

# 46 HIGH STREET, EXETER, DEVON TREE-RING ANALYSIS OF TIMBERS

SCIENTIFIC DATING REPORT

Alison Arnold and Robert Howard



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**46 HIGH STREET,  
EXETER,  
DEVON**

## **TREE-RING ANALYSIS OF TIMBERS**

A J Arnold and R E Howard

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## **SUMMARY**

Dendrochronological analysis of 32 of the samples obtained predominantly from the roof and floor frames of 46 High Street, Exeter, has produced two site chronologies. The first site chronology comprises 25 samples, from the roof, floor frames, and a small number of other timbers, and has an overall length of 183 rings. These rings are dated as spanning the years AD 1309–1491. Interpretation of the sapwood on these samples indicates that all the timbers represented were probably cut as part of a single programme of felling, estimated to have taken place in AD 1492–1515.

The second site chronology comprises two samples with an overall length of 84 rings. This site chronology, and a further five ungrouped samples and one unmeasured sample, remain undated.

## **CONTRIBUTORS**

Alison Arnold and Robert Howard

## **ACKNOWLEDGEMENTS**

The Laboratory would like to thank Thorntons, the owners of 46 High Street Exeter, and their shop staff, for their cooperation with this programme of tree-ring analysis and their help during sampling. We would also like to thank the staff of St Blaise, conservation builders, for their considerable cooperation, help, and interest during sampling as well. We must also thank John Allan of Exeter Archaeology for his help and advice in respect of the phasing of this building, Richard Parker, also of Exeter Archaeology, for the use of his drawings, and Andy Pye, Planning Archaeologist at Exeter City Council, for his assistance with this programme of analysis. Finally we would like to thank Dr Peter Marshall, Scientific Dating Coordinator, for commissioning this programme of tree-ring dating.

## **ARCHIVE LOCATION**

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## **DATE OF INVESTIGATION**

2009

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## INTRODUCTION

According to the Exeter Urban Archaeological Database record (11183.00), from which this introduction is taken, the buildings now known as 46 and 47 High Street, Exeter (SX 92036 92650, Figs 1 and 2) represent an early, and now rare surviving, example of the construction of a pair of late/post-medieval, 'semi-detached', timber-framed houses as 'mirror images' of each other. The buildings are particularly unusual for Exeter in being entirely timber-framed, rather than the combination of stone side, or party walls, and timber transverse walls more common to the City, eg 41/42 High Street.

Superficially, the two now look very different to each other. While number 46, which is Grade II\* listed, retains most of its original façade (Fig 3), number 47 was refaced with render in the eighteenth century. Also, the street-front gable of number 46 has been replaced by a hipped roof. Internally, although the ground floors of both buildings have been extensively fitted out as shops, and little actual framing survives here other than some in the south-west wall of number 47, the upper floors of both retain much of their original fabric.

In plan (Fig 4) the buildings consist of two rooms to the main block, centred on a central stack and stair turret, with a further block to the rear. The jettied timber-framed frontage of number 46 once continued across number 47; this has carved angel figures (renewed) on the brackets, and a coved jetty with curving shafts ornamented with barley-twist fillets and pellets. The side elevation of number 46 was originally open to a narrow street called Lamb Alley, running between High Street and what is now known as Cathedral Yard, this elevation also being ornamented. The ground floors originally consisted of a shop at the front of each property, and domestic accommodation behind.

The typical framing style is of close-studding, with massive studs stretching from floor to ceiling on ground, first, and second floors. The original roof comprised seven bays formed by eight principal-rafter trusses (Fig 5) with chamfered tiebeams, there being double through-purlins to each pitch as well as a ridge to the apex. The pair of buildings has been variously dated from as early as AD 1500–40 by some authorities, to as late as AD 1550 by others, and there is a similar example, at 41/42 High Street, believed to have been built in the AD 1560s, but not dated by dendrochronology.

## SAMPLING

Sampling and analysis by dendrochronology of the timbers at number 46 High Street were requested by Francis Kelly, Historic Buildings Inspector at English Heritage's Bristol office. The primary purpose of this programme was to inform listed building consent as part of repairs and alterations to the structure. It was hoped that this analysis would establish the extent of the surviving primary phase elements and hence indicate with greater certainty the date of the initial construction of this house. This would place it, and

by inference its partner, more securely in the typological sequence of post-medieval development of this part of Exeter.

Thus, from the timbers available a total of 33 oak samples was obtained by coring. Each sample was given the code EXT-H (for Exeter, site 'H') and numbered 01–33. Fifteen of these samples, EXT-H01–15, were taken from the roof of number 46. A further 14 samples, EXT-H16–23, and EXT-H24–29, respectively, were obtained from the small areas of second and first floor-framing exposed immediately behind the west, or street frontage, gable (Fig 6a/b). A final four samples, EXT-H30–33, were obtained from a small selection of other timbers.

Given that additional timbers were in theory available for sampling, particular to the front rooms of both the first and second floors, the samples obtained in this programme of analysis might appear a little restricted in both location and element type. Sampling was constrained, however, by the small areas of floor-boarding that could be lifted and by the thinness of the wall studs (despite being broad), and the fact that they formed the immediate party wall, without any intervening void, to the properties to either side. A very small number of other timbers to the rear first and second floor might also have been available, but, being set deeply in ceilings, and in food preparation, storage, and sales areas, it was deemed inappropriate to core these timbers.

The location of samples was noted at the time of coring and, where possible, the exception being EXT-H32 from the gable header beam, marked on the drawings made by Richard Parker of Exeter Archaeology and provided by English Heritage, or on photographs taken at the time of sampling. These are reproduced here as Figures 7a–d. Further details relating to the samples can be found in Table 1. In this Table the trusses have been located and numbered following the scheme on the drawings provided, ie, from site east to site west, with individual timbers being further located on a north–south basis as appropriate.

## ANALYSIS

Each of the 33 samples obtained was prepared by sanding and polishing. It was seen at this time that one sample, EXT-H19, had less than the minimum of 54 rings necessary for reliable dating, and this sample was rejected from this programme of analysis. The annual growth-ring widths of the remaining 32 samples were, however, measured, the data of these measurements being given at the end of this report.

The data of the 32 measured samples were then compared with each other by the Litton/Zainodin grouping procedure (see Appendix), and at a minimum value of  $t=4.9$  two groups of cross-matching samples could be formed. The first group comprises 25 samples, cross-matching with each other as shown, sorted by sample location, in the bar diagram, Figure 8. These were combined at the indicated off-sets to form site chronology EXTHSQ01, this having an overall length of 183 rings. Site chronology EXTHSQ01 was then compared to an extensive series of reference chronologies for oak matching

repeatedly and consistently with a number of these when the date of its first ring is AD 1309 and the date of its last measured ring is AD 1491. The evidence for this dating is given in Table 2.

The second group comprises two samples, cross-matching with each other as shown in the bar diagram, Figure 9. These two samples were combined at the indicated off-sets to form site chronology EXTHSQ02, this having an overall length of 84 rings. Site chronology EXTHSQ02 was also compared to an extensive series of reference chronologies for oak, but there was no cross-matching and the samples must remain undated for the moment.

The two site chronologies, EXTHSQ01 and EXTHSQ02 were compared to each other, and with the five remaining measured but ungrouped samples. There was however no further satisfactory intra-site cross-matching, although some tenuous cross-matching was noted which would clearly require additional statistical support. The five ungrouped samples were then compared individually with the full series of reference chronologies but, again, there was no satisfactory cross-matching and all such individuals must, therefore, remain undated.

## INTERPRETATION

None of the dated samples in site chronology EXTHSQ01 retains complete sapwood, and it is thus not possible to indicate a precise felling date for any of the timbers represented. Fourteen of the 25 samples, however, do retain some sapwood, or at least the heartwood/sapwood boundary. It may be seen from Table 1 and the bar diagram, Figure 8, that this boundary varies by 18 years, from relative position 158, AD 1466, on sample EXT-H16, to relative position 176, AD 1484, on sample EXT-H26. Such consistency in the position of the heartwood/sapwood boundary is indicative of timbers representing a single programme of felling, with all the trees being cut at the same, or very similar, time.

The average date of the heartwood/sapwood boundary on these 14 dated samples is AD 1476. Using a 95% confidence interval of 15–40 years for the sapwood rings the trees might have had, and allowing that the latest dated ring on any sample, EXT-H02, is AD 1491, would give the timbers represented an estimated felling date in the range AD 1492–1516.

## CONCLUSION

The evidence of tree-ring dating suggests, therefore, that all the timbers dated in this programme of analysis were cut as part of a single episode of felling which took place between AD 1492 and AD 1516. Such a date would support the view that numbers 46 and 47 represent late-medieval developments of this part of Exeter, and date to the late fifteenth or early sixteenth century, slightly earlier than had been inferred previously.

It may be noted that the level of cross-matching between two samples, EXT-H02 and H07, at a value of  $t=13.7$ , is sufficiently high to suggest the likelihood that the two timbers represented, the south principals of trusses 2 and 4 respectively, are derived from the same tree, an interpretation supported by the probability that both beams appear to be half trees. A similar interpretation might also be made in respect of the timbers represented by samples EXT-H24 and H33, a first-floor joist and a main post respectively which cross-match with each other with a value of  $t=12.4$ . In this case, however, while the joist might be a halved, or indeed, a quartered tree, it seems most likely that the post is a whole tree trimmed down. The remaining intra-site cross-matching is such that it suggests that these timbers were likely to have been derived from a single, though potentially extensive, woodland source.

Where this source woodland was cannot be identified precisely by dendrochronology (eg Bridge 2000). However, it would appear that the timbers analysed are likely to have been derived from nearby sources. As may be seen from Table 2, which lists a short selection of the reference chronologies used to date site sequence EXTHSQ01, some of the highest  $t$ -values are with reference chronologies from other sites in Exeter itself or elsewhere in Devon.

A second sequence, comprising two samples, and five further individual samples, or just fewer than 16% of those obtained and measured, remain ungrouped and undated. None of these samples show any obvious problems with their annual growth rings, such as distortion, compression, or erratic growth, which would make cross-matching and dating difficult, and only two samples, EXT-H06 and H10, have numbers of rings which, although above the minimum of 54, are towards the lower end of the required figure. All other single samples have sufficient rings and show no peculiarities.



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## TABLES

*Table 1: Details of tree-ring samples from 46 High Street (Thornton's), Exeter, Devon*

Sample number	Sample location	Total rings	Sapwood rings	First measured ring date (AD)	Last heartwood ring date (AD)	Last measured ring date (AD)
Roof						
EXT-H01	Upper south purlin, truss 2–3	128	h/s	1347	1474	1474
EXT-H02	South principal rafter, truss 2	157	23	1335	1468	1491
EXT-H03	Tiebeam, truss 2	125	h/s	1352	1476	1476
EXT-H04	North principal rafter, truss 3	126	15	1362	1472	1487
EXT-H05	Tiebeam, truss 3	89	no h/s	1355	-----	1443
EXT-H06	North principal rafter, truss 4	57	15	-----	-----	-----
EXT-H07	South principal rafter, truss 4	106	no h/s	1331	-----	1436
EXT-H08	Tiebeam, truss 4	123	h/s	1360	1482	1482
EXT-H09	North lower purlin, truss 3–4	108	h/s	1372	1479	1479
EXT-H10	North principal rafter, truss 5	58	no h/s	-----	-----	-----
EXT-H11	South principal rafter, truss 5	85	no h/s	1355	-----	1439
EXT-H12	North principal rafter, truss 6	117	4	1364	1476	1480
EXT-H13	South principal rafter, truss 6	126	h/s	1353	1478	1478
EXT-H14	North principal rafter, truss 7	119	no h/s	-----	-----	-----
EXT-H15	North upper purlin, truss 6–7	73	2	1409	1479	1481

*Table 1: continued*

Sample number	Sample location	Total rings	Sapwood rings	First measured ring date (AD)	Last heartwood ring date (AD)	Last measured ring date (AD)
Second floor frame						
EXT-H16	Joist 2 (from north)	101	h/s	1366	1466	1466
EXT-H17	Joist 3	58	no h/s	-----	-----	-----
EXT-H18	Joist 4	86	no h/s	1379	-----	1464
EXT-H19	Joist 5	nm	---	-----	-----	-----
EXT-H20	Joist 6	88	4	1392	1475	1479
EXT-H21	Joist 7	84	no h/s	-----	-----	-----
EXT-H22	Joist 8	84	no h/s	-----	-----	-----
EXT-H23	Joist 9	81	no h/s	1384	-----	1464
First floor frame						
EXT-H24	Joist 3	86	no h/s	1369	-----	1454
EXT-H25	Joist 4	95	h/s	1384	1478	1478
EXT-H26	Joist 5	91	h/s	1394	1484	1484
EXT-H27	Joist 6	54	no h/s	1396	-----	1449
EXT-H28	Joist 7	69	no h/s	1378	-----	1446
EXT-H29	Joist 8	77	h/s	1407	1483	1483
Other timbers						
EXT-H30	South wall, stud post 1, first floor	126	no h/s	1309	-----	1432
EXT-H31	South wall, stud post 2, first floor	63	no h/s	-----	-----	-----
EXT-H32	West gable header beam, second floor	108	no h/s	1323	-----	1430
EXT-H33	North-west corner post, first floor	99	no h/s	1370	-----	1468

h/s = the heartwood/sapwood ring is the last ring on the sample

nm = sample not measured

*Table 2: Results of the cross-matching of site sequence EXTHSQ01 and relevant reference chronologies when the first-ring date is AD 1309 and the last-ring date is AD 1491*

Reference chronology	Span of chronology	t-value	Reference
West Challacombe, Devon	AD 1319–1452	8.6	( Tyers and Groves 1999 )
Kings Pyon barn, Herefordshire	AD 1346–1480	8.6	( Groves and Hillam 1993 )
The Mint, Exeter	AD 1350–1429	8.6	( Nayling 2001 )
Booth Hall/16–18 High Town, Hereford	AD 1302–1489	8.5	( Boswijk and Tyers 1997 )
Hampshire Chronology	AD 443–1972	8.2	( Miles 2003 )
Roscarrock, nr Port Isaac, Cornwall	AD 1373–1500	7.3	( Tyers 2004 )
66/68 Westgate Street, Gloucester	AD 1209–1518	6.9	( Tyers and Wilson 2000 )
Prowse barn, Sandford, Devon	AD 1380–1473	6.8	( Groves 2005 )

## FIGURES



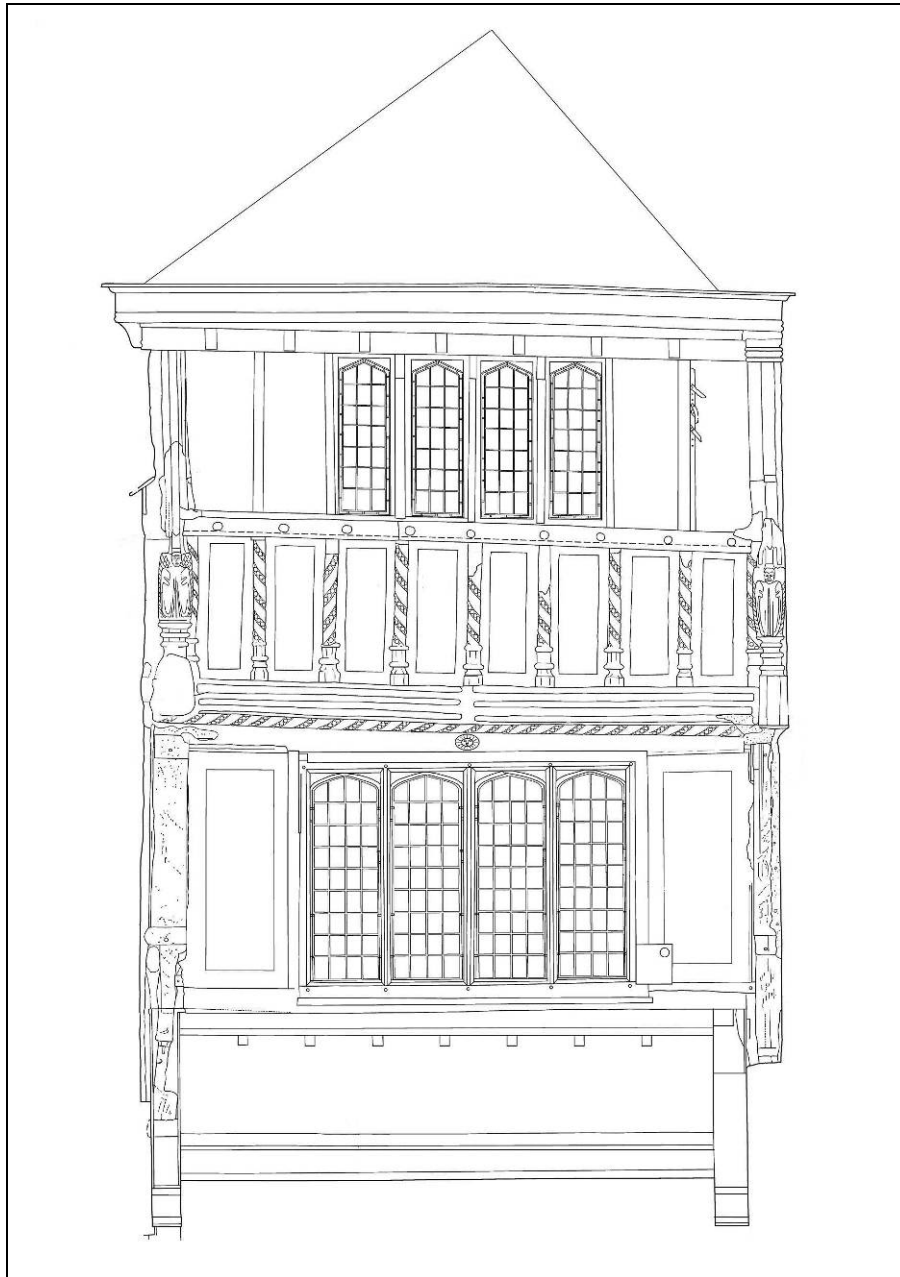
Figure 1: Map to show the location of Exeter

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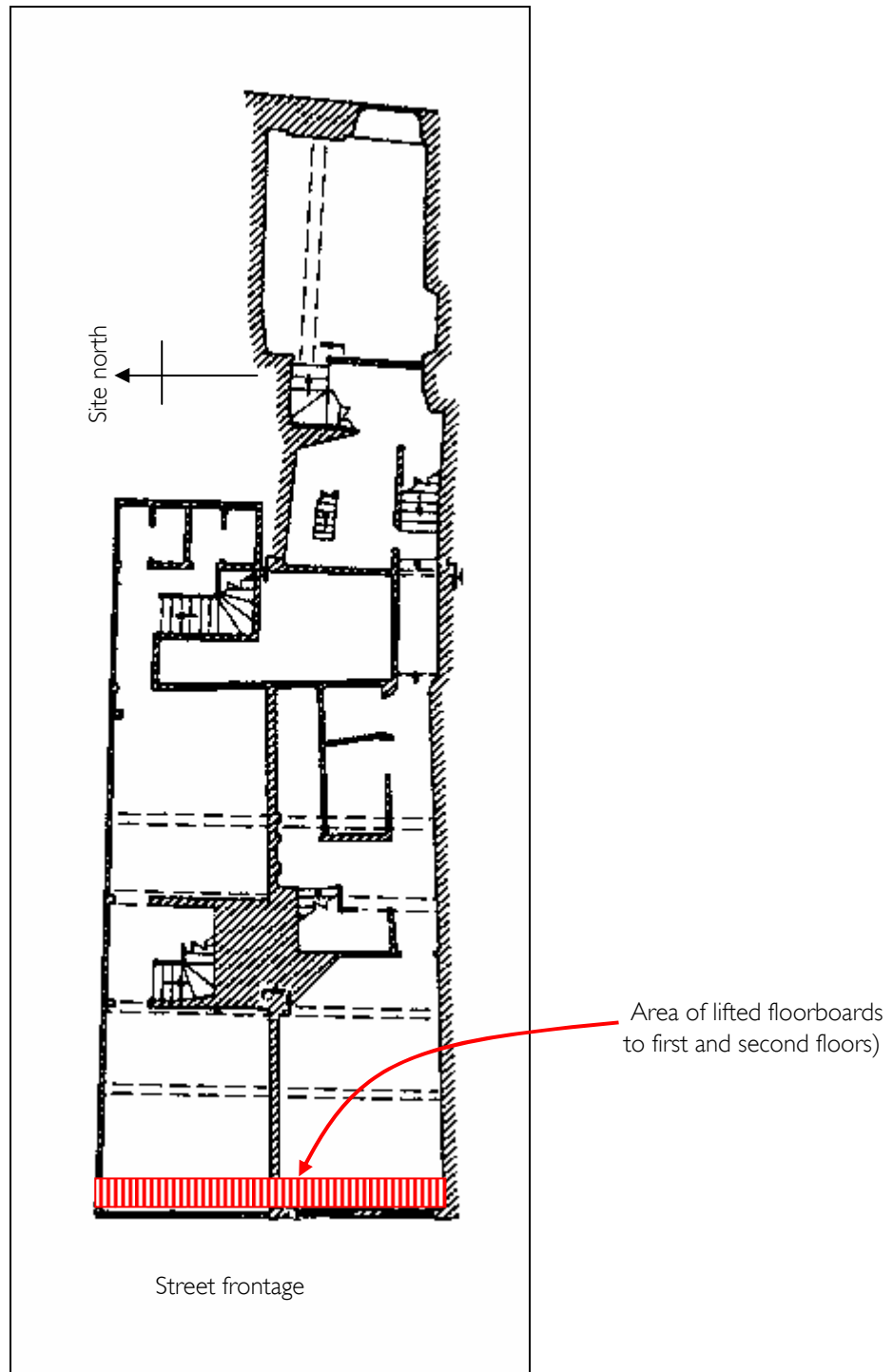


Figure 2: Map to show the location of 46 High Street, Exeter

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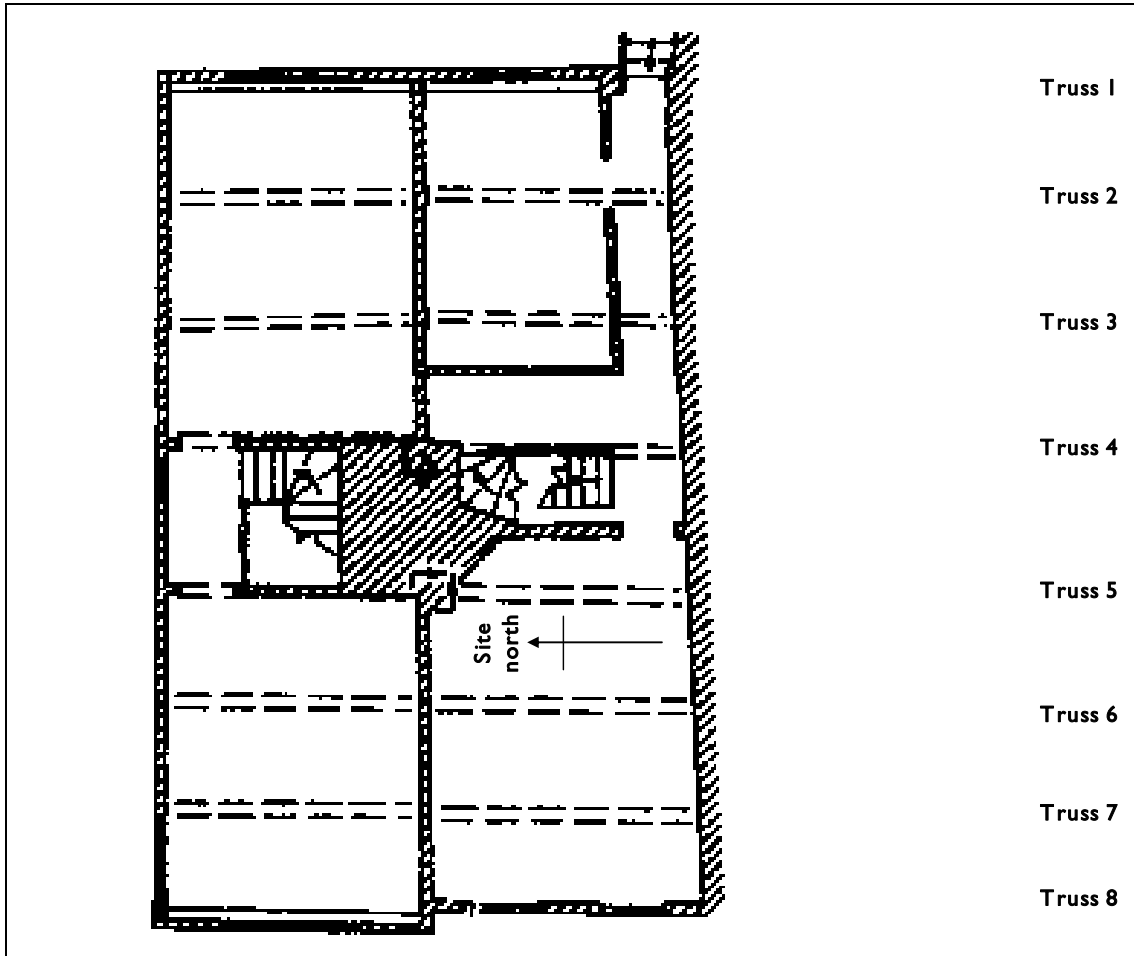


*Figure 3: Elevation of the upper floors of 46 High Street (after Richard Parker, Exeter Archaeology)*



*Figure 4: Plan of 46 High Street at first-floor level (after Richard Parker, Exeter Archaeology)*

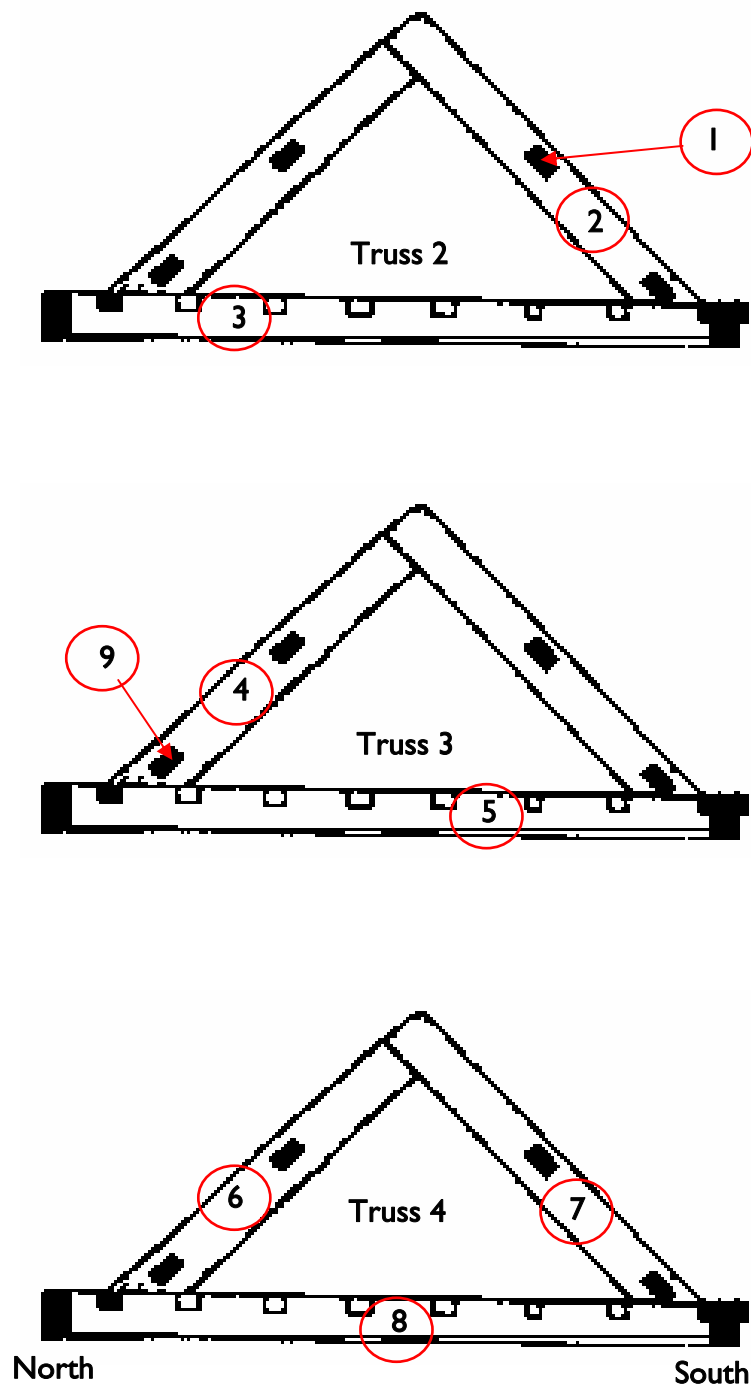




*Figure 5: Plan to show location of the trusses (after Richard Parker, Exeter Archaeology)*



*Figure 6a/b: View of the exposed joists to second (top) and first-floor frames (bottom)(viewed looking east to west)*



*Figure 7a: Trusses 2–4 to show sampled timbers (after Richard Parker, Exeter Archaeology)*

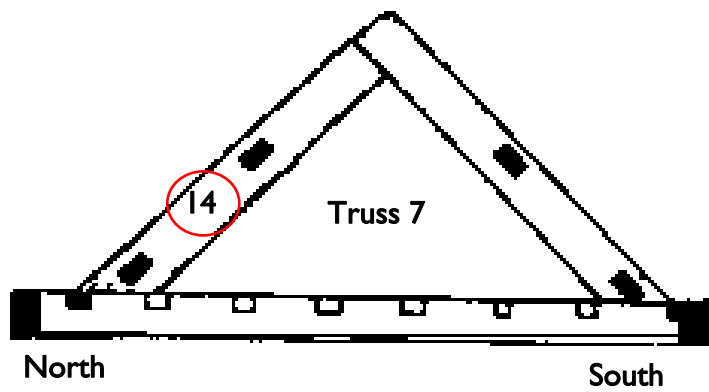
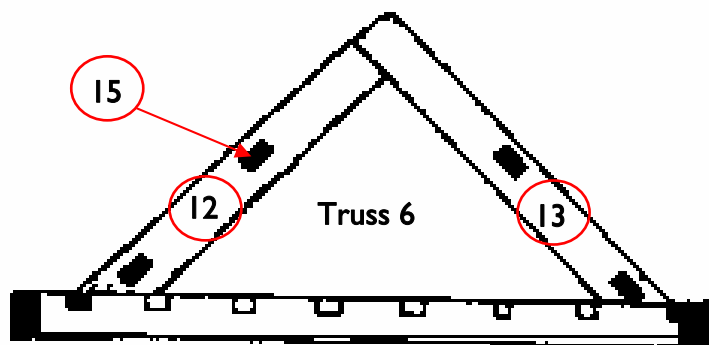
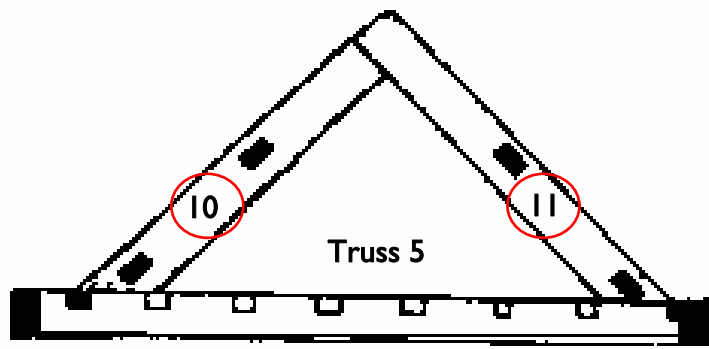


Figure 7b: Trusses 5–7 to show sampled timbers (after Richard Parker, Exeter Archaeology)

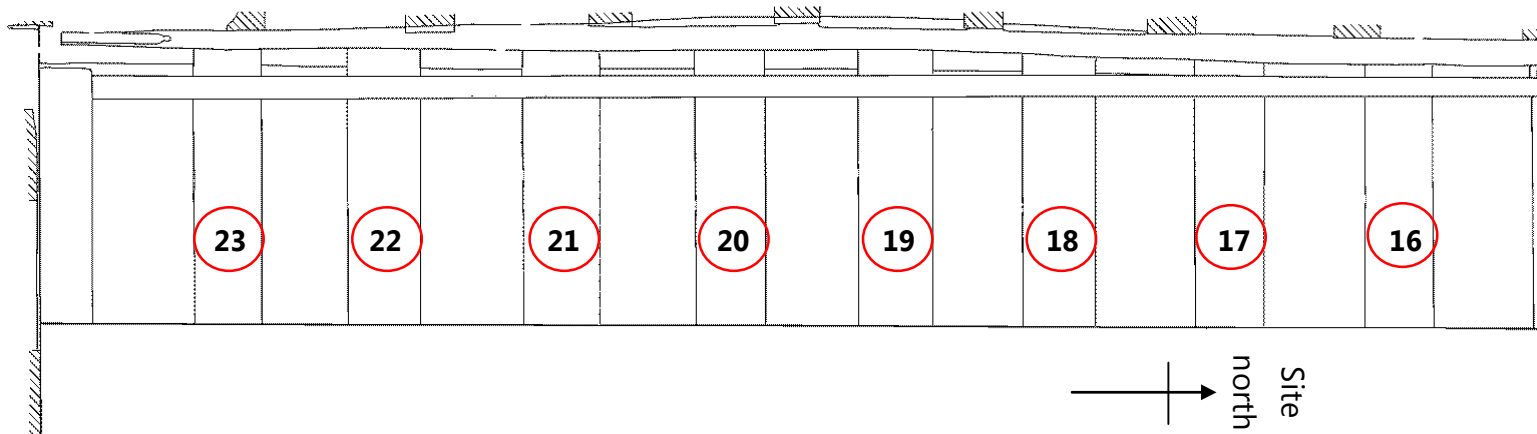


Figure 7c: Second-floor frame to show sampled timbers (after Richard Parker, Exeter Archaeology)

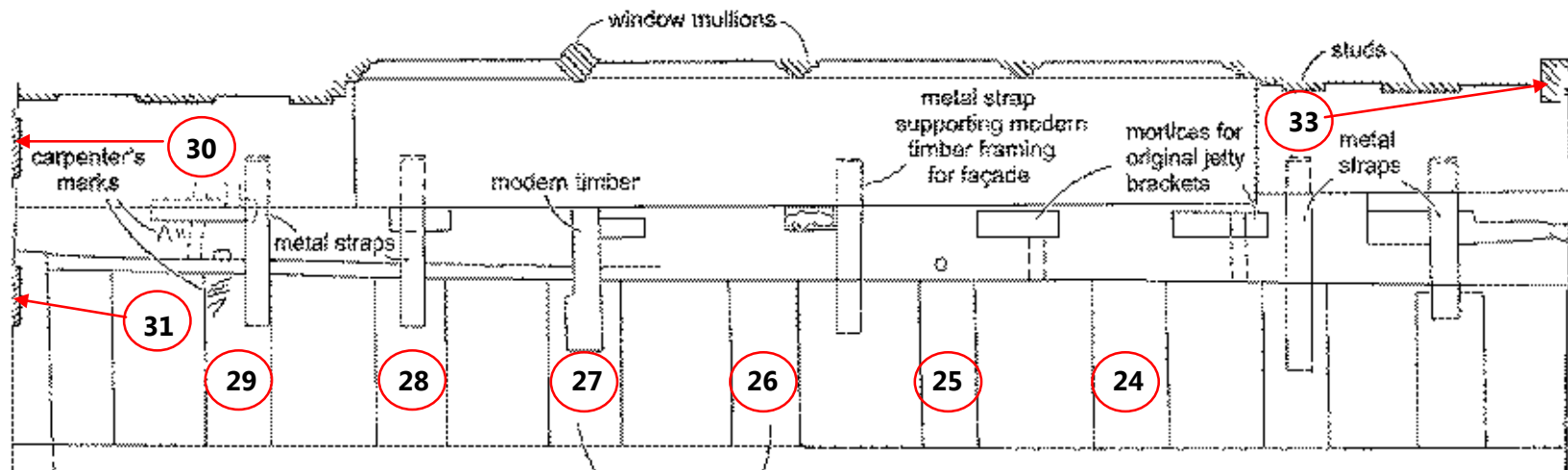
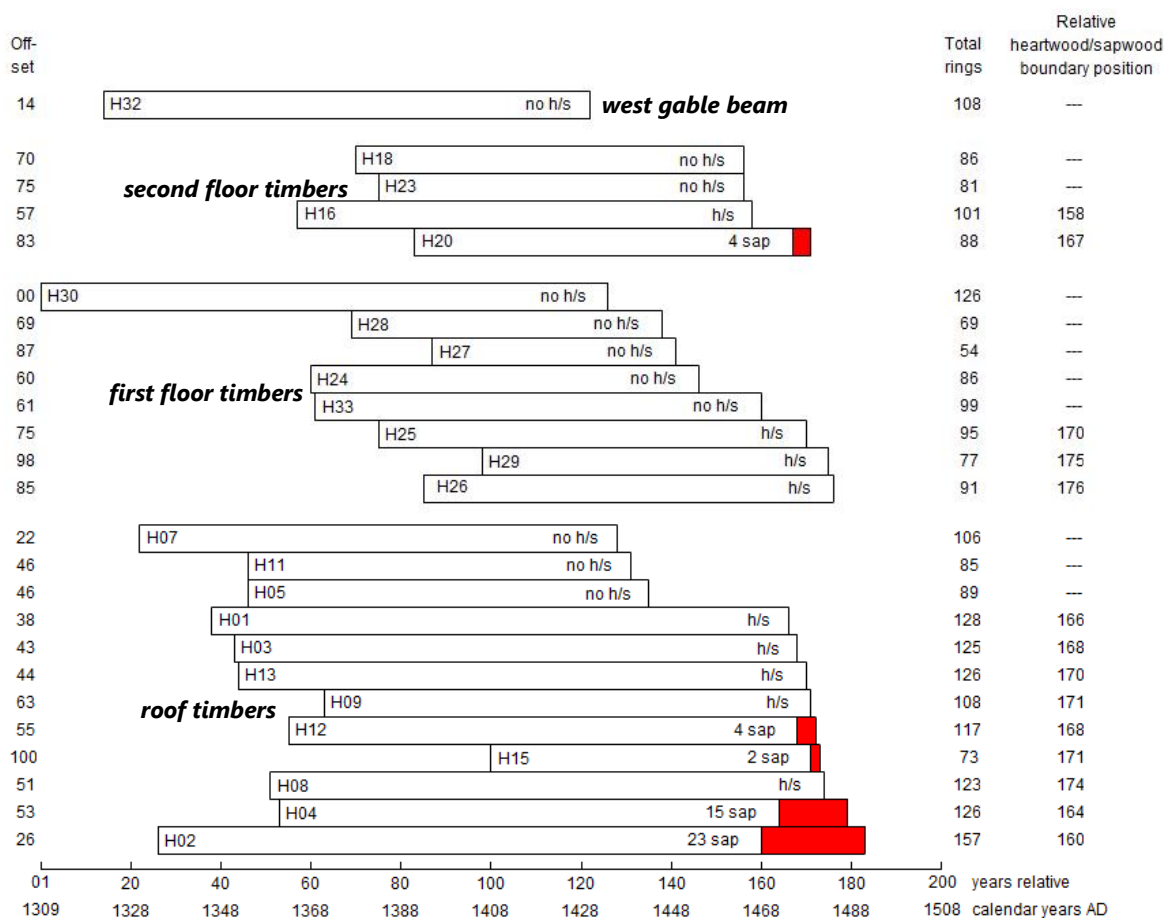


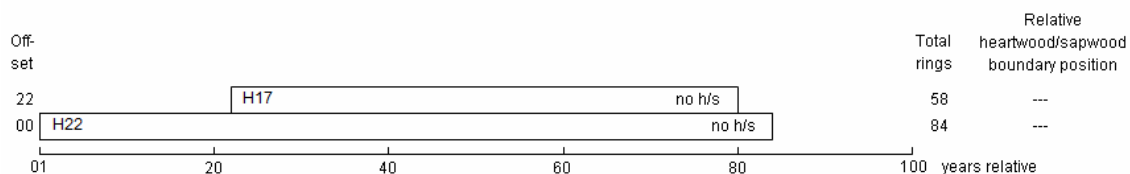
Figure 7d: First-floor frame to show sampled timbers (after Richard Parker, Exeter Archaeology)



White bars = heartwood rings, shaded area = sapwood rings

h/s = the last ring on the sample is at the heartwood/sapwood boundary; only the sapwood rings are missing

**Figure 8: Bar diagram of the samples in site chronology EXTSHQ01 sorted by sample location**



White bars = heartwood rings

h/s = the last ring on the sample is at the heartwood/sapwood boundary; only the sapwood rings are missing

**Figure 9: Bar diagram of the samples in site chronology EXTSHQ02**

## DATA OF MEASURED SAMPLES

Measurements in 0.01mm units

### EXT-H01A 128

168 158 269 177 255 177 172 174 174 159 136 78 113 112 202 126 255 198 165 185  
144 143 126 105 106 114 52 103 153 158 120 127 141 122 133 111 195 180 174 228  
163 162 112 98 105 103 94 77 57 92 89 111 116 99 115 112 153 152 145 101  
138 168 123 94 94 114 146 136 173 134 134 159 118 77 120 127 190 235 173 192  
162 146 142 136 131 133 138 101 124 94 113 125 84 84 86 109 91 135 90 82  
94 101 98 84 104 89 103 116 101 116 104 116 100 113 72 87 93 93 88 78  
123 115 80 106 99 102 113 137

### EXT-H01B 128

162 156 268 165 253 183 189 165 176 161 135 81 108 110 200 137 254 211 156 178  
148 136 129 110 100 111 56 95 166 158 119 132 127 126 132 117 184 185 175 220  
173 157 118 91 103 111 91 74 56 95 98 98 127 106 107 101 145 144 142 100  
134 163 128 95 94 112 149 130 153 129 130 141 116 84 114 131 195 260 152 172  
149 139 139 151 127 132 130 109 120 96 129 114 78 79 80 116 107 127 89 72  
79 107 105 90 97 85 103 123 101 112 102 115 93 105 78 76 109 87 89 78  
120 116 96 111 94 77 111 145

### EXT-H02A 157

187 177 115 158 142 120 89 101 78 84 90 75 106 107 187 257 440 190 175 222  
270 148 212 210 194 134 185 193 196 232 158 211 180 161 119 127 128 159 87 70  
121 105 91 92 164 109 88 109 124 83 91 133 82 90 75 69 71 73 95 99  
134 166 170 127 144 114 81 88 130 148 111 148 190 219 127 105 65 73 89 131  
118 71 115 106 73 98 126 78 155 150 131 98 89 92 70 95 146 263 200 188  
208 107 141 177 71 81 81 76 98 74 75 127 145 137 152 168 114 88 132 94  
115 207 152 144 79 118 115 96 107 109 135 113 88 108 130 163 144 99 112 93  
161 188 93 111 87 55 131 126 153 269 156 111 118 116 267 161 83

### EXT-H02B 157

164 174 110 173 133 125 101 104 83 70 92 102 120 136 207 279 434 181 170 224  
260 160 199 223 197 133 182 208 197 222 162 206 188 159 130 131 122 155 78 77  
123 108 85 99 167 99 88 113 114 91 98 129 93 80 76 70 72 84 95 92  
133 171 161 118 152 111 69 86 126 156 116 141 181 228 128 100 68 83 88 123  
117 67 122 110 70 93 138 69 157 149 138 99 76 96 65 104 139 269 210 195  
194 110 143 168 77 80 74 73 80 79 67 120 147 149 145 158 125 84 129 98  
119 199 162 135 66 118 122 102 96 115 129 110 74 113 122 157 142 102 109 94  
157 179 94 116 81 58 136 127 143 288 161 119 111 112 302 136 91

### EXT-H03A 125

336 503 488 247 338 284 468 415 260 330 498 444 347 296 373 371 309 421 181 283  
196 156 202 194 196 151 110 145 126 108 136 138 121 124 157 125 114 73 91 98  
113 109 72 110 136 108 120 132 109 131 112 89 100 81 157 111 121 144 58 100  
128 115 108 85 93 98 99 68 132 111 84 147 113 100 70 75 100 87 105 92  
150 139 149 201 104 108 55 74 64 110 76 71 64 88 73 85 142 143 153 180  
109 110 157 137 168 142 132 85 84 65 98 108 78 108 104 115 123 113 100 122  
89 85 129 118 134

### EXT-H03B 125

398 496 487 209 326 279 466 417 249 339 495 448 348 278 368 360 338 386 198 260  
201 159 204 164 210 156 103 144 111 122 142 147 134 123 163 127 116 67 88 98  
110 105 71 102 131 121 108 137 113 117 120 90 91 97 141 120 114 137 64 99  
116 120 127 90 86 98 87 64 135 117 73 149 112 97 80 95 105 73 105 103  
149 127 155 197 103 100 72 69 67 108 86 70 70 80 74 84 139 133 163 172

112 109 145 147 163 138 138 78 80 76 97 101 86 91 116 126 114 114 113 90  
89 87 134 124 141

EXT-H04A 126

387 426 388 271 383 345 338 325 327 213 181 173 154 206 262 236 248 287 324 214  
208 150 154 115 137 141 151 134 108 85 77 85 68 97 114 121 119 142 170 174  
113 124 160 187 188 183 188 175 92 70 95 88 144 131 124 90 117 91 104 148  
102 169 155 124 129 121 141 118 109 89 143 112 133 146 131 150 136 81 103 117  
97 112 135 116 97 109 121 109 98 119 99 100 111 87 93 93 124 111 133 99  
98 116 114 100 72 83 97 95 121 100 104 95 104 104 135 108 80 97 102 115  
171 172 208 179 223 265

EXT-H04B 126

386 453 390 273 376 347 332 318 302 210 178 176 163 174 244 250 231 278 312 199  
215 145 153 120 138 135 151 129 112 90 85 78 71 88 125 114 131 153 169 169  
116 123 156 177 198 174 200 168 97 68 95 81 141 131 105 89 104 90 104 150  
109 146 155 129 131 115 144 123 108 103 128 111 124 145 125 155 132 78 104 126  
93 109 135 112 93 115 112 108 101 104 112 103 112 101 106 90 132 103 138 96  
104 119 124 87 78 81 95 88 116 105 122 89 95 101 136 107 82 89 92 105  
185 186 204 197 222 259

EXT-H05A 89

221 373 280 430 379 240 325 468 461 326 294 354 359 318 298 171 282 233 194 277  
165 233 124 134 176 156 134 142 132 168 169 203 191 222 177 102 126 116 125 111  
113 125 105 107 117 102 82 91 99 92 102 168 98 130 93 57 80 73 89 126  
77 78 72 46 52 112 116 97 110 109 107 85 83 62 63 85 95 170 97 121  
175 94 156 82 99 67 114 107 141

EXT-H05B 89

230 371 283 426 384 237 322 480 449 345 286 328 374 309 300 195 273 233 195 248  
198 220 101 133 168 149 129 147 142 166 165 220 201 209 168 120 136 123 157 119  
117 114 116 115 110 99 90 80 103 101 95 170 96 130 97 57 74 76 83 128  
80 78 74 46 58 103 120 103 107 112 105 78 83 66 70 76 97 154 114 127  
174 96 150 88 104 59 124 105 141

EXT-H06A 57

195 133 132 164 254 350 246 308 218 198 191 216 251 428 320 228 147 427 189 221  
134 278 232 255 306 450 297 358 259 167 173 158 303 308 249 261 223 145 245 551  
328 317 611 365 234 478 413 464 253 119 236 239 258 542 522 343 392

EXT-H06B 57

224 140 125 176 240 324 273 308 225 195 187 222 251 458 290 250 134 411 201 221  
120 290 231 278 345 420 295 366 266 148 177 156 308 323 231 258 226 131 264 530  
296 323 591 351 263 491 395 598 254 116 226 245 219 503 548 341 390

EXT-H07A 106

121 175 252 201 209 172 155 244 190 181 129 174 132 141 143 86 89 89 104 153  
210 124 186 171 230 108 133 167 202 162 186 174 160 289 187 262 251 150 134 161  
153 175 105 95 115 104 117 158 224 142 114 117 112 111 106 190 120 109 104 63  
117 125 196 151 190 214 181 143 202 150 85 65 118 141 129 134 183 217 137 121  
58 81 86 172 152 73 126 129 79 107 152 70 182 179 122 75 97 154 100 212  
314 407 238 277 385 164

EXT-H07B 106

137 194 262 180 225 152 159 239 200 201 143 173 116 137 149 88 86 84 103 152  
222 130 181 192 242 104 135 166 190 164 189 180 159 288 197 252 259 146 129 164  
136 185 110 99 101 114 111 157 216 140 120 123 103 110 103 196 117 106 98 73  
127 133 181 135 201 210 162 144 203 153 77 75 124 136 132 125 191 207 139 99  
67 78 93 154 142 76 123 111 76 102 159 87 175 183 125 87 102 145 100 204  
313 391 249 266 388 170

EXT-H08A 123



187 240 185 213 236 249 203 273 300 338 267 232 233 226 286 284 236 257 214 279  
229 193 207 219 207 210 357 305 315 258 173 139 163 124 122 133 163 155 174 206  
180 266 150 161 179 171 205 210 196 211 199 172 193 183 198 207 147 166 135 106  
170 161 148 175 174 162 117 119 156 140 141 133 181 148 129 156 135 130 93 81  
89 123 136 102 102 91 93 125 139 118 112 109 117 84 76 115 107 125 132 104  
147 156 109 137 124 117 124 171 130 147 130 126 119 111 122 139 104 90 73 87  
123 120 160

EXT-H08B 123

168 227 204 191 255 223 199 303 293 376 297 234 239 223 285 287 254 254 231 280  
226 198 209 224 208 227 343 268 325 242 158 146 156 125 124 137 157 153 183 194  
185 277 132 173 209 168 229 195 199 220 203 167 187 189 201 213 144 170 136 100  
156 167 164 184 186 166 134 116 169 147 134 133 185 145 122 164 147 129 100 77  
93 107 136 104 100 95 92 121 133 120 120 110 118 86 80 107 114 135 127 109  
151 135 131 135 119 118 110 147 145 135 131 127 114 121 124 152 116 72 85 94  
128 120 161

EXT-H09A 108

166 178 168 151 147 127 127 174 151 125 158 123 145 162 212 139 157 124 114 106  
73 94 83 89 106 85 87 89 115 137 107 110 123 89 103 128 137 142 118 97  
97 119 120 131 88 79 91 71 97 122 87 151 175 94 89 98 103 71 74 91  
137 77 106 105 88 91 65 58 68 78 68 63 71 65 53 59 61 62 59 67  
46 51 69 55 78 71 82 84 102 101 99 86 101 92 82 93 98 89 90 96  
81 121 101 87 87 86 110 148

EXT-H09B 108

193 155 160 153 150 115 131 174 172 125 156 135 145 159 201 157 153 129 108 116  
67 91 86 88 111 79 90 97 118 137 106 110 128 86 99 128 142 146 114 95  
89 122 120 140 79 79 99 77 93 117 82 146 153 116 102 97 101 77 84 86  
139 90 117 100 77 105 64 58 62 87 67 67 72 60 53 61 68 64 54 61  
43 66 74 57 82 73 86 91 104 105 103 86 98 93 81 93 90 98 86 86  
94 105 98 100 79 98 97 151

EXT-H10A 58

178 166 176 271 248 326 213 260 237 204 159 202 189 297 256 273 149 194 174 161  
267 198 210 157 228 156 240 293 245 164 260 124 171 138 194 152 146 222 253 270  
194 175 130 110 154 184 192 224 208 273 310 158 86 131 154 231 212 123

EXT-H10B 58

160 155 190 280 245 324 225 256 237 213 162 206 197 298 252 244 177 197 167 155  
220 251 189 160 217 191 233 256 263 156 257 115 176 143 195 143 149 207 268 270  
201 176 132 123 144 178 179 237 204 270 313 147 88 128 145 222 220 102

EXT-H11A 85

254 382 337 296 237 198 288 245 287 302 197 191 266 211 392 278 187 222 209 251  
277 321 271 332 336 317 297 246 279 239 202 269 212 224 229 164 156 189 229 147  
155 202 155 177 204 166 225 163 175 190 165 143 164 169 148 150 160 177 163 188  
192 136 146 125 122 191 168 157 146 154 135 111 78 115 91 90 103 101 118 98  
130 117 107 109 106

EXT-H11B 85

293 382 330 300 244 206 289 230 288 295 181 204 251 233 382 282 199 224 194 243  
276 332 239 343 309 346 325 264 264 215 215 306 239 218 253 163 138 178 209 132  
157 205 144 166 189 156 220 178 169 194 162 152 158 172 147 137 161 177 173 191  
187 143 144 135 126 188 160 148 160 157 132 112 77 119 80 98 107 97 114 96  
129 122 108 112 101

EXT-H12A 117

278 193 162 185 245 263 196 162 155 162 171 199 204 147 229 222 185 186 147 210  
136 146 137 118 169 158 118 139 112 127 95 113 171 136 122 109 126 155 103 135  
100 89 122 122 128 106 85 95 105 131 111 103 94 101 90 98 109 133 98 104

101 71 65 57 76 60 60 87 115 102 84 102 76 81 71 94 92 65 61 66  
87 72 77 106 87 81 95 80 98 96 135 147 119 164 153 133 111 126 105 131  
74 78 90 66 61 54 63 65 67 70 62 92 102 79 116 116 127

EXT-HI2B 117

270 190 161 190 249 265 193 170 150 162 171 195 213 146 234 206 192 185 147 225  
126 145 143 118 172 161 115 133 121 129 105 103 172 136 120 114 118 145 112 122  
113 89 113 128 129 102 94 102 104 135 86 124 90 99 99 93 112 160 98 102  
98 71 75 56 73 65 56 92 102 93 88 92 75 83 91 105 64 72 72 77  
78 72 80 111 91 84 99 90 91 104 149 151 148 174 151 108 138 141 114 112  
90 76 86 67 65 58 66 61 61 79 60 90 101 90 111 98 122

EXT-HI3A 126

401 472 316 399 343 417 337 213 282 289 282 230 194 217 242 281 344 258 239 207  
198 201 254 289 231 286 311 217 165 211 184 186 174 276 187 206 156 71 94 118  
95 95 96 172 147 114 162 141 145 124 153 105 125 112 116 113 188 85 101 153  
164 159 106 78 95 142 104 122 115 84 82 89 77 79 60 87 57 62 80 80  
91 95 114 59 51 61 56 84 79 61 75 93 51 66 92 74 70 52 64 61  
60 63 87 107 120 99 55 87 90 109 103 110 100 109 140 110 96 119 105 88  
105 99 228 134 99 125

EXT-HI3B 126

409 479 318 401 343 412 351 204 282 293 278 236 211 220 243 283 359 282 217 206  
195 197 250 299 230 286 305 221 160 205 190 183 186 263 195 197 160 83 84 120  
102 96 91 170 148 120 148 138 155 108 150 113 126 118 109 128 187 89 93 150  
154 155 108 70 96 142 112 132 111 77 83 85 91 72 63 76 63 72 68 95  
89 78 120 65 54 49 57 88 78 64 68 96 46 72 85 81 67 56 67 64  
62 65 85 111 119 95 61 83 105 98 105 118 107 91 149 110 105 115 109 93  
125 90 207 144 103 126

EXT-HI4A 119

319 361 332 227 280 379 318 279 279 253 257 283 297 262 214 212 173 241 199 77  
92 150 197 176 172 153 142 165 153 172 177 164 124 118 74 79 77 79 88 134  
103 104 122 119 152 119 107 91 87 84 105 124 99 93 69 99 98 94 90 93  
93 112 91 102 104 102 102 90 87 84 78 80 89 52 55 67 72 57 71 70  
60 57 42 44 49 61 54 52 50 49 56 66 64 69 69 74 78 74 89 105  
117 103 102 114 90 119 89 117 126 177 274 228 116 189 205 206 237 175 258

EXT-HI4B 119

313 355 312 274 319 364 280 273 260 261 276 297 312 267 217 205 168 252 191 78  
94 149 203 175 171 135 145 157 138 183 174 161 130 122 68 80 68 83 93 117  
106 98 112 124 147 114 112 85 89 86 98 117 105 89 79 89 102 95 83 97  
98 107 96 104 106 106 93 90 84 85 70 86 84 59 45 68 80 55 70 70  
71 54 44 50 48 58 53 65 42 51 68 57 71 70 72 74 75 66 89 108  
115 124 96 107 95 111 101 108 122 180 258 231 119 193 204 213 229 178 260

EXT-HI5A 73

265 164 201 214 233 276 417 185 157 255 129 228 148 172 329 230 250 177 166 173  
152 140 153 228 191 220 187 150 185 156 72 132 145 155 174 170 166 136 180 111  
139 118 139 131 117 188 145 219 165 147 136 184 178 111 153 117 163 150 165 189  
171 161 133 146 154 191 191 171 145 148 160 143 160

EXT-HI5B 73

277 157 200 191 229 291 416 182 152 266 145 233 147 179 330 234 249 194 156 143  
158 162 152 234 199 194 174 166 199 156 71 137 124 147 149 169 155 142 171 135  
136 113 141 144 122 178 145 220 172 142 146 195 152 124 151 107 162 155 163 180  
183 165 124 150 152 198 177 178 143 142 165 142 166

EXT-HI6A 101

282 265 141 195 184 147 161 95 107 158 111 101 117 228 425 445 295 350 418 348  
403 292 372 318 204 204 203 151 162 248 254 153 130 191 224 220 152 199 182 188

222 254 306 278 92 88 182 234 196 257 163 209 194 126 91 207 206 191 276 206  
172 179 172 176 155 215 166 141 109 343 173 234 199 134 178 171 158 130 189 120  
158 114 120 112 85 90 94 77 150 115 157 128 135 106 109 96 78 94 118 100  
118

EXT-H16B 101

293 255 166 189 183 138 158 99 116 143 103 99 116 226 440 466 290 341 413 347  
387 295 373 327 202 195 198 160 161 240 255 152 129 176 199 214 167 194 182 214  
200 255 310 270 85 101 195 216 202 285 147 206 204 123 92 208 216 170 282 207  
168 190 175 171 163 207 170 131 98 340 180 234 194 126 184 166 160 124 196 113  
165 108 117 115 84 95 91 82 152 110 156 124 133 107 108 90 93 88 133 95  
99

EXT-H17A 58

724 450 412 301 376 212 292 278 313 529 192 133 159 138 227 90 94 121 120 126  
130 107 108 229 200 155 176 265 227 177 209 267 277 289 278 209 148 137 129 185  
247 185 183 132 224 166 111 168 210 125 148 149 166 160 157 184 165 166

EXT-H17B 58

746 431 438 335 391 183 289 256 333 534 192 133 151 142 220 92 99 132 116 127  
137 101 116 211 208 149 201 252 208 185 198 280 270 281 280 230 132 136 136 186  
239 176 176 132 219 148 114 160 210 119 128 153 192 166 153 191 200 172

EXT-H18A 86

249 259 217 206 291 256 262 274 225 237 191 187 202 168 167 179 156 266 196 269  
282 330 225 199 209 228 208 251 294 251 269 197 147 225 341 310 318 260 224 289  
182 177 208 180 215 199 201 208 159 176 143 174 213 229 170 192 237 219 268 191  
122 130 132 141 160 168 157 130 153 190 168 142 152 135 150 190 162 168 155 176  
173 137 147 142 135 178

EXT-H18B 86

302 257 218 200 323 248 252 274 230 241 230 174 198 162 167 184 147 265 226 226  
302 321 193 220 226 194 219 241 293 248 280 183 172 207 353 310 305 257 228 277  
178 166 216 182 214 202 200 205 158 179 154 165 214 226 178 196 233 215 279 183  
121 135 125 147 156 170 138 132 147 187 155 146 160 135 148 182 164 158 157 174  
166 134 152 132 111 165

EXT-H20A 88

328 282 242 380 339 354 347 311 253 316 276 372 384 339 335 349 341 187 192 112  
200 216 210 247 158 228 164 138 110 245 165 209 247 129 227 218 232 217 210 229  
209 151 144 169 158 155 171 95 150 126 117 108 131 51 144 159 143 115 139 151  
127 115 149 140 164 142 137 113 108 113 159 158 151 123 176 152 178 203 244 210  
192 175 166 216 123 192 164 203

EXT-H20B 88

331 291 245 375 337 360 355 308 244 312 296 385 386 333 339 333 346 181 202 109  
195 227 207 243 175 211 195 144 134 204 161 205 248 131 240 196 227 230 210 223  
210 150 139 170 154 149 177 92 144 135 119 113 123 58 145 156 142 114 128 149  
131 120 158 124 165 134 141 112 113 110 156 159 161 111 155 164 177 209 230 203  
173 166 160 204 110 207 161 181

EXT-H21A 84

324 523 593 442 471 320 283 427 331 264 268 188 237 300 400 301 221 221 112 176  
190 204 166 148 151 86 139 183 187 217 261 252 179 171 160 164 92 232 135 87  
57 74 90 88 124 108 131 162 139 144 85 69 71 77 169 160 190 59 100 174  
190 75 51 93 122 187 135 107 94 101 62 62 81 79 116 160 120 123 127 110  
84 91 123 211

EXT-H21B 84

316 522 609 432 475 327 293 421 330 267 269 169 242 302 390 317 226 230 132 150  
179 202 168 150 151 87 139 185 196 228 272 252 174 171 160 158 102 214 128 79  
56 82 85 96 125 112 123 158 136 149 77 64 77 86 164 169 199 72 107 214

175 87 47 86 106 204 146 101 104 96 67 52 90 68 115 158 126 126 123 107  
84 83 111 245

EXT-H22A 84

336 289 311 307 255 243 232 304 313 353 323 389 304 360 353 568 411 398 402 334  
260 334 340 275 280 219 266 178 219 203 177 203 107 138 185 165 182 117 130 154  
171 139 125 92 125 143 177 132 157 207 177 154 172 193 187 179 204 181 190 151  
167 248 190 159 155 197 283 233 261 233 274 292 290 269 211 188 224 221 213 309  
246 194 294 420

EXT-H22B 84

320 301 302 307 260 232 239 302 288 351 329 381 305 368 361 560 392 408 417 326  
268 319 348 274 285 219 280 179 216 196 179 210 106 139 159 167 170 117 132 156  
160 130 129 95 123 133 187 133 155 225 181 148 182 190 188 177 201 192 179 157  
177 240 192 163 172 187 290 267 257 263 284 279 292 277 219 181 233 224 209 315  
207 221 276 443

EXT-H23A 81

271 263 242 175 200 171 129 180 115 292 138 230 291 206 203 290 265 306 210 238  
317 198 242 198 204 202 175 132 146 211 198 183 118 150 197 112 146 217 148 224  
273 291 239 207 290 137 123 196 285 199 214 269 280 461 486 214 348 389 245 218  
166 224 172 295 233 221 227 149 116 110 230 222 244 197 215 190 306 227 149 230  
369

EXT-H23B 81

225 270 244 159 209 179 157 156 116 259 186 281 279 201 226 279 259 309 213 240  
302 208 222 203 187 207 177 129 133 218 195 185 123 162 186 134 152 224 151 218  
267 290 246 196 300 136 138 195 290 198 206 258 271 481 467 200 364 403 238 227  
163 230 162 300 248 231 204 146 119 112 234 223 246 169 224 186 305 227 161 202  
355

XT-H24A 86

191 150 150 121 140 150 158 273 170 200 247 148 121 153 198 85 71 188 175 207  
133 52 65 84 198 120 162 211 123 218 202 202 166 132 113 166 174 201 159 184  
166 104 96 188 252 317 313 153 153 173 129 275 222 134 335 261 230 223 68 120  
103 143 201 247 211 234 360 208 183 152 207 268 266 161 172 219 109 112 189 179  
241 455 386 177 106 273

EXT-H24B 86

200 154 133 123 145 150 158 278 162 189 240 151 120 160 194 73 74 186 145 194  
130 53 62 93 212 120 181 201 147 217 203 195 169 143 121 161 154 199 146 152  
149 109 96 191 254 329 295 164 149 173 139 283 210 144 346 262 237 209 66 120  
97 128 207 242 211 238 360 200 185 154 215 258 266 152 177 214 117 115 206 179  
234 457 382 164 132 229

EXT-H25A 95

427 296 452 290 239 360 169 378 296 116 127 166 259 198 221 254 176 314 239 291  
277 151 175 251 271 120 130 98 233 217 283 231 112 134 229 114 184 280 200 365  
326 172 253 285 429 346 364 250 380 168 324 223 159 164 230 144 157 170 135 136  
179 134 263 236 264 155 216 180 167 138 234 226 247 156 164 138 171 213 106 83  
132 102 189 226 297 275 280 173 153 234 221 264 147 212 245

EXT-H25B 95

456 316 458 295 224 360 182 402 289 119 126 170 234 193 204 243 175 321 255 282  
281 180 136 269 297 95 125 97 236 285 281 232 91 136 227 122 188 276 207 332  
359 162 250 276 386 368 363 247 380 157 301 220 178 158 212 144 154 146 129 146  
173 136 270 266 266 147 218 203 136 139 233 214 243 155 150 147 170 199 117 89  
129 103 189 223 307 261 298 160 150 235 219 240 178 229 208

EXT-H26A 91

368 348 429 391 367 312 283 282 201 340 481 463 417 434 423 245 153 186 223 253  
248 276 149 123 204 109 286 108 144 355 267 258 157 111 137 155 110 124 206 190

165 144 120 108 129 68 132 99 130 195 115 137 96 180 132 155 92 101 105 117  
181 110 167 171 157 125 101 160 105 167 115 104 169 176 246 165 174 126 143 124  
164 126 182 115 110 139 155 147 185 156 271

EXT-H26B 91

372 321 437 394 357 311 286 305 201 288 482 463 412 428 442 238 157 178 243 246  
257 275 133 136 193 110 290 112 153 347 251 283 148 110 119 150 110 126 216 203  
157 132 128 105 111 76 129 98 120 185 110 138 115 173 120 161 90 96 109 116  
185 123 162 175 161 108 94 163 107 164 116 111 156 189 230 154 162 138 137 127  
164 140 185 117 111 133 147 154 169 176 272

EXT-H27A 54

156 106 172 169 109 121 121 387 493 375 354 311 334 195 151 157 328 302 354 388  
201 168 285 133 372 200 219 486 326 292 205 200 249 288 289 281 464 254 253 187  
220 227 190 96 239 226 151 234 186 171 141 246 202 263

EXT-H27B 54

171 99 176 172 105 125 110 392 477 337 346 324 336 194 145 169 314 280 361 405  
180 175 289 138 364 208 219 489 324 276 208 172 251 290 289 266 463 273 247 186  
201 227 236 101 243 213 154 201 187 163 141 244 216 257

EXT-H28A 69

565 388 569 262 425 347 269 155 449 184 171 162 156 220 177 179 196 204 316 242  
228 219 97 146 136 195 239 244 140 155 173 120 100 128 178 229 166 169 160 121  
139 122 161 68 114 189 159 201 130 113 115 138 107 87 133 97 132 140 152 149  
92 58 107 101 70 109 99 105 109

EXT-H28B 69

553 372 565 278 414 343 263 159 425 199 174 153 162 220 176 171 203 203 328 242  
218 231 91 150 127 205 234 257 140 157 191 114 108 121 182 230 157 177 163 120  
140 117 170 78 104 200 144 219 131 109 110 137 106 84 127 110 126 131 153 155  
92 60 105 110 71 109 100 105 97

EXT-H29A 77

331 324 210 178 209 276 340 329 264 147 108 248 145 387 155 212 440 253 181 177  
164 129 187 149 145 195 169 198 209 175 143 124 78 120 122 147 167 122 125 121  
181 125 193 112 113 118 104 194 153 181 122 111 104 95 130 97 169 147 142 204  
235 245 171 166 124 156 222 250 218 183 104 108 146 226 275 296 229

EXT-H29B 77

315 331 216 172 211 278 325 359 260 139 104 240 146 390 156 223 445 238 189 175  
159 142 190 132 157 179 171 214 203 189 169 155 76 130 119 155 178 124 126 105  
179 126 188 120 106 112 101 202 158 181 137 126 109 87 146 112 184 145 130 199  
214 218 176 185 118 169 229 256 200 173 120 107 138 223 268 312 251

EXT-H30A 126

291 150 159 152 173 132 173 166 182 235 239 236 258 277 241 161 224 275 260 240  
259 275 149 150 218 199 177 240 187 217 257 186 168 219 233 190 227 182 155 141  
180 151 192 101 155 149 120 125 167 152 142 125 141 87 179 151 149 144 169 125  
134 122 106 107 103 86 111 115 101 152 140 94 111 120 107 84 88 123 101 125  
128 87 81 85 68 90 88 157 113 131 149 129 172 119 163 117 107 135 132 120  
139 143 135 107 87 136 103 109 139 158 92 135 138 104 146 135 141 115 77 106  
65 69 97 114 82 131

EXT-H30B 126

225 144 173 166 200 116 164 172 179 241 246 240 256 274 238 165 230 265 258 246  
222 248 159 155 194 205 161 220 183 217 252 176 181 210 225 183 228 193 153 153  
179 150 206 106 143 151 126 105 173 164 154 109 156 91 163 160 144 144 170 120  
122 135 112 93 95 104 114 116 105 134 150 94 113 105 97 85 88 146 99 116  
151 79 70 94 91 87 83 157 126 97 140 111 180 117 158 104 113 138 129 126  
142 143 134 105 94 128 110 106 150 157 95 146 128 113 148 140 134 120 80 88  
83 74 99 104 82 123

EXT-H31A 79

110 130 104 257 203 250 236 277 292 202 249 491 495 540 260 334 320 289 358 377  
374 357 284 292 333 368 274 282 201 270 269 274 168 151 125 86 86 140 204 163  
176 206 236 169 134 162 191 140 163 183 210 155 110 87 97 82 110 113 155 143  
162 174 198 218 189 182 187 112 113 126 146 121 137 119 119 172 132 106 121

EXT-H31B 66

260 315 391 363 346 311 300 318 352 257 270 208 280 271 287 183 134 122 84 95  
136 189 185 196 193 231 168 139 184 188 139 171 164 222 162 119 91 98 97 101  
101 149 140 164 164 186 226 192 164 166 106 108 136 132 138 136 101 121 133 122  
100 92 100 147 94 115

EXT-H32A 92

243 160 157 115 186 177 208 307 231 329 207 186 253 165 220 223 306 236 299 247  
344 176 307 274 201 230 308 205 424 197 254 284 176 229 204 270 243 112 213 314  
230 186 143 167 126 125 161 209 192 191 247 266 188 272 171 200 271 316 205 307  
218 257 213 238 199 309 263 138 212 154 205 100 145 159 157 222 171 267 202 160  
142 172 252 254 209 270 321 166 129 155 202 270

EXT-H32B 94

238 255 337 275 333 253 351 154 292 203 162 171 235 229 451 176 178 191 130 209  
173 223 157 92 185 495 278 193 162 166 109 140 188 193 176 166 272 153 124 175  
96 166 222 225 147 134 111 89 62 100 90 106 87 70 119 58 91 55 69 69  
58 88 70 78 58 61 62 80 89 103 101 101 127 104 115 126 121 125 109 65  
65 52 49 70 76 55 120 101 104 87 109 138 131 141

EXT-H33A 99

271 157 210 160 198 192 321 238 295 331 182 190 197 216 138 141 251 276 234 223  
84 111 155 248 172 216 215 209 283 209 201 196 141 131 153 120 195 193 181 185  
129 135 173 198 141 181 136 135 134 126 277 200 104 159 138 186 163 103 115 95  
119 181 183 165 235 277 264 195 206 285 278 331 202 311 290 177 159 304 365 317  
377 396 250 177 440 286 305 301 279 255 244 339 307 380 311 247 362 353 339

EXT-H33B 99

275 150 197 156 203 196 326 227 293 332 196 184 182 216 135 152 255 221 235 177  
73 129 148 250 172 210 221 206 256 232 214 190 136 126 165 132 184 173 200 172  
127 123 182 182 167 176 142 145 125 134 257 197 112 166 142 177 152 106 124 92  
117 179 187 158 257 277 250 189 197 314 277 327 221 303 266 187 171 316 365 309  
359 382 248 165 445 286 305 266 287 254 291 339 299 394 317 249 351 302 311

## APPENDIX: TREE-RING DATING

### The Principles of Tree-Ring Dating

Tree-ring dating, or dendrochronology as it is known, is discussed in some detail in the Laboratory's Monograph, *An East Midlands Master Tree-Ring Chronology and its uses for dating Vernacular Building* (Laxton and Litton 1988) and *Dendrochronology: Guidelines on Producing and Interpreting Dendrochronological Dates* (English Heritage 1988). Here we will give the bare outlines. Each year an oak tree grows an extra ring on the outside of its trunk and all its branches just inside its bark. The width of this annual ring depends largely on the weather during the growing season, about April to October, and possibly also on the weather during the previous year. Good growing seasons give rise to relatively wide rings, poor ones to very narrow rings and average ones to relatively average ring widths. Since the climate is so variable from year to year, almost random-like, the widths of these rings will also appear random-like in sequence, reflecting the seasons. This is illustrated in Figure A1 where, for example, the widest rings appear at irregular intervals. This is the key to dating by tree rings, or rather, by their widths. Records of the average ring widths for oaks, one for each year for the last 1000 years or more, are available for different areas. These are called master chronologies. Because of the random-like nature of these sequences of widths, there is usually only one position at which a sequence of ring widths from a sample of oak timber with at least 70 rings will match a master. This will date the timber and, in particular, the last ring.

If the bark is still on the sample, as in Figure A1, then the date of the last ring will be the date of felling of the oak from which it was cut. There is much evidence that in medieval times oaks cut down for building purposes were used almost immediately, usually within the year or so (Rackham 1976). Hence if bark is present on several main timbers in a building, none of which appear reused or are later insertions, and if they all have the same date for their last ring, then we can be quite confident that this is the date of construction or soon after. If there is no bark on the sample, then we have to make an estimate of the felling date; how this is done is explained below.

### The Practice of Tree-Ring Dating at the Nottingham Tree-Ring Dating Laboratory

I. **Inspecting the Building and Sampling the Timbers.** Together with a building historian the timbers in a building are inspected to try to ensure that those sampled are not reused or later insertions. Sampling is almost always done by coring into the timber, which has the great advantage that we can sample *in situ* timbers and those judged best to give the date of construction, or phase of construction if there is more than one in the building. The timbers to be sampled are also inspected to see how many rings they have. We normally look for timbers with at least 70 rings, and preferably more. With fewer rings than this, 50 for example, sequences of widths become difficult to match to a unique

position within a master sequence of ring widths and so are difficult to date (Litton and Zainodin 1991). The cross-section of the rafter shown in Figure A2 has about 120 rings; about 20 of which are sapwood rings – the lighter rings on the outside. Similarly the core has just over 100 rings with a few sapwood rings.

To ensure that we are getting the date of the building as a whole, or the whole of a phase of construction if there is more than one, about 8–10 samples per phase are usually taken. Sometimes we take many more, especially if the construction is complicated. One reason for taking so many samples is that, in general, some will fail to give a date. There may be many reasons why a particular sequence of ring widths from a sample of timber fails to give a date even though others from the same building do. For example, a particular tree may have grown in an odd ecological niche, so odd indeed that the widths of its rings were determined by factors other than the local climate! In such circumstances it will be impossible to date a timber from this tree using the master sequence whose widths, we can assume, were predominantly determined by the local climate at the time.

Sampling is done by coring into the timber with a hollow corer attached to an electric drill and usually from its outer rings inwards towards where the centre of the tree, the pith, is judged to be. An illustration of a core is shown in Figure A2; it is about 150mm long and 10mm diameter. Great care has to be taken to ensure that as few as possible of the outer rings are lost in coring. This can be difficult as these outer rings are often very soft (see below on sapwood). Each sample is given a code which identifies uniquely which timber it comes from, which building it is from and where the building is located. For example, CRO-A06 is the sixth core taken from the first building (A) sampled by the Laboratory in Cropwell Bishop. Where it came from in that building will be shown in the sampling records and drawings. No structural damage is done to any timbers by coring, nor does it weaken them.

During the initial inspection of the building and its timbers the dendrochronologist may come to the conclusion that, as far as can be judged, none of the timbers have sufficient rings in them for dating purposes and may advise against sampling to save further unwarranted expense.

All sampling by the Laboratory is undertaken according to current Health and Safety Standards. The Laboratory's dendrochronologists are insured.





*Figure A1: A wedge of oak from a tree felled in 1976. It shows the annual growth rings, one for each year from the innermost ring to the last ring on the outside just inside the bark. The year of each ring can be determined by counting back from the outside ring, which grew in 1976*



*Figure A2: Cross-section of a rafter, showing sapwood rings in the left-hand corner, the arrow points to the heartwood/sapwood boundary (H/S); and a core with sapwood; again the arrow is pointing to the H/S. The core is about the size of a pencil*



*Figure A3: Measuring ring widths under a microscope. The microscope is fixed while the sample is on a moving platform. The total sequence of widths is measured twice to ensure that an error has not been made. This type of apparatus is needed to process a large number of samples on a regular basis*



*Figure A4: Three cores from timbers in a building. They come from trees growing at the same time. Notice that, although the sequences of widths look similar, they are not identical. This is typical*

**2. Measuring Ring Widths.** Each core is sanded down with a belt sander using medium-grit paper and then finished by hand with flourgrade-grit paper. The rings are then clearly visible and differentiated from each other with a result very much like that shown in Figure A2. The core is then mounted on a movable table below a microscope and the ring-widths measured individually from the innermost ring to the outermost. The widths are automatically recorded in a computer file as they are measured (see Fig A3).

**3. Cross-Matching and Dating the Samples.** Because of the factors besides the local climate which may determine the annual widths of a tree's rings, no two sequences of ring widths from different oaks growing at the same time are exactly alike (Fig A4). Indeed, the sequences may not be exactly alike even when the trees are growing near to each other. Consequently, in the Laboratory we do not attempt to match two sequences of ring widths by eye, or graphically, or by any other subjective method. Instead, it is done objectively (ie statistically) on a computer by a process called cross-matching. The output from the computer tells us the extent of correlation between two sample sequences of widths or, if we are dating, between a sample sequence of widths and the master, at each relative position of one to the other (offsets). The extent of the correlation at an offset is determined by the  $t$ -value (defined in almost any introductory book on statistics). That offset with the maximum  $t$ -value among the  $t$ -values at all the offsets will be the best candidate for dating one sequence relative to the other. If one of these is a master chronology, then this will date the other. Experiments carried out in the past with sequences from oaks of known date suggest that a  $t$ -value of at least 4.5, and preferably at least 5.0, is usually adequate for the dating to be accepted with reasonable confidence (Laxton and Litton 1988; Laxton *et al*/1988; Howard *et al*/1984–1995).

This is illustrated in Figure A5 with timbers from one of the roofs of Lincoln Cathedral. Here four sequences of ring widths, LIN-C04, 05, 08, and 45, have been cross-matched with each other. The ring widths themselves have been omitted in the bar diagram, as is usual, but the offsets at which they best cross-match each other are shown; eg the sequence of ring widths of C08 matches the sequence of ring widths of C45 best when it is at a position starting 20 rings after the first ring of C45, and similarly for the others. The actual  $t$ -values between the four at these offsets of best correlations are in the matrix. Thus at the offset of +20 rings, the  $t$ -value between C45 and C08 is 5.6 and is the maximum found between these two among all the positions of one sequence relative to the other.

It is standard practice in our Laboratory first to cross-match as many as possible of the ring-width sequences of the samples in a building and then to form an average from them. This average is called a site sequence of the building being dated and is illustrated in Figure A5. The fifth bar at the bottom is a site sequence for a roof at Lincoln Cathedral and is constructed from the matching sequences of the four timbers. The site sequence width for each year is the average of the widths in each of the sample sequences which has a width for that year. Thus in Fig A5 if the widths shown are 0.8mm for C45, 0.2mm for C08, 0.7mm for C05, and 0.3mm for C04, then the corresponding width of the site

sequence is the average of these, 0.55mm. The actual sequence of widths of this site sequence is stored on the computer. The reason for creating site sequences is that it is usually easier to date an average sequence of ring widths with a master sequence than it is to date the individual component sample sequences separately.

The straightforward method of cross-matching several sample sequences with each other one at a time is called the 'maximal *t*-value' method. The actual method of cross-matching a group of sequences of ring-widths used in the Laboratory involves grouping and averaging the ring-width sequences and is called the 'Litton-Zainodin Grouping Procedure'. It is a modification of the straightforward method and was successfully developed and tested in the Laboratory and has been published (Litton and Zainodin 1991; Laxton *et al* 1988).

**4. Estimating the Felling Date.** As mentioned above, if the bark is present on a sample, then the date of its last ring is the date of the felling of its tree (or the last full year before felling, if it was felled in the first three months of the following calendar year, before any new growth had started, but this is not too important a consideration in most cases). The actual bark may not be present on a timber in a building, though the dendrochronologist who is sampling can often see from its surface that only the bark is missing. In these cases the date of the last ring is still the date of felling.

Quite often some, though not all, of the original outer rings are missing on a timber. The outer rings on an oak, called sapwood rings, are usually lighter than the inner rings, the heartwood, and so are relatively easy to identify. For example, sapwood can be seen in the corner of the rafter and at the outer end of the core in Figure A2, both indicated by arrows. More importantly for dendrochronology, the sapwood is relatively soft and so liable to insect attack and wear and tear. The builder, therefore, may remove some of the sapwood for precisely these reasons. Nevertheless, if at least some of the sapwood rings are left on a sample, we will know that not too many rings have been lost since felling so that the date of the last ring on the sample is only a few years before the date of the original last ring on the tree, and so to the date of felling.

Various estimates have been made and used for the average number of sapwood rings in mature oak trees (English Heritage 1998). A fairly conservative range is between 15 and 50 and that this holds for 95% of mature oaks. This means, of course, that in a small number of cases there could be fewer than 15 and more than 50 sapwood rings. For example, the core CRO-A06 has only 9 sapwood rings and some have obviously been lost over time – either they were removed originally by the carpenter and/or they rotted away in the building and/or they were lost in the coring. It is not known exactly how many sapwood rings are missing, but using the above range the Laboratory would estimate between a minimum of 6 (=15-9) and a maximum of 41 (=50-9). If the last ring of CRO-A06 has been dated to 1500, say, then the estimated felling-date range for the tree from which it came originally would be between 1506 and 1541. The Laboratory uses this estimate for sapwood in areas of England where it has no prior information. It

also uses it when dealing with samples with very many rings, about 120 to the last heartwood ring. But in other areas of England where the Laboratory has accumulated a number of samples with complete sapwood, that is, no sapwood lost since felling, other estimates in place of the conservative range of 15 to 50 are used. In the East Midlands (Laxton *et al*/2001) and the east to the south down to Kent (Pearson 1995) where it has sampled extensively in the past, the Laboratory uses the shorter estimate of 15 to 35 sapwood rings in 95% of mature oaks growing in these parts. Since the sample CRO-A06 comes from a house in Cropwell Bishop in the East Midlands, a better estimate of sapwood rings lost since felling is between a minimum of 6 (=15-9) and 26 (=35-9) and the felling would be estimated to have taken place between 1506 and 1526, a shorter period than before. Oak boards quite often come from the Baltic region and in these cases the 95% confidence limits for sapwood are 9 to 36 (Howard *et al*/1992, 56).

Even more precise estimates of the felling date and range can often be obtained using knowledge of a particular case and information gathered at the time of sampling. For example, at the time of sampling the dendrochronologist may have noted that the timber from which the core of Figure A2 was taken still had complete sapwood but that some of the soft sapwood rings were lost in coring. By measuring into the timber the depth of sapwood lost, say 20mm, a reasonable estimate can be made of the number of sapwood rings lost, say 12 to 15 rings in this case. By adding on 12 to 15 years to the date of the last ring on the sample a good tight estimate for the range of the felling date can be obtained, which is often better than the 15 to 35 years later we would have estimated without this observation. In the example, the felling is now estimated to have taken place between AD 1512 and 1515, which is much more precise than without this extra information.

Even if all the sapwood rings are missing on a sample, but none of the heartwood rings are, then an estimate of the felling-date range is possible by adding on the full compliment of, say, 15 to 35 years to the date of the last heartwood ring (called the heartwood/sapwood boundary or transition ring and denoted H/S). Fortunately it is often easy for a trained dendrochronologist to identify this boundary on a timber. If a timber does not have its heartwood/sapwood boundary, then only a *post quem* date for felling is possible.

**5. Estimating the Date of Construction.** There is a considerable body of evidence collected by dendrochronologists over the years that oak timbers used in buildings were not seasoned in medieval or early modern times (English Heritage 1998; Miles 1997, 50–5). Hence, provided that all the samples in a building have estimated felling-date ranges broadly in agreement with each other, so that they appear to have been felled as a group, then this should give an accurate estimate of the period when the structure was built, or soon after (Laxton *et al*/2001, fig 8; 34–5, where ‘associated groups of fellings’ are discussed in detail). However, if there is any evidence of storage before use, or if there is evidence the oak came from abroad (eg Baltic boards), then some allowance has to be made for this.

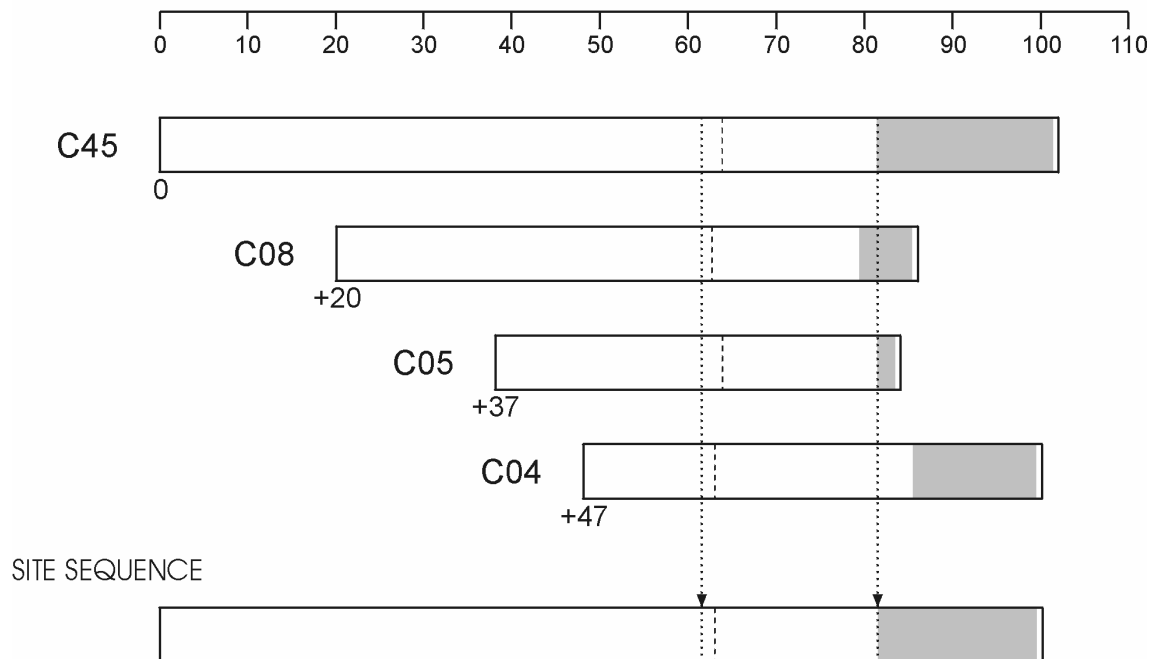
**6. Master Chronological Sequences.** Ultimately, to date a sequence of ring widths, or a site sequence, we need a master sequence of dated ring widths with which to cross-match it, a Master Chronology. To construct such a sequence we have to start with a sequence of widths whose dates are known and this means beginning with a sequence from an oak tree whose date of felling is known. In Figure A6 such a sequence is SHE-T, which came from a tree in Sherwood Forest which was blown down in a recent gale. After this other sequences which cross-match with it are added and gradually the sequence is 'pushed back in time' as far as the age of samples will allow. This process is illustrated in Figure A6. We have a master chronological sequence of widths for Nottinghamshire and East Midlands oak for each year from AD 882 to 1981. It is described in great detail in Laxton and Litton (1988), but the components it contains are shown here in the form of a bar diagram. As can be seen, it is well replicated in that for each year in this period there are several sample sequences having widths for that year. The master is the average of these. This master can now be used to date oak from this area and from the surrounding areas where the climate is very similar to that in the East Midlands. The Laboratory has also constructed a master for Kent (Laxton and Litton 1989). The method the Laboratory uses to construct a master sequence, such as the East Midlands and Kent, is completely objective and uses the Litton-Zainodin grouping procedure (Laxton *et al* 1988). Other laboratories and individuals have constructed masters for other areas and have made them available. As well as these masters, local (dated) site chronologies can be used to date other buildings from nearby. The Laboratory has hundreds of these site sequences from many parts of England and Wales covering many short periods.

**7. Ring-Width Indices.** Tree-ring dating can be done by cross-matching the ring widths themselves, as described above. However, it is advantageous to modify the widths first. Because different trees grow at different rates and because a young oak grows in a different way from an older oak, irrespective of the climate, the widths are first standardized before any matching between them is attempted. These standard widths are known as ring-width indices and were first used in dendrochronology by Baillie and Pilcher (1973). The exact form they take is explained in this paper and in the appendix of Laxton and Litton (1988) and is illustrated in the graphs in Figure A7. Here ring-widths are plotted vertically, one for each year of growth. In the upper sequence of (a), the generally large early growth after 1810 is very apparent as is the smaller later growth from about 1900 onwards when the tree is maturing. A similar phenomenon can be observed in the lower sequence of (a) starting in 1835. In both the widths are also changing rapidly from year to year. The peaks are the wide rings and the troughs are the narrow rings corresponding to good and poor growing seasons, respectively. The two corresponding sequence of Baillie-Pilcher indices are plotted in (b) where the differences in the immature and mature growths have been removed and only the rapidly changing peaks and troughs remain, that are associated with the common climatic signal. This makes cross-matching easier.

*t*-value/offset Matrix

	C45	C08	C05	C04
C45		+20	+37	+47
C08	5.6		+17	+27
C05	5.2	10.4		+10
C04	5.9	3.7	5.1	

Bar Diagram



**Figure A5: Cross-matching of four sequences from a Lincoln Cathedral roof and the formation of a site sequence from them**

The bar diagram represents these sequences without the rings themselves. The length of the bar is proportional to the number of rings in the sequence. Here the four sequences are set at relative positions (offsets) to each other at which they have maximum correlation as measured by the *t*-values. The *t*-value/offset matrix contains the maximum *t*-values below the diagonal and the offsets above it. Thus, the maximum *t*-value between C08 and C45 occurs at the offset of +20 rings and the *t*-value is then 5.6. The site sequence is composed of the average of the corresponding widths, as illustrated with one width



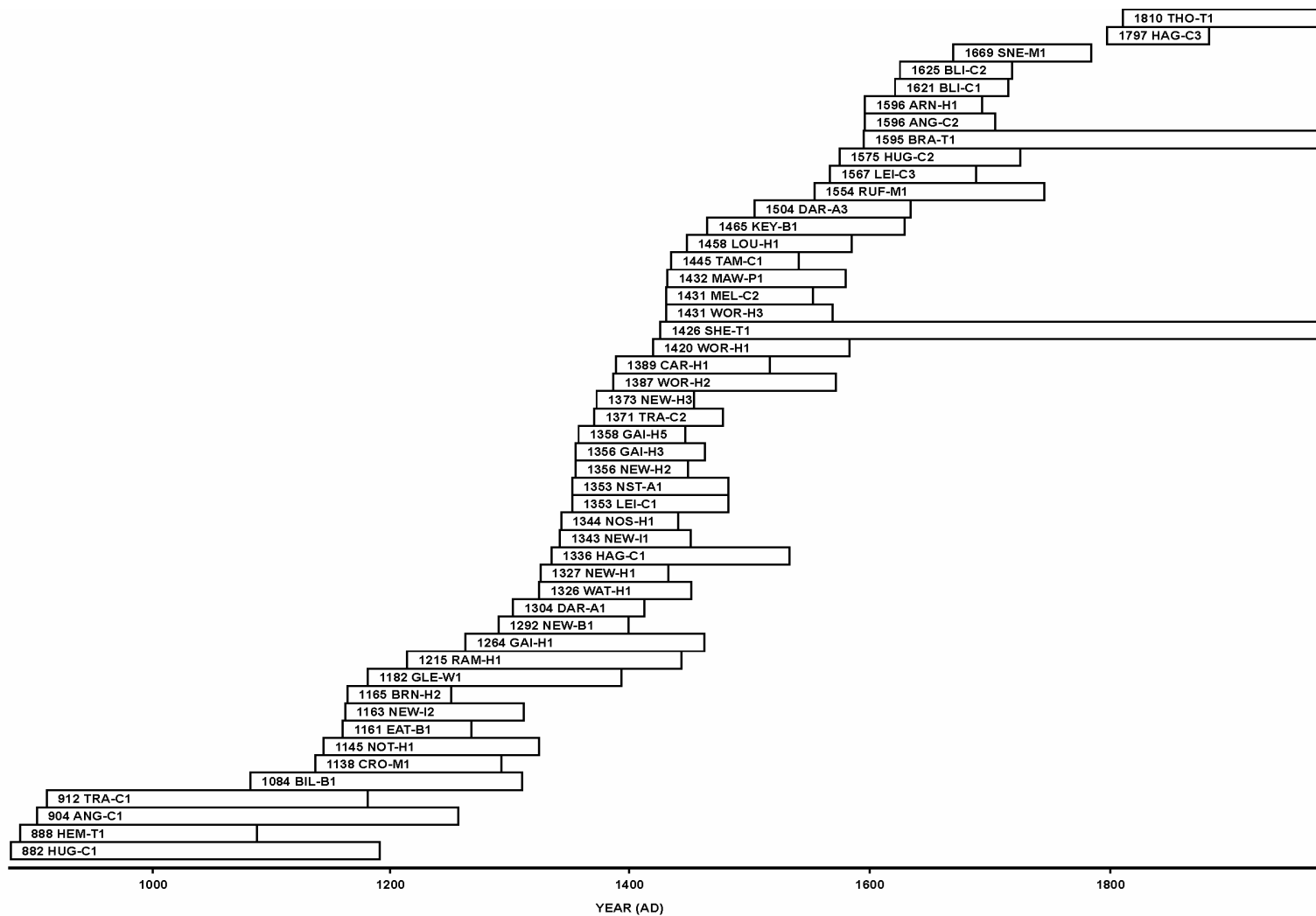
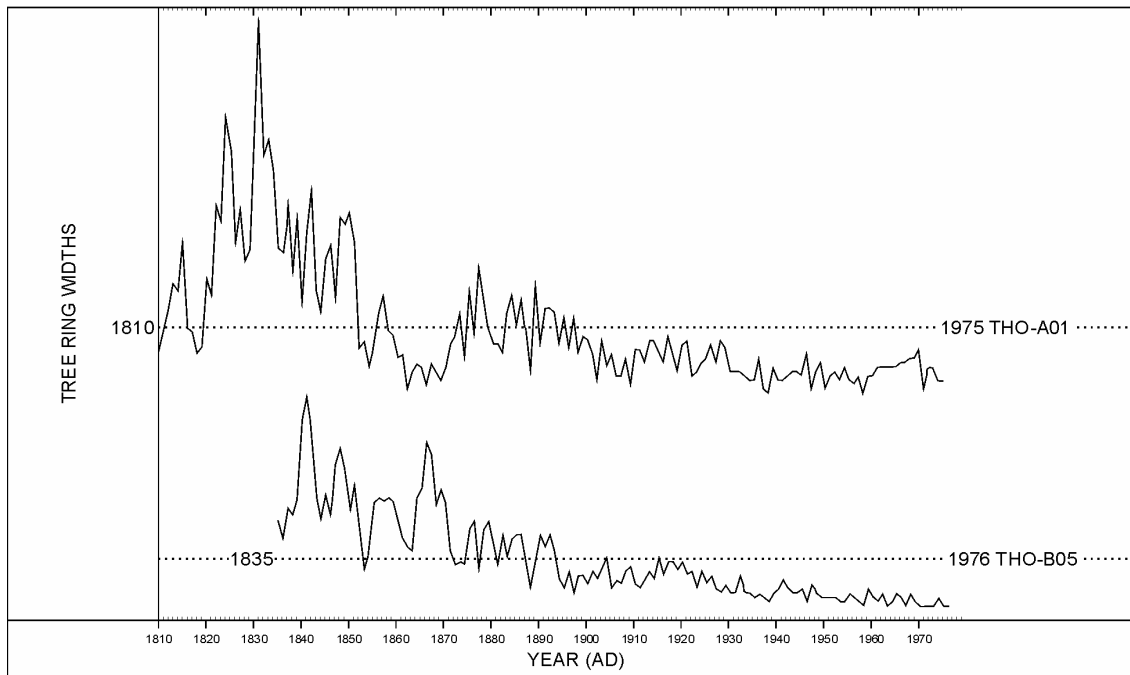
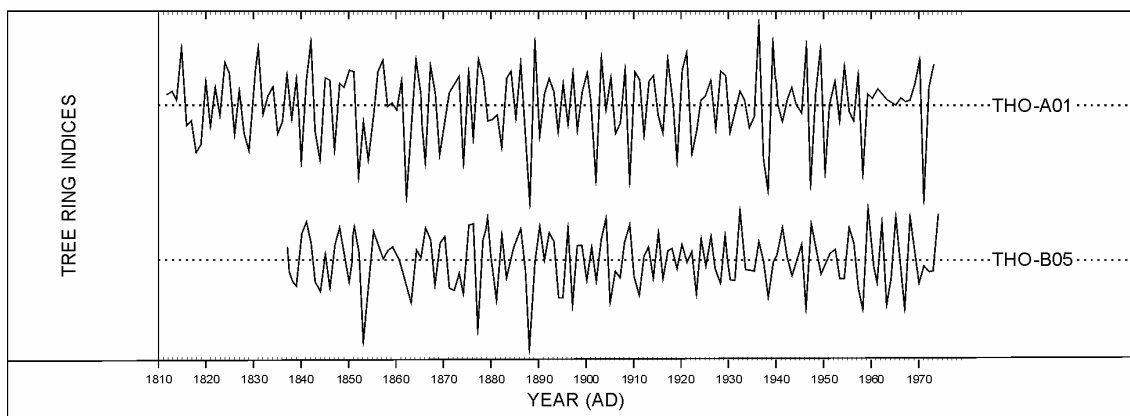


Figure A6: Bar diagram showing the relative positions and dates of the first rings of the component site sequences in the East Midlands Master Dendrochronological Sequence, EM08/87

(a)



(b)



**Figure A7 (a):** *The raw ring-widths of two samples, THO-A01 and THO-B05, whose felling dates are known*

Here the ring widths are plotted vertically, one for each year, so that peaks represent wide rings and troughs narrow ones. Notice the growth-trends in each; on average the earlier rings of the young tree are wider than the later ones of the older tree in both sequences

**Figure A7 (b):** *The Baillie-Pilcher indices of the above widths*

The growth trends have been removed completely

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