ring widths themselves, as described above. However, it is advantageous to modify the widths first. Because different trees grow at different rates and because a young oak grows in a different way from an older oak, irrespective of the climate, the widths are first standardized before any matching between them is attempted. These standard widths are known as ring-width indices and were first used in dendrochronology by Baillie and Pilcher (1973). The exact form they take is explained in this paper and in the appendix of Laxton and Litton (1988) and is illustrated in the graphs in Figure A7. Here ring-widths are plotted vertically, one for each year of growth. In the upper sequence of (a), the generally large early growth after 1810 is very apparent as is the smaller later growth from about 1900 onwards when the tree is maturing. A similar phenomenon can be observed in the lower sequence of (a) starting in 1835. In both the widths are also changing rapidly from year to year. The peaks are the wide rings and the troughs are the narrow rings corresponding to good and poor growing seasons, respectively. The two corresponding sequence of Baillie-Pilcher indices are plotted in (b) where the differences in the immature and mature growths have been removed and only the rapidly changing peaks and troughs remain, that are associated with the common climatic signal. This makes cross-matching easier.

*t*-value/offset Matrix

	C45	C08	C05	C04
C45		+20	+37	+47
C08	5.6		+17	+27
C05	5.2	10.4		+10
C04	5.9	3.7	5.1	

Bar Diagram



**Figure A5: Cross-matching of four sequences from a Lincoln Cathedral roof and the formation of a site sequence from them**

The bar diagram represents these sequences without the rings themselves. The length of the bar is proportional to the number of rings in the sequence. Here the four sequences are set at relative positions (offsets) to each other at which they have maximum correlation as measured by the *t*-values. The *t*-value/offset matrix contains the maximum *t*-values below the diagonal and the offsets above it. Thus, the maximum *t*-value between C08 and C45 occurs at the offset of +20 rings and the *t*-value is then 5.6. The site sequence is composed of the average of the corresponding widths, as illustrated with one width

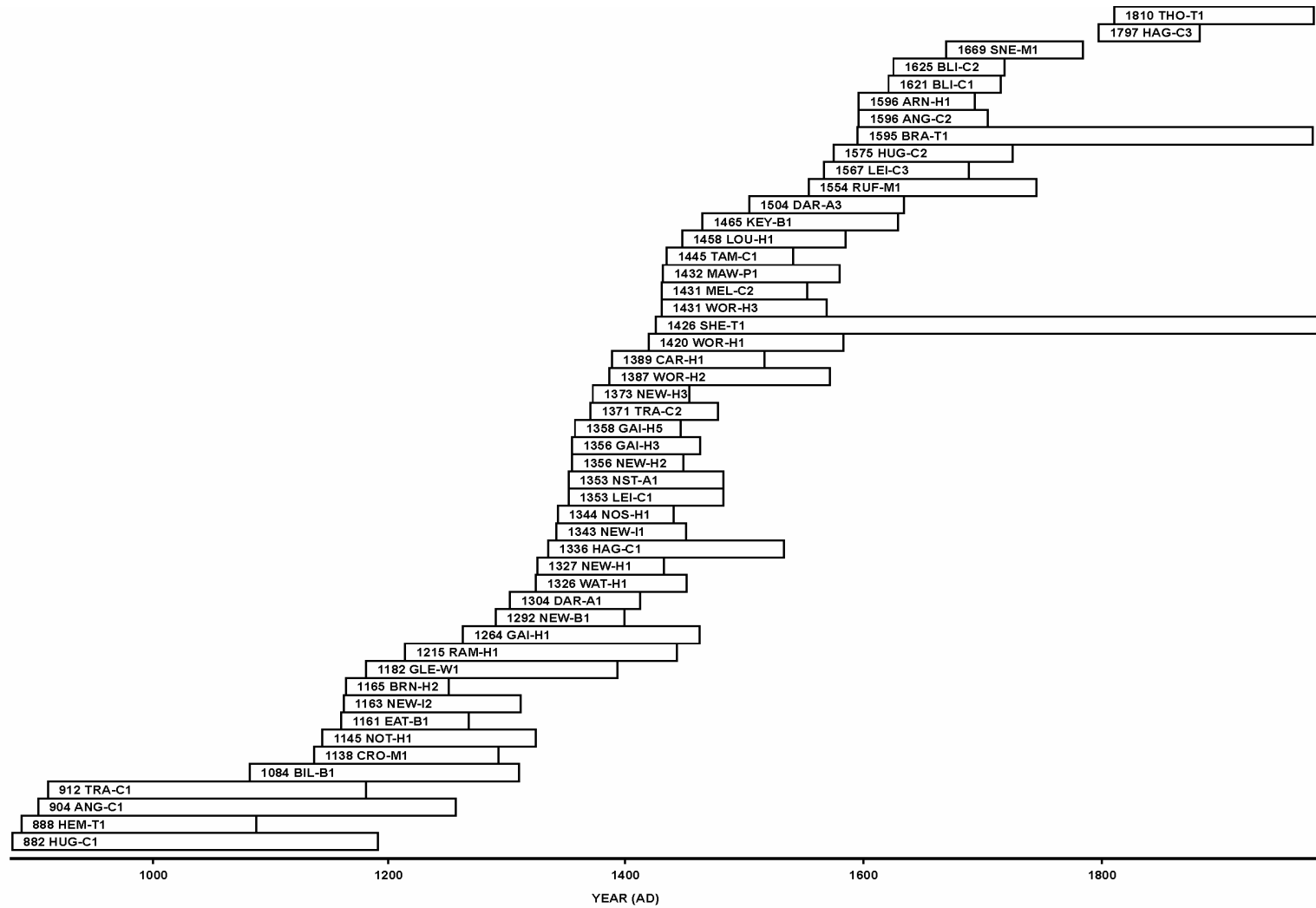
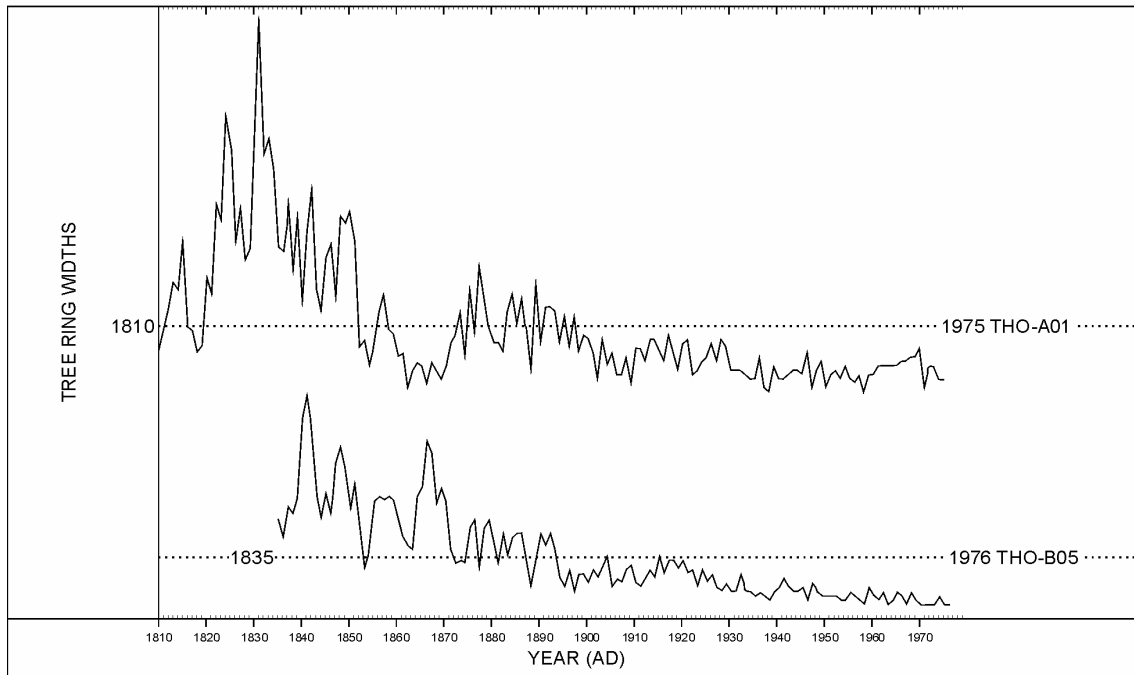
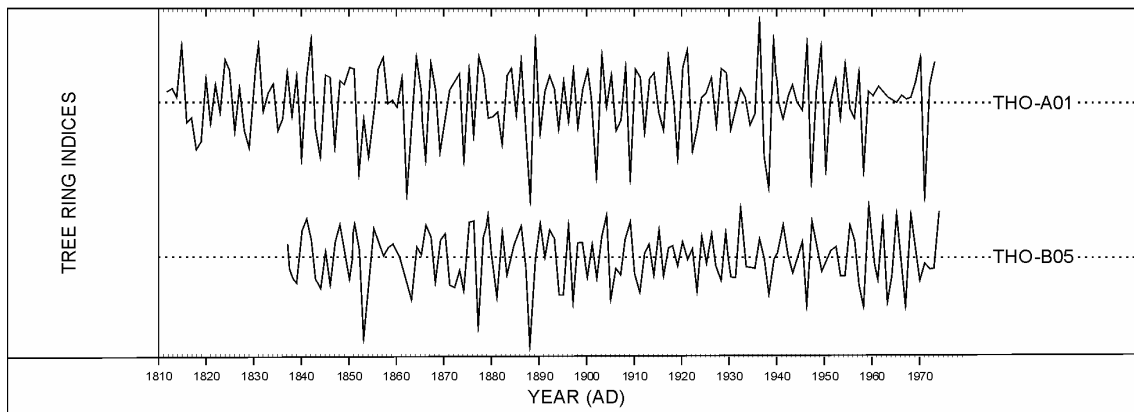


Figure A6: Bar diagram showing the relative positions and dates of the first rings of the component site sequences in the East Midlands Master Dendrochronological Sequence, EM08/87

(a)



(b)



**Figure A7 (a):** *The raw ring-widths of two samples, THO-A01 and THO-B05, whose felling dates are known*

Here the ring widths are plotted vertically, one for each year, so that peaks represent wide rings and troughs narrow ones. Notice the growth-trends in each; on average the earlier rings of the young tree are wider than the later ones of the older tree in both sequences

**Figure A7 (b):** *The Baillie-Pilcher indices of the above widths*

The growth trends have been removed completely



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