

Centre for Archaeology Report 44/2005

**Tree-Ring Analysis of Timbers from the Nave Roof  
and Ceiling of the Cathedral Church of St Peter  
and St Wilfred, Ripon, North Yorkshire**

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ISSN 1473-9224

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## **Tree-Ring Analysis of Timbers from the Nave Roof and Ceiling of the Cathedral Church of St Peter and St Wilfred, Ripon, North Yorkshire**

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### **Summary**

A total of 30 core samples was obtained from the principal oak timbers of the roof and the ceiling ribs of the nave of Ripon Cathedral. The analysis of these produced two major site chronologies, one of six samples, 226 rings long, and another of nine samples, 117 rings long. Two other site chronologies with only two samples each were also created.

Despite the number of samples obtained, the length of the site chronologies created, and despite being compared with a very extensive range of reference chronologies, none of the site chronologies, nor any individual samples, could be dated.

It would certainly appear that timbers within groups were felled at the same time as each other, possibly for use as specific elements. However, it is not possible to ascertain whether the groups of timbers, or the ungrouped individual timbers, are either contemporary, or whether they represent different woodland sources.

### **Keywords**

Dendrochronology  
Standing Building

### **Author's address**

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## **Introduction**

The earliest church on the site of Ripon Cathedral (NE 314 711; Fig 1) was originally part of a Scottish monastery. This was reorganised along Benedictine lines by St Wilfred in AD 660. Between then and AD 1050 it was refounded as a College of secular canons under the patronage of the Archbishop of York. It remained as a parish church even after the dissolution of the college in AD 1547. In AD 1604 the college was re-founded under James I, dissolved during the commonwealth, but founded yet again in AD 1660. It was elevated to Cathedral status in AD 1836.

Major rebuilding work was begun under Archbishop Roger, AD 1154 – 81, and completed by Walter Gray, AD 1215 – 55. A library was added in the early-fourteenth century, with further alterations in the fifteenth century. The nave is believed to have undergone substantial alterations in the early-sixteenth century, with aisles being added at this time. In AD 1615 the spire on the crossing tower collapsed and in AD 1664 the spires on the two western towers were taken down. Nineteenth-century repairs were undertaken in AD 1829 – 31 by Edward Blore, and in AD 1843 – 44 by William Railton, with more drastic alterations being made by Gilbert Scott in AD 1862.

## **Sampling**

Sampling and analysis by tree-ring dating of the timbers at Ripon Cathedral were commissioned by English Heritage. Initially this was to include timbers in both the nave and the chancel roofs. However, only the timbers of the nave were accessible. This programme of analysis was requested to inform grant-aided repairs by providing a precise date for the construction of the roof and to date any repairs or alterations. The dates, of various elements of the roof, are unclear. It is uncertain, for example, how much, if any, of the roof comprises sixteenth-century, or indeed earlier, material in its original position or possibly reused. This is particularly so with the timbers of the ceiling vault, some of which retain carpenters' marks in the form of Roman numerals. It is also uncertain as to how much of the roof might represent nineteenth-century repair material. Indeed, at the time the roof was first taken off it appeared as if all the timbers were softwood, with no oak remaining at all. A general plan of the Cathedral, taken from 'The Builder', February 1893, and provided by English Heritage, is given in Figure 2.

The nave roof consists of 15 'truncated' trusses, consisting alternately of single larger principal rafters, (trusses 1, 3, 5 etc, numbering from west to east) or of two very slightly smaller principal rafters in close-set pairs (trusses 2, 4, 6, etc). All such principal rafters are of oak. Apart from slight differences in dimension, there appear to be other very slight variations between the timbers of the two types of truss. The larger single rafters appear to be more squarely cut, and have more regular saw-marks on their faces. The smaller 'double' rafters are less well worked, being less well trimmed, and appear slightly more uneven in their sawing. It thus appears as if there are two sets of timbers within the principal trusses.

The apex of each truss appears to have been cut off (if indeed the original ever went to the ridge), and replaced in softwood. In addition the apex sections, the collars, purlins, and all

other roof timbers are of softwood. These softwood timbers have the appearance, judging by the carpentry, of being nineteenth-century pieces.

From these principal roof timbers a total of 15 core samples was obtained. Each sample was given the code RIP-C (for Ripon Cathedral) and numbered 01 – 15. An attempt was made to obtain samples from what were thought to be the two possible sets of timbers here, the single principal rafters, and the 'double' principals.

Set to the underside of the principal roof timbers are the beams of the ceiling vault. These consist of ridge and vault ribs, from which spring diagonal and intermediate ribs. All these timbers are of oak. From these beams a further 15 core samples were obtained, RIP-C16 – 30. Because of safety concerns, there being no support or platform beneath the ceiling, it was only possible to sample the ceiling beams at each end of the nave roof, where boarding could be safely laid from above. There is a substantial quantity of other oak timber which could be sampled with the aid of a harness, though preventing public access to the area below might also be necessary.

The positions of these 30 samples are shown on drawings provided by EH, reproduced here as Figure 3. Details of the samples are given in Table 1. In this report the trusses and bays have been numbered from west to east, with the 'double' principals being further designated 'A' or 'B', the west and east of the pair respectively. Individual timbers are described on a north-south basis as appropriate.

The Laboratory would like to take this opportunity to thank Jane McComish and Mark Johnson of York Archaeological Trust for their help in arranging site access, as well as the staff of Joseph Hardgrave, Roofers, Ltd, York, who were most helpful during sampling. We would also like to thank Cathy Groves of the University of Sheffield Dendrochronology Laboratory and our other, international, colleagues who all attempted to find a cross-match and date for the samples.

## Analysis

Each of the 30 samples was prepared by sanding and polishing and their annual growth-ring widths measured. The data of these measurements are given at the end of the report. These data were then compared with each other by the Litton/Zainodin grouping procedure (see appendix) and at a minimum value of  $t=4.5$  four satisfactory site chronologies could be formed:

Site chronology	Number of samples	Sequence length	Bar diagram Figure
RIPCSQ01	6	226	4
RIPCSQ02	9	117	5
RIPCSQ03	2	130	6
RIPCSQ04	2	127	7

Each site chronology thus created was compared with an extensive range of British and European site chronologies, including those held by the Nottingham Laboratory and others, the Sheffield Dendrochronology Laboratory for example. Despite this extensive comparison, and despite the length of the site chronologies, there was no satisfactory cross-matching against any available reference chronologies.

### **Interpretation**

Of the 30 samples obtained, 19 have been formed into one of four site chronologies. Although none of these site chronologies, or any of the remaining individual samples, can be dated, it is possible to say something about the relative felling dates of the timbers concerned.

Firstly it is certain that some timbers represent a single phase of felling. For example, five samples, RIP-C02, C03, C08, C10, and C11, in site chronology RIPCSQ01, retain complete sapwood. This means that they each have the last ring produced by the tree represented before it was felled. In each case the last sapwood ring is at the same relative position indicating that the timbers were all cut at the same time. It is highly likely that the timber represented by sample RIP-C09 was felled at the same time as well. It also appears possible that these timbers are used for specific beams. All the samples in site chronology RIPCSQ01 are from the single principal rafter trusses.

A single phase of felling is also represented by a number of samples in site chronology RIPCSQ02. Samples RIP-C05, C13, C14, C15, C20, C29, and C30 retain complete sapwood, the last sapwood ring being at the same relative position in each case. It is probable that the other timbers represented in this site chronology were felled at the same time. There again may be some specific use for the timber represented, many of the samples in this second site chronology, RIP-C05, C07, C13, C14, and C15, being from the 'double' rafter trusses. This site chronology does, however, contain some samples from the ribs of the ceiling.

A single phase of felling is represented by samples RIP-C21 and C27 in site chronology RIPCSQ03, the last complete sapwood rings on these two being in the same relative positions. It is possible, though not certain, that samples RIP-C23 and C24 in site sequence RIPCSQ04, represent a single phase of felling also.

### **Conclusion**

Analysis by dendrochronology has in this instance not been able to provide a date for a single sample. It can show, however, that some specific beams, those of the single principal rafters, are representative of a single phase of felling, as are those of the 'double' principal rafters, and some of the ribs of the ceiling. Other samples also represent single phases of felling.

What it has not been possible to show is the relationship between these felling phases. It is possible that all the groups of timbers were felled at different times, there being no cross-matching between them because they have no temporal overlap with each other. It

is also possible that they were all felled at the same time, but there is no cross-matching between them because they are from different sources. Whatever the relative felling of the groups, the original woodland source, or sources, is not represented in any available reference chronology. It is possible that some combination of these two factors is represented by the timbers.

It is unusual to have so many highly suitable samples left undated. Were the timbers felled at different times, it would perhaps be unlikely that every group formed would be unrepresented in the gamut of reference material. Some, at least, of the site chronologies, or some of the remaining individual samples, might be dated. But this is not the case in this instance.

The fact that none of the samples are dated is perhaps most easily explained by the timber being felled at the same time from different sources, which would help account for the site chronologies not cross-matching with each other, and also by the timber being nineteenth century. There are very few reference chronologies available for Yorkshire or the northeast for this time period. Such difficulties might be compounded if, perhaps, the woodland sources were all foreign. This is possibly due to the development in the eighteenth, and especially the nineteenth century, of timber-yards, or timber merchants, along the lines that we know of today. Ripon Cathedral may not have obtained the timbers sampled direct from a single, known, woodland source, as is more often the case in the medieval period, but from a supplier who has obtained material from an extensive range of sources, including, perhaps in this case, from abroad.

Two other features of the samples are noteworthy. Firstly it will be seen from Table 1 that some of them have in excess of 200 rings, and several are in excess of 150 rings long. While this is not unusual it is not common in material of possible nineteenth century or very late-medieval date. The second feature the samples display is the low number of sapwood rings found on the samples. The 95% confidence limit for the amount of sapwood rings on mature oaks in England is usually in the range 15 – 40 rings. In a group of 30 samples it might be expected that one or maybe two samples might have more or less sapwood rings than this. It will again be seen from Table 1 that only a few samples analysed here sapwood rings within the 95% limit, all the others have less, the lowest number of sapwood rings on any sample where it is complete is 9. Such low numbers of sapwood rings are more common in timbers from the east of England and continental Europe.

Table 1: Details of samples from the nave roof and ceiling, Ripon Cathedral

Sample number	Sample location	Total rings	*Sapwood rings	First measured ring date	Last heartwood ring date	Last measured ring date
Principal roof timbers						
RIP-C01	South principal rafter, truss 1	159	17C	-----	-----	-----
RIP-C02	South principal rafter, truss 3	226	16C	-----	-----	-----
RIP-C03	South principal rafter, truss 5	218	14C	-----	-----	-----
RIP-C04	South principal rafter, truss 7	86	14C	-----	-----	-----
RIP-C05	South double rafter, truss 2A	61	13C	-----	-----	-----
RIP-C06	South double rafter, truss 4B	112	no h/s	-----	-----	-----
RIP-C07	South double rafter, truss 6B	81	h/s	-----	-----	-----
RIP-C08	North principal rafter, truss 3	206	17C	-----	-----	-----
RIP-C09	North principal rafter, truss 5	108	no h/s	-----	-----	-----
RIP-C10	North principal rafter, truss 9	212	14C	-----	-----	-----
RIP-C11	North principal rafter, truss 11	212	17C	-----	-----	-----
RIP-C12	North double rafter, truss 2B	75	9C	-----	-----	-----
RIP-C13	North double rafter, truss 6A	91	12C	-----	-----	-----
RIP-C14	North double rafter, truss 6B	104	12C	-----	-----	-----
RIP-C15	North double rafter, truss 10B	83	18C	-----	-----	-----

Table 1: continued

Sample number	Sample location	Total rings	*Sapwood rings	First measured ring date	Last heartwood ring date	Last measured ring date
Ceiling, bay 1, west end						
RIP-C16	Ceiling rib	79	14C	-----	-----	-----
RIP-C17	Ceiling rib	120	no h/s	-----	-----	-----
RIP-C18	Ceiling rib	66	12C	-----	-----	-----
RIP-C19	Ceiling rib	89	2	-----	-----	-----
RIP-C20	Ceiling rib	82	12C	-----	-----	-----
RIP-C21	Ceiling rib	82	10C	-----	-----	-----
RIP-C22	Ceiling rib	79	no h/s	-----	-----	-----
RIP-C23	Ceiling rib	125	16	-----	-----	-----
RIP-C24	Ceiling rib	120	18C	-----	-----	-----
RIP-C25	Ceiling rib	92	5	-----	-----	-----
Ceiling, bays 11 & 12						
RIP-C26	Ceiling rib	56	13C	-----	-----	-----
RIP-C27	Ceiling rib	130	13C	-----	-----	-----
RIP-C28	Ceiling rib	69	no h/s	-----	-----	-----
RIP-C29	Ceiling rib	117	11C	-----	-----	-----
RIP-C30	Ceiling rib	110	10C	-----	-----	-----

h/s = heartwood/sapwood boundary is last ring on sample  
 C = complete sapwood retained on sample



**Figure 1: Map to show general location of Ripon Cathedral**

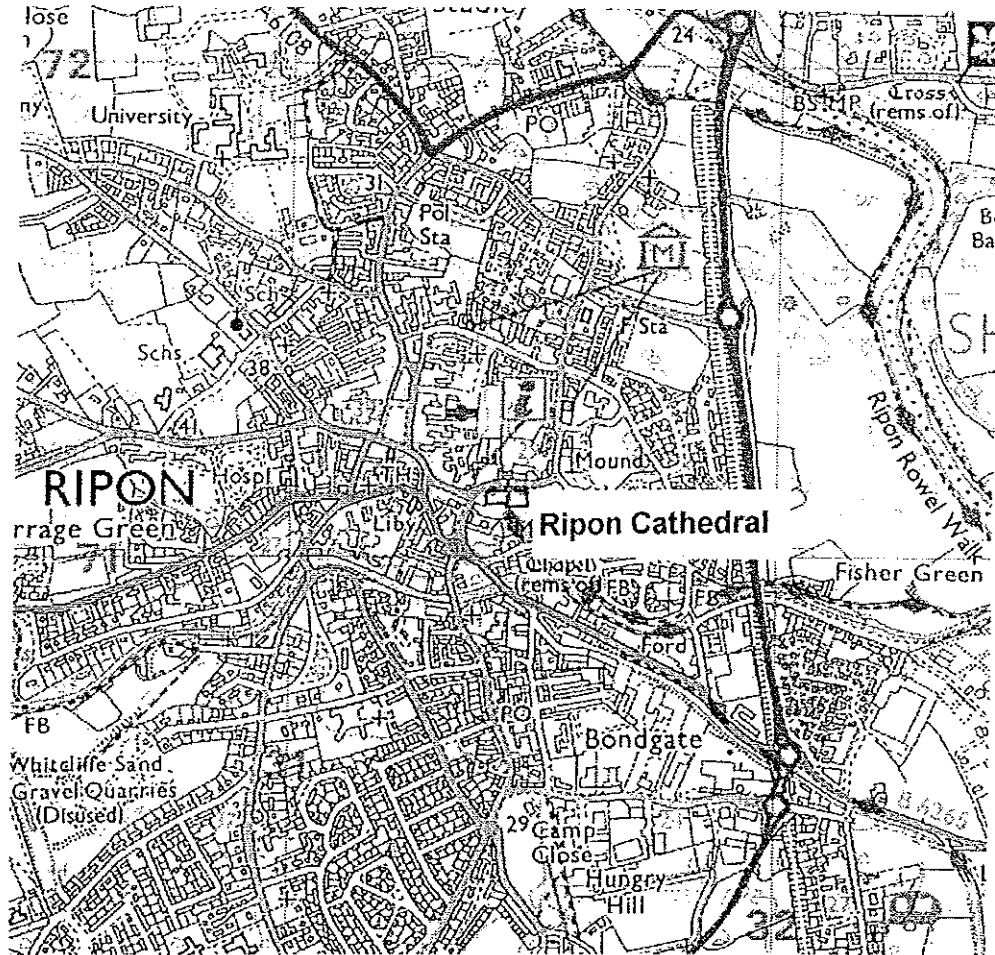


Figure 2: General plan of Ripon Cathedral © NMR 93/7827

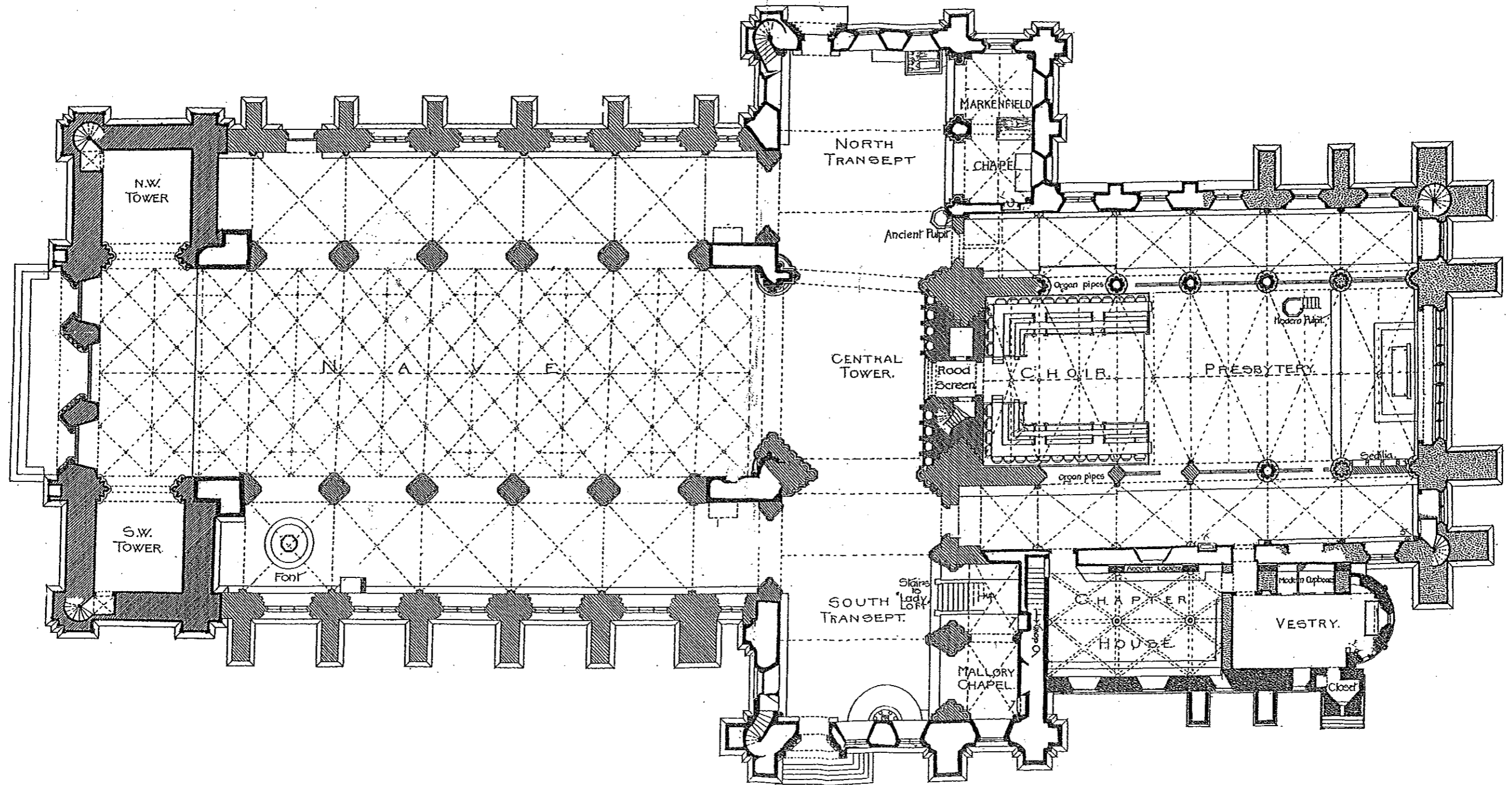


Figure 3: Plan to show position of sampled timbers from the nave roof of Ripon Cathedral © NMR 93/7827

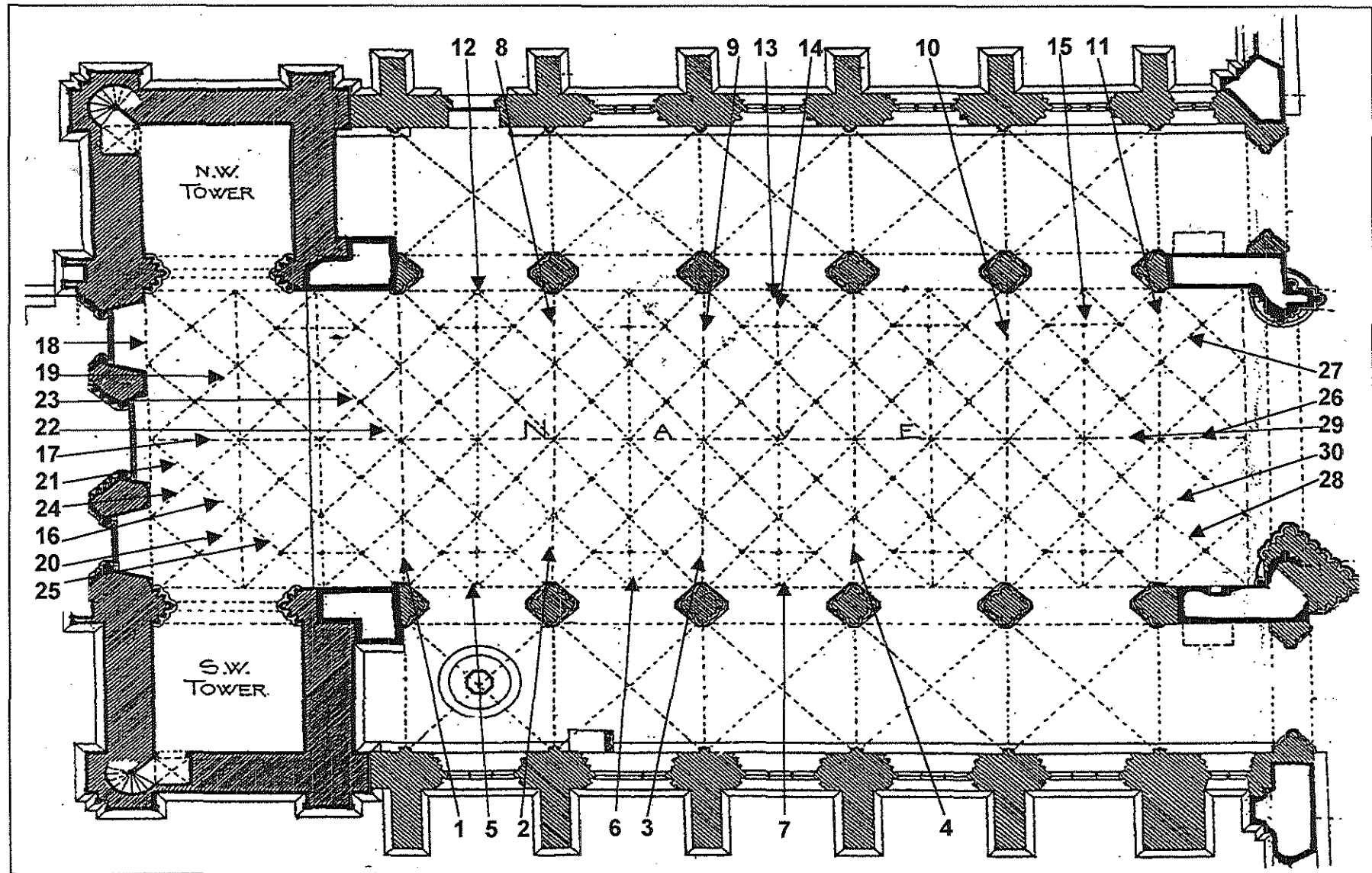
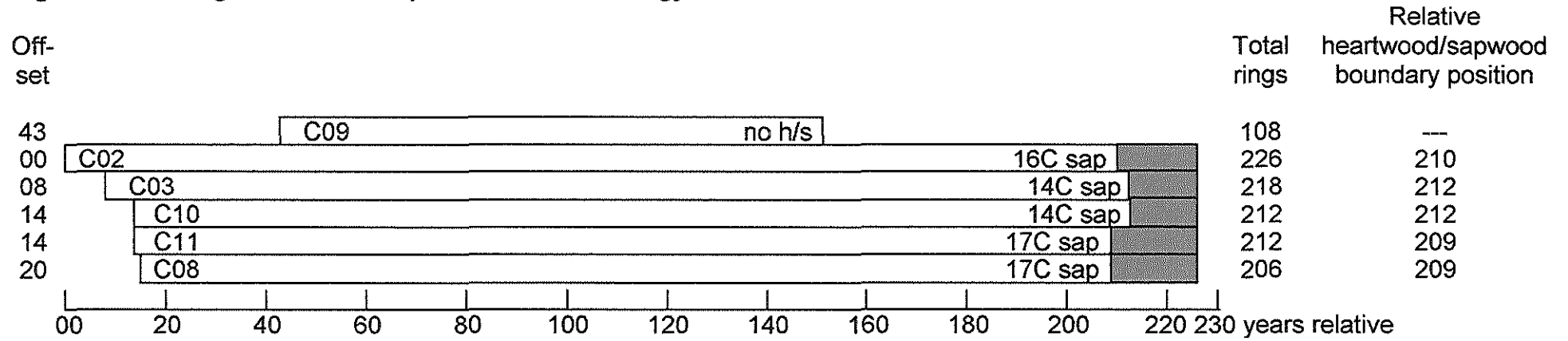


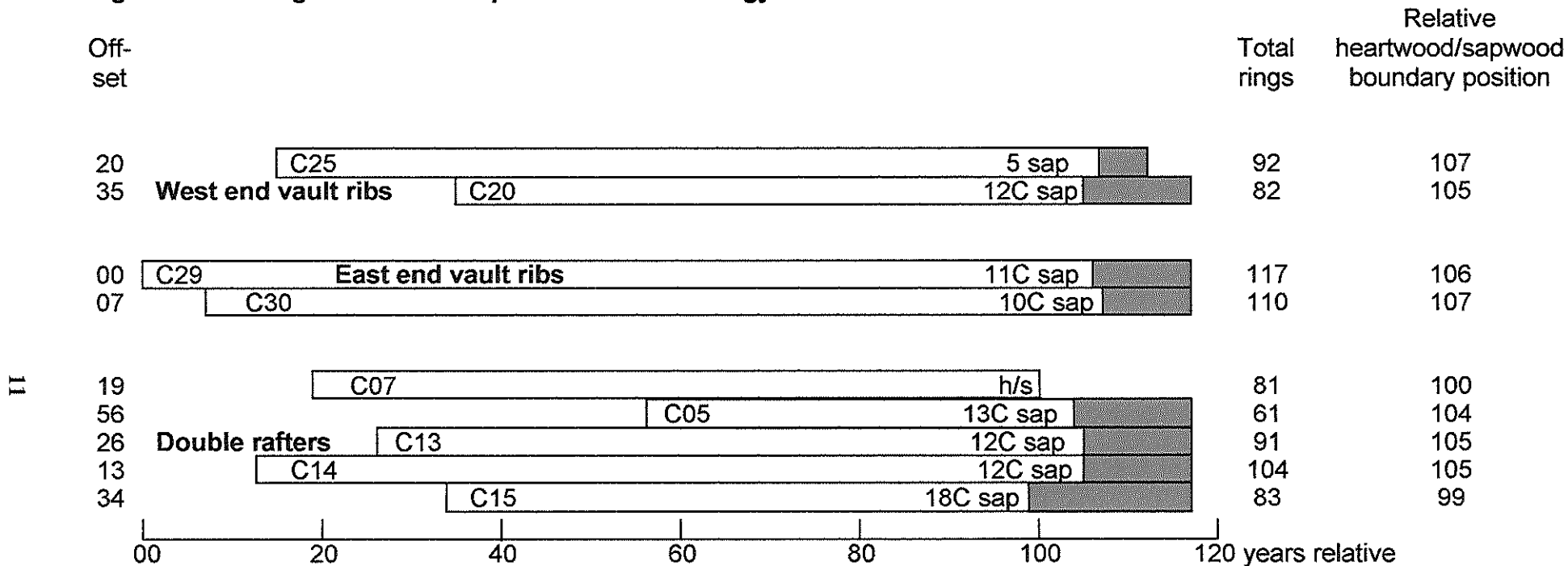
Figure 4: Bar diagram of the samples in site chronology RIPCSQ01



10

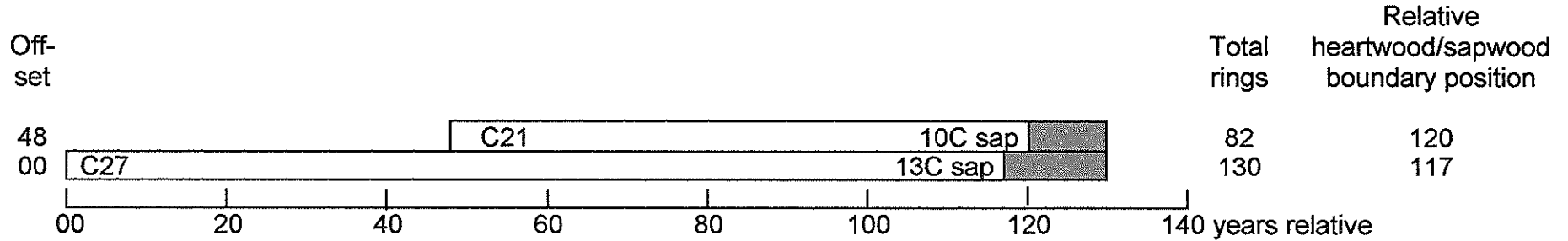
white bars = heartwood rings, shaded area = sapwood rings  
 h/s = heartwood/sapwood boundary is last ring on sample  
 C = complete sapwood retained on sample

Figure 5: Bar diagram of the samples in site chronology RIPCSQ02



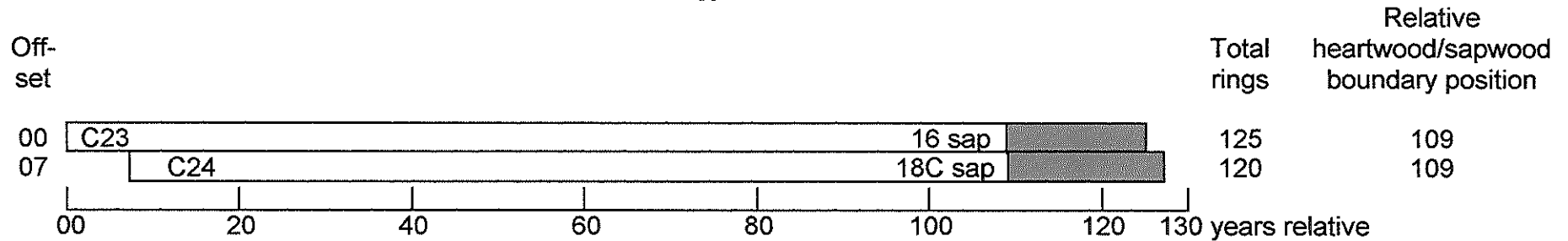
white bars = heartwood rings, shaded area = sapwood rings  
 h/s = heartwood/sapwood boundary is last ring on sample  
 C = complete sapwood retained on sample

Figure 6: Bar diagram of the samples in site chronology RIPCSQ03



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Figure 7: Bar diagram of the samples in site chronology RIPCSQ04



white bars = heartwood rings, shaded area = sapwood rings  
 h/s = heartwood/sapwood boundary is last ring on sample  
 C = complete sapwood retained on sample

Data of measured samples – measurements in 0.01 mm units

RIP-C01A 159

131 141 187 161 233 198 144 149 177 188 155 132 139 145 154 142 156 128 164 147  
136 149 138 172 197 156 149 102 111 102 94 103 119 134 159 181 76 79 64 57  
39 47 41 49 56 64 64 59 58 75 77 66 65 77 64 68 101 69 62 81  
94 80 91 101 94 76 77 82 59 68 51 58 65 70 96 66 90 76 69 83  
79 68 77 112 58 89 69 87 80 62 130 110 72 115 80 77 125 130 120 120  
93 134 175 183 188 188 186 124 118 130 165 148 151 137 125 101 85 94 111 150  
113 79 84 84 72 68 102 78 94 76 109 111 101 151 136 159 122 138 136 185  
135 138 171 208 225 144 119 75 120 116 153 112 112 85 63 109 89 107 100

RIP-C01B 159

150 132 186 160 241 189 140 149 194 180 172 126 143 142 158 141 150 120 178 144  
141 153 143 172 186 168 138 111 100 99 98 96 112 139 158 174 70 87 70 54  
47 37 46 53 55 69 60 46 65 75 79 64 81 60 80 58 109 58 58 92  
78 91 85 101 91 77 77 81 62 72 44 58 66 72 92 71 88 73 78 75  
81 65 75 111 55 89 72 85 85 56 129 111 78 118 77 79 118 138 116 122  
91 134 172 182 193 185 188 127 110 136 170 136 171 138 120 90 85 99 111 142  
121 66 90 75 76 65 116 69 96 75 119 119 103 132 150 184 108 144 138 168  
131 139 171 210 215 141 120 75 119 119 151 118 103 89 73 93 99 127 110

RIP-C02A 226

290 437 474 428 226 521 422 357 516 474 249 274 302 253 196 133 153 178 209 286  
196 172 124 126 103 73 75 71 55 47 70 64 122 91 114 106 156 184 116 100  
113 107 74 131 136 127 123 84 88 112 118 161 97 82 72 74 60 49 55 61  
56 48 66 67 84 92 99 65 64 73 92 121 123 76 58 61 61 40 54 95  
118 105 94 80 73 90 92 64 48 66 96 102 84 62 89 57 68 49 52 52  
57 55 109 110 89 87 122 123 129 106 135 58 116 108 74 70 82 80 73 73  
76 56 47 46 67 80 66 59 85 76 73 103 91 102 94 83 54 94 81 91  
60 60 85 58 78 97 57 81 80 81 55 89 60 91 107 100 88 70 100 90  
56 65 84 49 72 50 56 53 50 49 59 65 80 76 69 57 54 47 51 69  
62 60 89 64 66 69 89 81 83 74 62 70 83 71 71 58 63 70 52 49  
80 56 66 64 61 78 62 62 66 97 87 78 67 71 47 68 68 72 71 83  
74 73 92 79 80 81

RIP-C02B 226

357 390 450 388 288 487 388 382 481 470 251 275 285 245 188 126 150 174 196 305  
185 185 132 119 90 80 77 56 64 63 62 68 119 101 112 95 137 186 119 93  
122 98 81 129 127 116 123 89 102 107 116 143 93 80 69 89 50 55 52 57  
71 55 60 73 87 90 101 72 70 57 100 115 119 89 53 56 64 45 45 96  
86 118 98 76 75 101 95 63 52 76 93 98 87 79 69 78 70 39 41 54  
51 61 112 93 100 96 124 126 135 88 102 89 126 110 68 72 85 84 74 57  
88 52 40 61 60 71 80 47 89 82 69 101 89 107 96 73 63 92 90 83  
60 49 86 78 79 92 67 70 88 71 65 86 63 99 109 95 90 66 100 86  
67 60 68 55 76 53 55 45 44 56 66 56 81 79 71 64 41 53 61 58  
57 71 89 68 58 81 70 82 83 66 64 72 78 81 62 58 68 70 50 50  
69 74 48 72 68 68 65 75 67 94 89 84 59 82 43 68 72 59 88 65  
90 79 85 77 79 80

RIP-C03A 218

218 337 218 262 211 159 175 130 177 289 254 308 221 146 134 91 102 97 75 69  
88 91 101 119 108 76 61 57 78 75 71 47 75 58 43 77 95 86 92 70  
74 68 98 76 85 53 52 80 50 51 64 47 48 43 47 40 49 59 70 64  
64 47 57 60 65 59 63 55 56 60 55 48 87 68 92 72 64 62 87 84  
53 63 77 172 147 99 126 159 129 84 91 79 80 66 57 88 117 135 170 142  
157 104 74 96 128 123 96 91 78 132 96 77 133 113 102 111 140 144 99 97  
123 92 97 136 149 127 124 110 94 117 112 84 77 81 125 117 138 169 182 118  
146 120 117 121 103 163 190 138 97 74 90 65 101 114 99 93 103 103 79 65  
63 86 107 102 117 125 131 116 65 77 130 97 112 126 147 95 132 177 158 146  
111 123 150 165 151 115 96 83 122 109 80 124 159 134 127 117 118 165 143 155  
126 172 146 141 122 106 100 125 127 111 131 152 137 128 103 174 138 140

RIP-C03B 218

222 327 228 260 224 154 176 133 179 285 245 306 228 156 121 94 107 86 82 79  
94 97 102 115 113 73 58 63 75 74 64 50 75 62 45 80 94 77 88 83  
77 67 94 80 85 55 57 69 49 66 57 41 53 43 48 42 51 58 66 68  
56 48 60 62 60 56 64 61 60 54 51 52 85 72 90 71 64 57 89 86  
41 81 68 163 145 104 127 151 113 82 95 84 68 71 54 98 106 148 166 134  
159 106 70 95 128 126 88 91 79 130 100 71 140 105 97 123 140 137 102 102  
119 99 91 142 148 132 127 103 85 125 111 79 90 78 122 115 148 167 185 113  
146 129 106 114 100 162 185 139 97 72 101 65 106 108 99 92 110 107 78 65  
64 85 104 105 116 128 133 110 72 74 125 93 105 138 148 95 131 179 155 161  
109 115 148 171 140 114 102 84 126 101 74 131 153 143 123 120 107 170 155 160  
140 166 142 144 122 116 100 137 115 89 151 146 139 113 115 172 136 138

RIP-C04A 86

176 119 191 106 205 323 192 101 111 139 134 109 106 74 92 133 89 83 106 81  
107 76 89 147 120 138 122 103 114 207 156 108 119 87 143 265 250 228 265 220  
93 119 160 97 174 192 142 156 137 105 157 251 260 314 273 282 285 191 200 257  
240 327 263 175 283 270 245 175 129 111 142 186 160 183 164 200 180 239 96 153  
122 141 133 147 151 155

RIP-C04B 86

131 119 175 113 204 319 184 110 121 126 131 122 117 69 114 115 105 81 100 86  
119 90 72 156 120 125 126 98 116 203 154 114 118 99 153 247 262 226 244 204  
84 127 166 90 155 194 142 159 139 115 156 260 256 311 265 287 277 186 200 258  
231 323 262 167 282 257 238 165 145 122 139 178 170 179 178 219 180 230 98 156  
139 150 127 141 142 172

RIP-C05A 61

273 185 166 130 205 274 344 205 273 247 192 136 152 157 184 148 182 195 204 168  
266 228 219 142 144 149 143 151 143 194 206 231 201 238 196 155 172 187 210 132  
111 167 168 184 131 135 118 180 177 225 181 178 195 232 186 183 169 234 204 200  
205

RIP-C05B 61

223 175 176 137 217 276 330 214 275 250 175 126 149 151 193 153 192 184 213 177  
252 226 217 164 124 144 158 145 146 195 199 231 196 244 202 147 178 184 199 139  
100 173 170 168 145 118 123 170 197 208 189 170 197 237 185 176 177 214 192 208  
202

RIP-C06A 112

305 271 238 184 146 270 195 174 65 109 73 123 132 156 106 66 86 95 96 115  
136 103 73 117 137 111 96 121 104 125 122 161 151 165 136 113 128 132 158 123  
116 161 156 116 130 174 270 189 197 241 156 117 188 297 426 185 168 223 165 125  
103 98 147 114 117 111 115 117 145 137 151 142 146 153 101 82 96 92 129 154  
217 188 269 182 260 189 176 100 85 126 154 109 116 189 137 187 192 182 199 136  
160 200 168 123 98 149 143 145 135 114 135 160



RIP-C06B 112

265 259 240 179 131 281 195 174 60 113 79 122 130 161 104 73 70 101 74 112  
137 101 85 99 138 118 92 137 105 121 131 156 148 152 144 113 135 129 164 120  
119 161 140 119 131 174 278 192 199 218 168 127 202 285 457 205 160 227 164 125  
105 96 145 117 121 107 111 119 143 133 146 162 148 153 99 73 96 97 115 142  
221 186 273 182 266 185 168 104 96 123 151 114 119 188 149 173 193 185 203 134  
162 204 161 127 102 141 146 145 140 110 142 148

RIP-C07A 81

262 390 351 417 233 172 405 211 157 129 171 178 301 224 183 183 247 231 317 314  
342 248 235 200 239 249 130 168 235 166 320 248 221 216 186 155 159 102 84 119  
85 120 170 139 91 155 145 135 110 109 138 164 159 157 138 136 159 193 208 156  
130 117 129 160 124 168 205 162 194 180 155 158 113 127 133 164 108 87 103 147  
180

RIP-C07B 81

327 391 322 395 204 190 410 211 154 136 179 190 319 261 217 181 237 252 331 310  
363 246 232 204 239 249 143 165 221 169 300 249 223 203 198 155 147 101 97 106  
85 129 178 135 108 137 147 123 105 120 140 157 164 160 128 145 158 201 202 154  
135 115 130 160 135 163 195 159 199 175 172 154 110 128 141 149 123 82 99 154  
169

RIP-C08A 206

328 237 234 111 110 125 107 89 143 117 179 139 119 87 69 46 55 37 52 42  
66 84 69 78 81 78 80 72 51 27 36 65 73 49 54 76 48 84 51 70  
52 41 58 54 65 66 88 73 67 83 128 68 83 75 72 65 68 74 66 101  
110 141 144 90 98 77 98 80 73 88 124 105 95 106 99 95 86 73 57 56  
64 60 73 72 89 108 113 101 115 119 78 109 74 105 81 128 138 141 128 92  
124 127 120 111 161 152 155 119 112 77 94 154 180 112 172 168 149 179 219 154  
136 142 175 177 179 205 205 143 178 151 168 134 132 140 160 173 146 115 126 125  
96 164 84 110 92 121 115 99 108 107 122 107 114 112 125 88 89 83 118 110  
125 139 83 111 121 123 111 136 124 107 119 119 106 98 67 88 115 96 76 117  
120 124 111 101 100 147 124 155 129 137 106 130 109 103 98 104 84 88 143 145  
117 109 115 135 123 136

RIP-C08B 206

423 243 228 118 116 125 111 82 140 132 180 142 113 88 71 49 50 39 46 52  
56 78 60 74 81 83 88 59 45 35 46 65 72 53 49 79 50 72 61 56  
49 55 49 54 65 59 93 75 71 87 114 69 81 81 69 66 68 74 70 96  
110 148 129 108 103 77 94 90 80 84 115 95 113 100 99 108 78 76 53 52  
66 61 78 66 91 112 112 100 116 100 98 99 86 107 62 140 117 145 135 95  
112 138 123 113 145 139 154 121 117 75 100 141 176 124 172 172 136 185 212 160  
122 137 177 185 176 212 210 145 179 147 171 143 113 152 167 155 135 122 136 129  
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143 118 93 105 118 126 121 127 107 107 137 136 107 93 73 83 106 101 84 107  
120 132 104 93 104 144 134 146 127 152 95 142 120 99 93 107 88 86 141 138  
121 106 118 138 124 132

RIP-C09A 108

86 159 129 153 104 123 66 123 99 136 75 80 164 88 67 64 44 54 50 64  
66 68 80 119 74 62 62 63 72 154 119 76 66 78 55 64 101 106 95 157  
96 80 86 103 78 51 90 103 131 105 66 65 80 73 60 51 49 46 54 115  
137 132 151 137 144 137 115 87 92 141 119 81 69 84 85 95 83 130 78 59  
56 96 96 94 79 74 107 101 138 136 148 130 94 81 110 98 84 66 87 115  
112 110 97 119 84 97 97 105

RIP-C09B 108

109 158 126 142 121 122 55 118 105 120 77 85 145 84 66 60 57 49 50 58  
65 72 76 116 76 53 78 61 102 150 125 67 75 76 68 58 106 108 88 168  
94 83 84 102 77 55 81 112 141 90 64 66 75 70 58 55 51 52 63 101  
112 135 141 143 148 134 110 98 87 135 124 70 60 85 88 81 89 134 88 56  
62 91 98 99 74 98 117 82 137 141 141 134 107 74 113 100 93 70 69 111  
98 108 111 109 86 90 101 142

RIP-C10A 212

93 134 113 226 160 305 235 111 135 100 77 86 57 53 44 66 39 101 161 95  
113 82 97 87 60 80 87 88 64 106 105 113 107 87 89 59 145 101 72 77  
64 120 66 58 52 51 59 45 45 54 58 56 73 85 44 90 106 97 148 97  
46 68 57 49 35 102 93 85 101 78 77 85 103 60 51 70 91 92 66 79  
77 73 53 64 60 47 48 63 86 86 97 89 148 98 149 75 75 90 119 116  
60 66 91 71 78 73 106 70 63 85 103 100 98 75 85 137 108 134 106 136  
126 112 115 121 102 98 87 83 135 122 99 122 95 104 102 92 112 131 85 93  
166 119 84 71 123 113 103 74 80 62 75 68 74 71 72 93 104 90 132 118  
100 113 80 68 93 96 111 130 114 93 84 118 125 161 117 106 86 96 94 90  
101 76 106 86 66 81 96 105 95 115 84 103 82 121 114 100 124 87 74 79  
80 85 98 79 98 107 113 99 96 125 133 103

RIP-C10B 212

135 116 124 231 148 298 262 111 143 89 70 87 55 50 55 57 46 113 144 93  
116 85 96 94 62 77 87 81 68 111 99 104 119 85 79 64 147 96 72 85  
60 125 60 66 57 45 53 48 42 44 63 61 68 83 48 91 105 99 143 98  
48 61 63 45 54 84 101 81 100 83 77 80 98 63 57 71 88 97 64 70  
77 73 72 52 53 52 51 58 87 91 93 89 144 107 149 71 80 86 120 119  
62 58 91 67 79 66 103 70 67 83 99 104 102 72 85 141 111 129 104 137  
116 117 119 119 96 103 87 71 132 133 108 101 103 107 97 104 104 126 86 98  
159 118 88 73 128 116 95 79 72 69 77 65 78 61 83 91 100 87 135 126  
95 113 79 76 94 89 104 110 125 94 86 105 131 169 118 128 88 89 84 94  
106 67 102 92 62 98 93 105 111 110 87 102 93 114 108 103 118 93 76 88  
67 91 92 78 99 103 117 99 88 119 137 124

RIP-C11A 212

162 156 157 241 212 300 194 125 76 62 69 89 97 64 125 160 198 165 92 88  
70 63 50 49 39 98 96 101 64 78 154 134 164 104 79 122 222 239 218 111  
184 227 149 120 95 98 89 141 199 178 138 200 368 270 150 235 329 229 330 230  
163 171 166 162 154 194 253 255 292 246 160 124 270 164 134 153 179 97 102 80  
119 97 93 97 51 70 75 73 79 123 106 145 134 117 136 104 84 125 173 208  
141 127 97 139 137 148 244 198 148 145 179 191 146 95 151 102 105 169 186 193  
132 147 116 171 119 127 115 209 153 126 104 128 212 123 121 103 117 93 113 149  
164 135 128 116 118 87 99 75 97 85 116 83 106 102 80 104 92 114 97 106  
113 120 132 105 94 114 101 136 129 100 125 139 133 170 135 94 104 145 135 186  
140 142 170 150 164 282 219 218 207 133 126 141 165 189 155 170 154 117 182 165  
180 181 129 136 153 152 190 168 155 178 229 206

RIP-C11B 212

134 153 159 233 209 313 181 135 68 79 55 108 77 62 125 168 196 164 113 73  
89 53 45 59 39 85 103 97 66 89 149 137 163 106 78 128 215 229 217 110  
167 229 145 128 104 81 111 125 205 174 136 204 375 252 157 234 331 225 328 237  
168 165 135 157 141 198 258 270 277 249 151 130 294 164 120 147 186 108 99 85  
104 94 112 73 68 68 66 88 65 131 102 139 131 136 123 107 91 110 176 205  
150 120 109 122 133 141 240 192 153 151 178 191 144 90 154 106 108 163 190 185  
128 153 109 181 112 124 121 204 154 130 111 125 204 134 115 112 110 92 110 152  
159 147 132 108 118 94 86 83 98 85 103 87 103 104 80 97 93 112 98 109  
113 129 126 101 97 126 87 103 155 84 116 107 157 174 128 109 116 147 138 163  
142 144 169 136 167 286 221 219 212 129 119 154 167 183 171 156 159 139 162 159  
166 160 157 130 171 150 196 164 167 174 217 223

RIP-C12A 75

223 263 254 332 260 266 167 249 200 180 145 139 144 151 133 153 146 158 129 183  
165 138 196 195 198 193 215 181 165 208 225 242 218 195 304 361 269 225 185 181  
176 198 200 194 189 199 153 163 165 132 170 147 153 177 127 162 176 156 150 166  
116 141 142 137 103 122 144 167 170 159 156 137 118 189 200

RIP-C12B 75

219 253 264 362 247 245 158 265 188 218 199 143 144 134 134 147 169 184 162 179  
173 134 195 205 204 179 212 181 174 203 221 203 266 192 300 350 250 240 188 204  
188 207 185 179 184 211 171 176 162 119 145 126 164 178 129 168 186 136 172 161  
106 142 153 132 98 127 161 167 146 171 150 128 126 179 229

RIP-C13A 91

223 188 155 169 192 246 234 184 150 201 166 229 205 196 198 178 145 168 180 146  
200 157 211 216 186 189 212 178 140 205 117 183 164 127 198 223 216 134 180 210  
173 190 167 162 182 254 180 170 179 171 182 171 176 92 100 157 145 110 114 198  
160 149 145 172 154 131 142 167 136 93 96 106 133 115 133 133 106 134 112 122  
97 98 92 144 95 104 87 103 113 124 109

RIP-C13B 91

222 181 159 160 189 228 235 170 162 213 145 228 191 204 209 173 138 147 184 161  
209 176 187 223 204 213 206 183 147 181 137 204 149 134 208 209 214 132 205 237  
178 168 165 136 204 264 185 166 172 177 164 197 165 100 111 134 147 117 108 232  
155 149 158 171 149 131 137 173 139 101 80 101 136 127 127 136 115 133 121 124  
83 96 113 125 96 98 89 100 119 104 128

RIP-C14A 104

200 203 253 234 221 241 220 240 236 195 184 186 172 190 154 143 125 159 152 187  
136 129 149 161 136 127 132 121 108 112 96 132 119 147 156 147 152 143 142 178  
157 164 145 96 148 148 92 187 163 147 111 179 191 170 146 139 132 176 237 196  
173 180 116 166 135 144 112 104 147 150 118 97 172 168 143 167 153 122 101 133  
150 122 106 96 126 179 110 118 135 124 146 128 132 95 98 118 124 92 91 110  
153 110 97 119

RIP-C14B 104

172 211 232 200 240 239 186 274 229 219 181 176 232 173 157 142 127 159 179 163  
134 119 140 148 149 141 155 106 117 116 96 128 113 145 174 154 148 144 142 177  
151 151 142 96 167 127 108 161 167 154 95 170 205 160 147 141 143 180 215 247  
137 184 117 142 158 166 97 104 143 151 94 108 186 137 130 173 149 132 101 121  
156 132 86 99 129 152 106 139 134 120 120 157 140 86 110 120 112 92 82 105  
159 117 92 122

RIP-C15A 83

212 198 155 146 164 135 137 143 137 144 153 112 145 139 101 144 112 98 136 118  
126 115 110 66 76 54 73 110 115 100 151 110 76 88 72 108 86 108 97 115  
106 110 119 121 130 103 112 99 104 83 62 90 77 78 93 84 87 63 95 68  
72 51 54 77 72 84 86 69 66 83 83 68 62 74 54 72 78 50 71 102  
86 86 129

RIP-C15B 83

185 205 143 140 174 135 147 147 124 139 107 105 116 129 128 118 118 117 140 125  
124 128 78 79 70 53 77 121 105 112 146 103 76 87 79 93 105 89 112 103  
111 97 126 130 139 97 112 105 89 88 80 91 70 82 94 81 86 57 96 70  
79 50 46 76 73 88 83 76 78 72 83 63 58 72 56 79 67 53 74 75  
109 80 127

RIP-C16A 79

178 342 485 486 448 410 235 210 300 269 377 361 321 311 222 299 270 251 252 186  
228 307 253 194 285 234 171 147 119 113 113 90 110 126 138 163 152 141 147 135  
159 151 106 86 164 143 163 157 136 170 123 155 120 72 115 129 108 82 69 88  
66 87 112 77 85 146 173 169 117 118 85 84 96 65 64 54 61 57 58

RIP-C16B 79

128 356 484 475 432 392 223 196 308 273 366 366 315 317 232 286 255 253 250 186  
225 303 261 194 294 203 150 155 119 102 113 100 108 141 126 167 133 151 157 128  
161 154 97 89 177 120 166 151 140 174 127 153 126 81 99 134 98 87 74 77  
76 81 116 71 89 142 169 172 119 132 74 90 90 78 60 45 70 51 46

RIP-C17A 120

85 89 138 138 113 173 460 351 205 233 170 297 171 239 189 200 268 221 197 155  
299 262 302 262 165 168 180 216 231 140 191 109 122 139 154 130 113 93 98 64  
109 162 128 240 131 192 316 346 419 186 145 307 262 107 50 44 48 59 45 41  
62 47 74 103 94 99 118 121 135 114 215 203 133 182 222 232 177 157 214 220  
106 161 146 117 114 116 147 150 130 99 109 106 80 109 130 130 151 147 147 137  
158 147 138 160 129 151 117 114 81 130 150 178 169 135 107 129 121 130 158 154

RIP-C17B 120

97 84 135 134 124 176 443 353 207 245 174 313 178 229 204 211 269 201 197 153  
317 246 292 274 180 169 164 215 231 151 193 109 115 148 147 136 97 91 95 80  
96 164 136 234 130 208 348 355 443 187 110 305 255 106 52 53 38 52 41 52  
51 40 76 91 101 95 125 124 123 112 221 215 131 178 215 234 185 160 213 208  
106 159 162 113 94 128 142 154 123 95 131 103 88 94 145 135 157 138 146 135  
157 150 126 172 127 146 121 116 96 121 145 174 187 109 115 144 130 117 178 177

RIP-C18A 66

81 127 166 174 184 159 118 245 301 205 147 192 255 176 136 269 272 170 226 228  
220 244 150 239 233 192 155 198 190 178 121 152 183 131 167 185 170 170 201 227  
202 156 172 139 149 148 209 184 244 287 286 271 308 267 226 270 179 211 242 247  
199 202 192 172 221 243

RIP-C18B 66

96 125 164 175 191 149 120 252 296 209 156 190 251 178 138 256 239 180 241 219  
195 257 142 225 242 190 153 218 177 166 126 154 176 133 156 190 156 180 182 228  
193 175 172 137 134 147 209 168 249 253 312 286 304 283 238 279 197 193 237 197  
267 204 177 174 216 256

RIP-C19A 89

302 462 465 426 244 274 365 275 270 271 268 344 267 131 290 307 292 241 248 276  
271 281 175 159 144 119 186 196 99 173 195 111 158 147 182 199 139 155 124 127  
105 99 90 128 107 108 78 116 82 107 97 125 128 151 153 108 110 102 111 123  
130 98 104 142 164 202 119 134 136 123 117 124 144 145 118 167 139 155 156 145  
176 213 224 124 168 233 246 233 227

RIP-C19B 89

290 457 501 422 223 283 357 263 278 256 275 347 258 161 264 289 293 253 264 276  
292 306 167 165 138 111 182 183 122 167 176 106 159 142 180 208 125 167 131 96  
116 102 80 141 110 105 86 102 94 104 104 114 121 153 168 129 95 119 108 121  
121 112 91 143 161 212 109 133 128 130 118 118 150 149 116 172 135 158 159 139  
181 199 192 152 172 237 231 217 255

RIP-C20A 82

245 236 254 198 189 156 174 133 150 134 108 138 123 128 133 132 121 123 114 89  
107 110 92 88 71 99 142 177 130 146 163 130 154 157 169 180 166 186 219 209  
196 189 210 220 174 137 143 180 169 130 175 118 218 160 194 170 182 168 175 174  
176 100 144 173 153 156 142 157 183 125 138 148 158 163 137 137 117 131 93 144  
136 139

RIP-C20B 82

233 240 243 202 178 157 185 127 144 158 102 131 97 127 128 123 123 133 128 106  
104 106 93 97 66 107 136 177 166 179 157 126 163 186 160 173 180 190 214 202  
195 204 208 217 193 138 148 175 170 126 171 129 202 168 187 184 177 148 187 181  
158 108 137 183 161 154 133 149 208 120 132 157 160 147 143 149 119 114 108 136  
136 130

RIP-C21A 82

82 154 129 160 169 206 229 260 357 213 337 475 225 414 355 311 280 245 244 257  
169 179 156 97 119 168 220 225 207 255 109 70 90 94 135 156 110 98 109 120  
106 116 145 162 115 120 76 64 70 121 107 130 133 95 99 51 92 91 106 108  
110 132 141 116 141 108 101 187 132 115 104 79 73 156 103 149 94 97 92 103  
65 116

RIP-C21B 82

81 150 134 160 161 220 220 254 268 217 345 481 215 465 374 326 259 269 243 247  
165 176 155 100 116 166 216 211 207 235 112 81 79 108 116 157 111 111 96 115  
107 104 152 169 121 107 82 55 93 103 119 127 123 97 88 63 73 101 95 114  
113 127 144 121 136 112 107 183 129 114 111 82 72 151 101 136 106 92 85 103  
73 101

RIP-C22A 79

391 389 396 379 287 283 233 194 149 236 194 244 180 276 301 208 256 219 235 270  
247 189 236 178 167 184 135 164 251 277 242 226 313 354 260 295 346 379 324 486  
296 365 309 435 305 280 326 255 234 357 352 265 227 287 207 247 260 297 236 237  
168 142 250 177 136 235 173 223 217 266 264 252 268 218 247 260 190 205 204

RIP-C22B 79

439 367 361 366 313 247 225 185 173 238 193 235 185 276 304 252 227 221 226 252  
249 196 231 185 173 179 186 156 262 284 202 235 314 353 265 283 344 401 327 487  
284 362 324 398 294 273 336 243 233 368 359 270 228 292 199 252 259 304 222 241  
162 148 253 180 135 226 173 212 216 279 247 265 262 201 256 274 179 212 219

RIP-C23A 125

108 103 65 67 75 89 119 110 136 134 131 177 145 153 160 165 162 121 135 110  
141 146 151 202 149 119 140 132 131 182 144 131 106 126 136 168 118 157 113 126  
93 124 129 118 124 128 120 91 99 74 98 88 85 91 87 85 91 77 101 85  
100 96 111 88 114 89 64 84 56 56 58 60 74 92 88 70 38 65 85 92  
85 89 99 88 84 114 108 127 94 145 137 130 114 90 154 99 129 112 93 113  
124 147 114 139 106 92 118 90 89 146 111 130 123 123 148 76 55 91 119 131  
103 131 94 139 156

RIP-C23B 125

118 100 63 68 80 93 111 120 123 156 118 178 143 147 183 162 170 131 141 111  
142 142 153 174 136 101 145 127 145 187 112 124 123 110 140 165 129 150 119 127  
75 144 124 120 115 129 124 100 86 80 110 97 76 105 80 101 80 74 101 87  
101 112 89 97 113 82 65 86 49 68 54 58 70 88 94 58 45 74 77 101  
77 85 100 95 83 107 109 125 100 137 133 132 118 80 165 101 128 116 100 106  
131 137 103 138 112 99 113 94 94 144 116 128 126 127 144 72 60 85 120 133  
111 113 102 133 138

RIP-C24A 120

114 134 126 114 172 149 144 177 151 157 113 129 123 142 157 171 205 158 103 152  
126 135 175 129 136 110 121 140 159 148 158 117 107 91 135 123 120 105 134 141  
105 86 86 101 110 73 107 81 104 76 78 94 98 91 116 108 93 103 84 82  
73 66 64 45 71 85 109 100 57 45 76 78 94 99 79 101 88 93 109 120  
128 100 114 121 122 111 90 154 106 132 116 90 101 97 106 103 123 106 93 126  
112 92 165 131 122 146 122 136 62 86 86 142 133 110 125 112 103 143 144 225

RIP-C24B 120

112 123 127 115 180 150 135 181 146 151 129 132 120 141 151 173 211 165 107 131  
125 130 172 132 135 133 113 132 165 151 165 123 105 87 129 130 115 124 135 140  
96 87 97 90 109 78 113 82 97 73 86 95 91 94 114 95 102 111 87 80  
73 52 72 50 71 83 109 84 54 49 73 76 98 96 75 95 93 87 104 123  
128 105 129 125 112 113 88 151 114 128 108 102 100 94 115 91 121 106 105 120  
114 97 158 127 121 141 126 141 76 67 99 138 125 112 123 120 99 144 141 169

RIP-C25A 92

138 154 282 218 275 220 221 189 150 170 134 178 162 152 86 124 157 168 137 129  
144 112 101 142 156 70 100 106 95 119 138 121 134 112 153 135 122 111 106 110  
138 193 209 130 171 126 112 166 124 176 136 160 186 143 192 122 166 258 366 292  
179 135 162 175 138 140 88 112 124 123 125 92 118 104 133 83 78 95 123 144  
152 106 139 148 122 124 123 120 116 140 119 151

RIP-C25B 92

144 174 268 208 276 221 159 173 174 174 151 185 147 151 115 135 161 151 132 144  
131 101 102 133 159 94 115 103 94 130 124 124 143 153 138 129 135 105 112 102  
166 186 193 136 172 144 121 155 141 156 141 163 174 152 176 193 155 242 351 286  
167 142 179 160 135 154 107 104 127 117 120 99 141 98 110 78 88 105 134 115  
143 95 129 142 136 110 128 133 110 122 115 141

RIP-C26A 53

351 349 204 139 129 219 233 338 307 322 356 335 447 356 336 316 230 376 317 318  
321 433 352 513 446 397 442 410 292 374 320 269 293 245 302 396 351 349 375 324  
248 264 235 226 249 253 238 230 315 293 292 350 507

RIP-C26B 54

123 139 56 168 328 189 131 141 197 217 338 305 327 373 344 438 398 308 286 235  
364 399 297 296 449 332 543 423 347 453 422 298 325 323 275 295 257 318 378 376  
357 361 326 221 286 238 220 244 251 248 241 316 277 283

RIP-C27A 130

195 170 116 180 201 192 200 177 165 213 219 207 173 175 147 195 256 236 198 170  
216 250 220 242 238 100 78 74 62 113 159 199 150 122 85 151 139 103 98 141  
117 99 133 206 132 119 114 161 118 169 131 154 143 172 185 161 162 158 227 255  
133 235 242 169 160 181 179 194 115 122 97 94 110 160 203 160 177 204 102 95  
116 151 168 176 136 99 129 142 165 163 197 194 151 126 116 120 156 189 175 203  
130 143 124 83 94 97 87 112 171 177 196 133 135 108 113 228 181 126 84 88  
91 171 148 122 102 85 89 130 122 165

RIP-C27B 130

226 191 126 191 218 251 159 146 189 231 197 248 132 149 151 184 253 238 191 140  
211 241 233 234 229 131 81 83 67 112 160 198 145 129 86 137 137 83 100 134  
118 109 161 186 142 96 114 148 108 173 125 152 140 155 186 165 167 144 221 249  
146 246 236 150 179 168 181 200 108 137 109 82 101 160 204 153 163 207 115 86  
113 143 167 174 134 111 138 138 149 164 208 208 136 132 141 109 145 191 157 204  
119 148 133 78 94 93 101 111 169 175 199 122 138 114 108 242 169 127 78 91  
81 177 152 129 84 102 83 133 141 127

RIP-C28A 69

81 99 85 114 93 104 92 65 77 59 82 71 77 78 83 84 156 197 226 220  
219 303 184 172 190 211 197 165 222 210 237 247 229 218 248 120 143 233 234 151  
162 210 181 74 120 187 179 152 205 240 300 225 332 204 174 247 204 235 253 153  
104 157 158 210 174 164 199 239 270

RIP-C28B 69

79 91 92 103 100 108 97 64 78 59 83 77 76 89 83 83 164 250 236 230  
223 299 191 210 179 195 183 165 217 223 241 239 236 246 237 130 156 214 235 131  
175 192 178 90 111 183 172 147 215 225 304 250 326 194 180 217 208 222 233 154  
110 157 155 218 147 187 191 245 274

RIP-C29A 117

330 422 371 356 445 413 383 335 318 235 185 178 104 145 249 361 260 184 229 242  
256 306 316 251 277 263 225 167 197 189 213 248 211 188 191 177 211 291 251 244  
192 180 139 160 199 146 170 162 131 215 166 167 154 135 189 172 138 101 118 116  
130 163 166 134 189 176 144 137 189 229 215 212 213 187 181 162 159 224 179 169  
137 124 165 121 168 150 135 154 174 162 172 124 139 119 130 103 91 176 181 199  
206 188 158 192 186 152 124 143 143 157 143 169 148 185 260 275 280

RIP-C29B 117

299 413 365 361 441 413 384 328 322 235 185 182 100 160 243 365 256 176 217 247  
251 317 308 269 269 272 223 172 189 183 206 257 215 195 185 179 222 277 261 248  
189 181 158 158 202 145 152 173 115 204 163 166 158 136 187 167 138 100 119 126  
130 156 173 137 199 156 147 159 175 217 216 229 201 177 175 160 162 221 184 171  
132 137 144 124 150 160 142 159 175 153 174 127 130 122 123 114 97 167 187 175  
197 196 157 182 173 155 132 141 151 158 138 163 151 204 239 273 281

RIP-C30A 110

402 475 392 199 208 193 288 252 232 207 198 218 251 273 271 265 268 232 194 196  
241 160 181 165 209 157 168 113 146 209 156 122 120 105 91 92 109 115 107 144  
109 143 146 149 126 131 138 103 93 108 84 108 87 113 139 163 98 123 99 97  
105 113 120 103 108 121 120 195 127 156 124 100 96 98 95 103 114 113 136 105  
108 120 113 115 98 137 105 121 68 88 91 112 129 137 118 122 149 119 109 132  
104 110 122 83 109 95 103 120 145 147

RIP-C30B 110

376 470 408 203 193 209 273 285 224 199 190 227 253 260 255 257 272 242 186 215  
224 163 193 162 213 174 168 130 135 201 141 136 120 96 97 87 106 126 81 142  
112 127 136 151 135 135 141 102 106 95 80 93 98 107 136 160 108 123 97 87  
113 106 117 100 113 119 125 190 130 147 127 98 104 97 101 112 111 120 122 101  
124 104 116 125 90 135 99 127 81 80 89 115 117 147 102 129 139 134 122 122  
112 102 106 115 98 111 88 115 142 145

## APPENDIX

### Tree-Ring Dating

#### The Principles of Tree-Ring Dating

Tree-ring dating, or *dendrochronology* as it is known, is discussed in some detail in the Laboratory's Monograph, '*An East Midlands Master Tree-Ring Chronology and its uses for dating Vernacular Building*' (Laxton and Litton 1988) and, *Dendrochronology; Guidelines on Producing and Interpreting Dendrochronological Dates* (English Heritage 1988). Here we will give the bare outlines. Each year an oak tree grows an extra ring on the outside of its trunk and all its branches just inside its bark. The *width* of this annual ring depends largely on the weather during the growing season, about April to October, and possibly also on the weather during the previous year. Good growing seasons give rise to relatively wide rings, poor ones to very narrow rings and average ones to relatively average ring widths. Since the climate is so variable from year to year, almost random-like, the widths of these rings will also appear random-like in sequence, reflecting the seasons. This is illustrated in Figure 1 where, for example, the widest rings appear at irregular intervals. This is the key to dating by tree rings, or rather, by their widths. Records of the average ring widths for oaks, one for each year for the last 1000 years or more, are available for different areas. These are called master chronologies. Because of the random-like nature of these sequences of widths, there is usually only one position at which a sequence of ring widths from a sample of oak timber with at least 70 rings will match a master. This will date the timber and, in particular, the last ring.

If the bark is still on the sample, as in Figure 1, then the date of the last ring will be the date of felling of the oak from which it was cut. There is much evidence that in medieval times oaks cut down for building purposes were used almost immediately, usually within the year or so (Rackham 1976). Hence if bark is present on several main timbers in a building, none of which appear reused or are later insertions, and if they all have the same date for their last ring, then we can be quite confident that this is the date of construction or soon after. If there is no bark on the sample, then we have to make an estimate of the felling date; how this is done is explained below.

#### The Practice of Tree-Ring Dating at the University of Nottingham Tree-Ring dating Laboratory

1. ***Inspecting the Building and Sampling the Timbers.*** Together with a building historian the timbers in a building are inspected to try to ensure that those sampled are not reused or later insertions. Sampling is almost always done by coring into the timber, which has the great advantage that we can sample *in situ* timbers and those judged best to give the date of construction, or phase of construction if there is more than one in the building. The timbers to be sampled are also inspected to see how many rings they have. We normally look for timbers with at least 70 rings, and preferably more. With fewer rings than this, 50 for example, sequences of widths become difficult to match to a unique position within a master sequence of ring widths and so are difficult to date (Litton and Zainodin 1991). The cross-section of the rafter shown in Figure 2 has about 120 rings; about 20 of which are sapwood rings – the lighter rings on the outside. Similarly the core has just over 100 rings with a few sapwood rings.

To ensure that we are getting the date of the building as a whole, or the whole of a phase of construction if there is more than one, about 8 to 10 samples per phase are usually taken. Sometimes we take many more, especially if the construction is complicated. One reason for taking so many samples is that, in general, some will fail to give a date. There may be many reasons why a particular sequence of ring widths from a sample of timber fails to give a date even though others from the same building do. For example, a particular tree may have grown in an odd ecological niche, so odd indeed that the widths of its rings were determined by factors other than the local climate! In such circumstances it will be impossible to date a timber from this tree using the master sequence whose widths, we can assume, were predominantly determined by the local climate at the time.



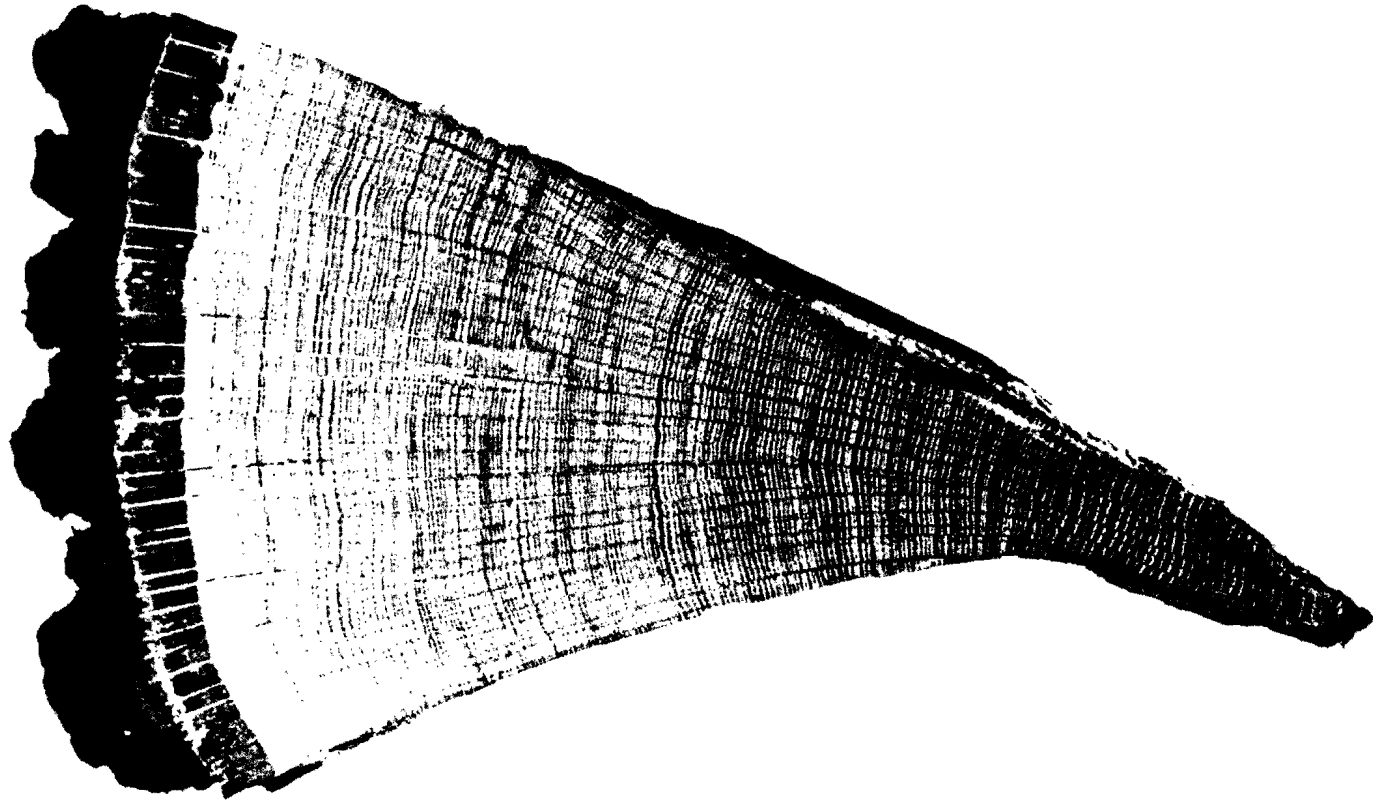


Fig 1. A wedge of oak from a tree felled in 1976. It shows the annual growth rings, one for each year from the innermost ring to the last ring on the outside just inside the bark. The year of each ring can be determined by counting back from the outside ring, which grew in 1976.

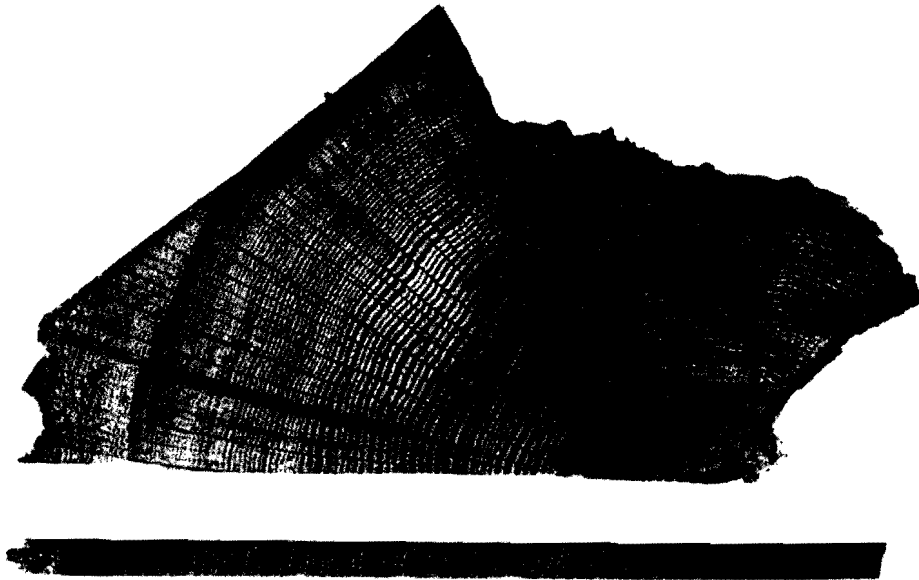


Fig 2. Cross-section of a rafter showing the presence of sapwood rings in the left hand corner, the arrow is pointing to the heartwood/sapwood boundary (H/S). Also a core with sapwood; again the arrow is pointing to the H/S. The core is about the size of a pencil.



Fig. 3 Measuring ring widths under a microscope. The microscope is fixed while the sample is on a moving platform. The total sequence of widths is measure twice to ensure that an error has not been made. This type of apparatus is needed to process a large number of samples on a regular basis.

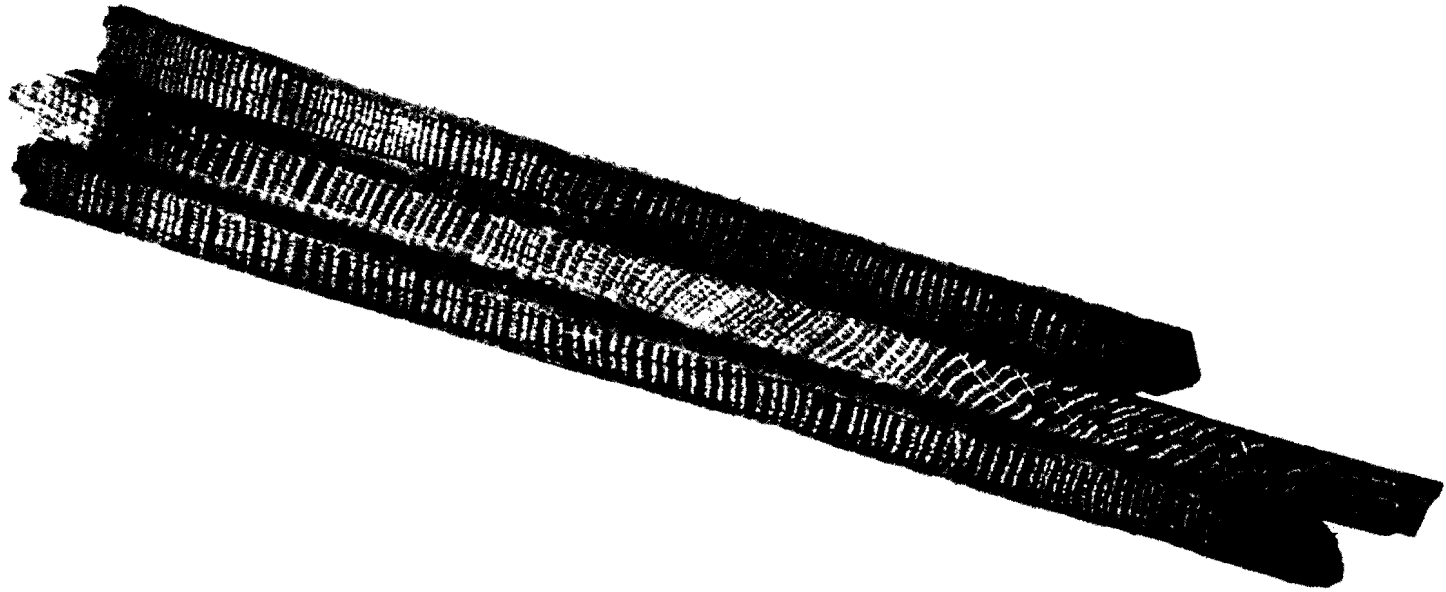


Fig 4. Three cores from timbers in a building. They come from trees growing at the same time. Notice that, although the sequences of widths look similar, they are not identical. This is typical.

Sampling is done by coring into the timber with a hollow corer attached to an electric drill and usually from its outer rings inwards towards where the centre of the tree, the pith, is judged to be. An illustration of a core is shown in Figure 2; it is about 15cm long and 1cm diameter. Great care has to be taken to ensure that as few as possible of the outer rings are lost in coring. This can be difficult as these outer rings are often very soft (see below on sapwood). Each sample is given a code which identifies uniquely which timber it comes from, which building it is from and where the building is located. For example, CRO-A06 is the sixth core taken from the first building (A) sampled by the Laboratory in Cropwell Bishop. Where it came from in that building will be shown in the sampling records and drawings. No structural damage is done to any timbers by coring, nor does it weaken them.

During the initial inspection of the building and its timbers the dendrochronologist may come to the conclusion that, as far as can be judged, none of the timbers have sufficient rings in them for dating purposes and may advise against sampling to save further unwarranted expense.

All sampling by the Laboratory is undertaken according to current Health and Safety Standards. The Laboratory's dendrochronologists are insured.

2. **Measuring Ring Widths.** Each core is sanded down with a belt sander using medium-grit paper and then finished by hand with flourgrade-grit paper. The rings are then clearly visible and differentiated from each other with a result very much like that shown in Figure 2. The core is then mounted on a movable table below a microscope and the ring-widths measured individually from the innermost ring to the outermost. The widths are automatically recorded in a computer file as they are measured (see Fig 3).
3. **Cross-matching and Dating the Samples.** Because of the factors besides the local climate which may determine the annual widths of a tree's rings, no two sequences of ring widths from different oaks growing at the same time are exactly alike (Fig 4). Indeed, the sequences may not be exactly alike even when the trees are growing near to each other. Consequently, in the Laboratory we do not attempt to match two sequences of ring widths by eye, or graphically, or by any other subjective method. Instead, it is done objectively (ie statistically) on a computer by a process called cross-matching. The output from the computer tells us the extent of correlation between two sample sequences of widths or, if we are dating, between a sample sequence of widths and the master, at each relative position of one to the other (offsets). The extent of the correlation at an offset is determined by the *t-value* (defined in almost any introductory book on statistics). That offset with the maximum *t-value* among the *t-values* at all the offsets will be the best candidate for dating one sequence relative to the other. If one of these is a master chronology, then this will date the other. Experiments carried out in the past with sequences from oaks of known date suggest that a *t-value* of at least 4.5, and preferably at least 5.0, is usually adequate for the dating to be accepted with reasonable confidence (Laxton and Litton 1988; Laxton *et al* 1988; Howard *et al* 1984-1995).

This is illustrated in Fig 5 with timbers from one of the roofs of Lincoln Cathedral. Here four sequences of ring widths, LIN-C04, 05, 08, and 45, have been cross-matched with each other. The ring widths themselves have been omitted in the *bar-diagram*, as is usual, but the offsets at which they best cross-match each other are shown; eg the sequence of ring widths of C08 matches the sequence of ring widths of C45 best when it is at a position starting 20 rings after the first ring of C45, and similarly for the others. The actual *t-values* between the four at these offsets of best correlations are in the matrix. Thus at the offset of +20 rings, the *t-value* between C45 and C08 is 5.6 and is the maximum found between these two among all the positions of one sequence relative to the other.

It is standard practice in our Laboratory first to cross-match as many as possible of the ring-width sequences of the samples in a building and then to form an average from them. This average is called a *site sequence* of the building being dated and is illustrated in Fig 5. The fifth bar at the bottom is a site sequence for a roof at Lincoln Cathedral and is constructed from the matching sequences of the four timbers. The site sequence width for each year is the average of the widths in each of the sample sequences which has a width for that year. Thus in Fig 5 if the widths shown are 0.8mm for C45, 0.2mm for C08, 0.7mm for C05, and 0.3mm for C04, then the corresponding width of the site sequence is the average of these, 0.55mm. The actual sequence

of widths of this site sequence is stored on the computer. The reason for creating site sequences is that it is usually easier to date an average sequence of ring widths with a master sequence than it is to date the individual component sample sequences separately.

The straightforward method of cross-matching several sample sequences with each other one at a time is called the 'maximal *t*-value' method. The actual method of cross-matching a group of sequences of ring-widths used in the Laboratory involves grouping and averaging the ring-width sequences and is called the 'Litton-Zainodin Grouping Procedure'. It is a modification of the straight forward method and was successfully developed and tested in the Laboratory and has been published (Litton and Zainodin 1991; Laxton *et al* 1988).

4. ***Estimating the Felling Date.*** As mentioned above, if the bark is present on a sample, then the date of its last ring is the date of the felling of its tree. Actually it could be the year after if it had been felled in the first three months before any new growth had started, but this is not too important a consideration in most cases. The actual bark may not be present on a timber in a building, though the dendrochronologist who is sampling can often see from its surface that only the bark is missing. In these cases the date of the last ring is still the date of felling.

Quite often some, though not all, of the original outer rings are missing on a timber. The outer rings on an oak, called *sapwood* rings, are usually lighter than the inner rings, the *heartwood*, and so are relatively easy to identify. For example, sapwood can be seen in the corner of the rafter and at the outer end of the core in Figure 2, both indicated by arrows. More importantly for dendrochronology, the sapwood is relatively soft and so liable to insect attack and wear and tear. The builder, therefore, may remove some of the sapwood for precisely these reasons. Nevertheless, if at least some of the sapwood rings are left on a sample, we will know that not too many rings have been lost since felling so that the date of the last ring on the sample is only a few years before the date of the original last ring on the tree, and so to the date of felling.

Various estimates have been made and used for the average number of sapwood rings in mature oak trees (English Heritage 1998). A fairly conservative range is between 15 and 50 and that this holds for 95% of mature oaks. This means, of course, that in a small number of cases there could be fewer than 15 and more than 50 sapwood rings. For example, the core CRO-A06 has only 9 sapwood rings and some have obviously been lost over time – either they were removed originally by the carpenter and/or they rotted away in the building and/or they were lost in the coring. It is not known exactly how many sapwood rings are missing, but using the above range the Laboratory would estimate between a minimum of 6 (=15-9) and a maximum of 41 (=50-9). If the last ring of CRO-A06 has been dated to 1500, say, then the estimated felling-date range for the tree from which it came originally would be between 1506 and 1541. The Laboratory uses this estimate for sapwood in areas of England where it has no prior information. It also uses it when dealing with samples with very many rings, about 120 to the last heartwood ring. But in other areas of England where the Laboratory has accumulated a number of samples with complete sapwood, that is, no sapwood lost since felling, other estimates in place of the conservative range of 15 to 50 are used. In the East Midlands (Laxton *et al* 2001) and the east to the south down to Kent (Pearson 1995) where it has sampled extensively in the past, the Laboratory uses the shorter estimate of 15 to 35 sapwood rings in 95% of mature oaks growing in these parts. Since the sample CRO-A06 comes from a house in Cropwell Bishop in the East Midlands, a better estimate of sapwood rings lost since felling is between a minimum of 6 (=15-9) and 26 (=35-9) and the felling would be estimated to have taken place between 1506 and 1526, a shorter period than before. (Oak boards quite often come from the Baltic and in these cases the 95% confidence limits for sapwood are 9 to 36 (Howard *et al* 1992, 56)).

Even more precise estimates of the felling date and range can often be obtained using knowledge of a particular case and information gathered at the time of sampling. For example, at the time of sampling the dendrochronologist may have noted that the timber from which the core of Figure 2 was taken still had complete sapwood but that none of the soft sapwood rings were lost in coring. By measuring into the timber the depth of sapwood lost, say 2 cm, a reasonable estimate can be made of the number of sapwood rings lost, say 12 to 15 rings in this case. By adding on 12 to 15 years to the date of the last ring on the sample a good tight estimate for the range of the felling date can be obtained, which is often better than the 15 to 35 years later we would have estimated without this observation. In the example, the felling is now estimated to

t-value/offset Matrix

	C45	C08	C05	C04
C45		+20	+37	+47
C08	5.6		+17	+27
C05	5.2	10.4		+10
C04	5.9	3.7	5.1	

Bar Diagram

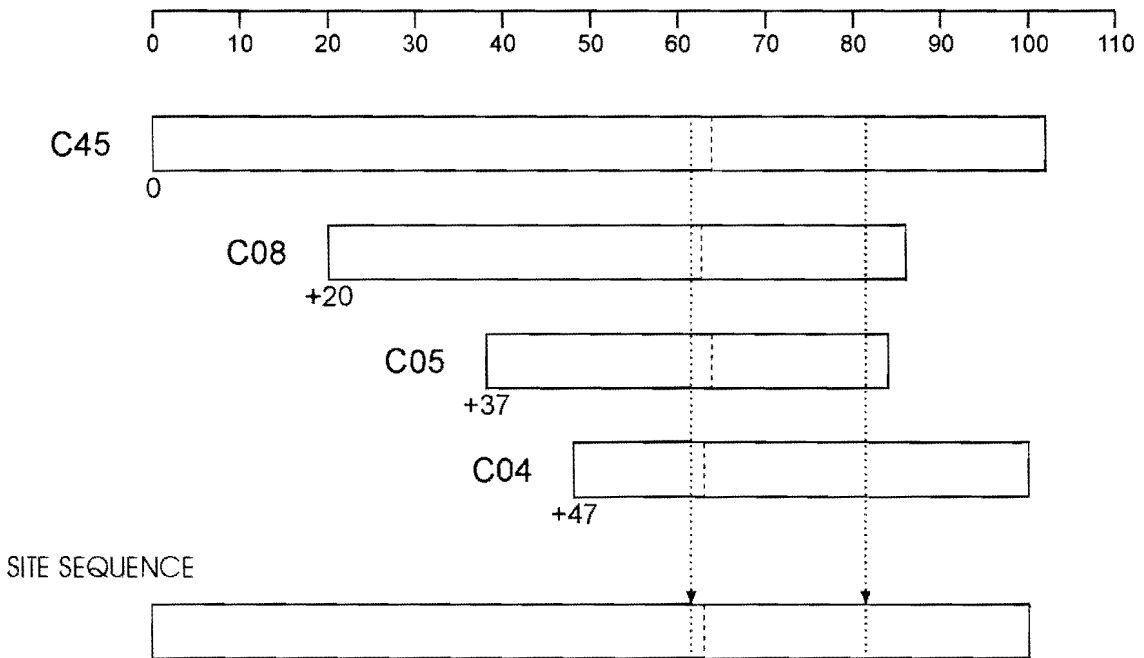


Fig 5. Cross-matching of four sequences from a Lincoln Cathedral roof and the formation of a site sequence from them.

The *bar diagram* represents these sequences without the rings themselves. The length of the bar is proportional to the number of rings in the sequence. Here the four sequences are set at relative positions (*offsets*) to each other at which they have maximum correlation as measured by the *t*-values.

The *t*-value/offset matrix contains the maximum *t*-values below the diagonal and the offsets above it. Thus, the maximum *t*-value between C08 and C45 occurs at the offset of +20 rings and the *t*-value is then 5.6.

The *site sequence* is composed of the average of the corresponding widths, as illustrated with one width.

have taken place between AD 1512 and 1515, which is much more precise than without this extra information.

Even if all the sapwood rings are missing on a sample, but none of the heartwood rings are, then an estimate of the felling-date range is possible by adding on the full complement of, say, 15 to 35 years to the date of the last heartwood ring (called the heartwood/sapwood boundary or transition ring and denoted H/S). Fortunately it is often easy for a trained dendrochronologist to identify this boundary on a timber. If a timber does not have its heartwood/sapwood boundary, then only a *post quem* date for felling is possible.

5. ***Estimating the Date of Construction.*** There is a considerable body of evidence collected by dendrochronologists over the years that oak timbers used in buildings were not seasoned in medieval or early modern times (English Heritage 1998 and Miles 1997, 50-55). Hence provided all the samples in a building have estimated felling-date ranges broadly in agreement with each other, so that they appear to have been felled as a group, then this should give an accurate estimate of the period when the structure was built, or soon after (Laxton *et al* 2001, figure 8 and pages 34-5 where 'associated groups of fellings' are discussed in detail). However, if there is any evidence of storing before use or if there is evidence the oak came from abroad (eg Baltic boards), then some allowance has to be made for this.
  
6. ***Master Chronological Sequences.*** Ultimately, to date a sequence of ring widths, or a site sequence, we need a master sequence of dated ring widths with which to cross-match it, a Master Chronology. To construct such a sequence we have to start with a sequence of widths whose dates are known and this means beginning with a sequence from an oak tree whose date of felling is known. In Fig 6 such a sequence is SHE-T, which came from a tree in Sherwood Forest which was blown down in a recent gale. After this other sequences which cross-match with it are added and gradually the sequence is 'pushed back in time' as far as the age of samples will allow. This process is illustrated in Fig 6. We have a master chronological sequence of widths for Nottinghamshire and East Midlands oak for each year from AD 882 to 1981. It is described in great detail in Laxton and Litton (1988), but the components it contains are shown here in the form of a bar diagram. As can be seen, it is well replicated in that for each year in this period there are several sample sequences having widths for that year. The master is the average of these. This master can now be used to date oak from this area and from the surrounding areas where the climate is very similar to that in the East Midlands. The Laboratory has also constructed a master for Kent (Laxton and Litton 1989). The method the Laboratory uses to construct a master sequence, such as the East Midlands and Kent, is completely objective and uses the Litton-Zainodin grouping procedure (Laxton *et al* 1988). Other laboratories and individuals have constructed masters for other areas and have made them available. As well as these masters, local (dated) site chronologies can be used to date other buildings from nearby. The Laboratory has hundreds of these site sequences from many parts of England and Wales covering many short periods.
  
7. ***Ring-width Indices.*** Tree-ring dating can be done by cross-matching the ring widths themselves, as described above. However, it is advantageous to modify the widths first. Because different trees grow at different rates and because a young oak grows in a different way from an older oak, irrespective of the climate, the widths are first standardized before any matching between them is attempted. These standard widths are known as ring-width indices and were first used in dendrochronology by Baillie and Pilcher (1973). The exact form they take is explained in this paper and in the appendix of Laxton and Litton (1988) and is illustrated in the graphs in Fig 7. Here ring-widths are plotted vertically, one for each year of growth. In the upper sequence of (a), the generally large early growth after 1810 is very apparent as is the smaller later growth from about 1900 onwards when the tree is maturing. A similar phenomena can be observed in the lower sequence of (a) starting in 1835. In both the widths are also changing rapidly from year to year. The peaks are the wide rings and the troughs are the narrow rings corresponding to good and poor growing seasons, respectively. The two corresponding sequence of Baillie-Pilcher indices are plotted in (b) where the differences in the immature and mature growths have been removed and only the rapidly changing peaks and troughs remain, that are associated with the common climatic signal. This makes cross-matching easier.

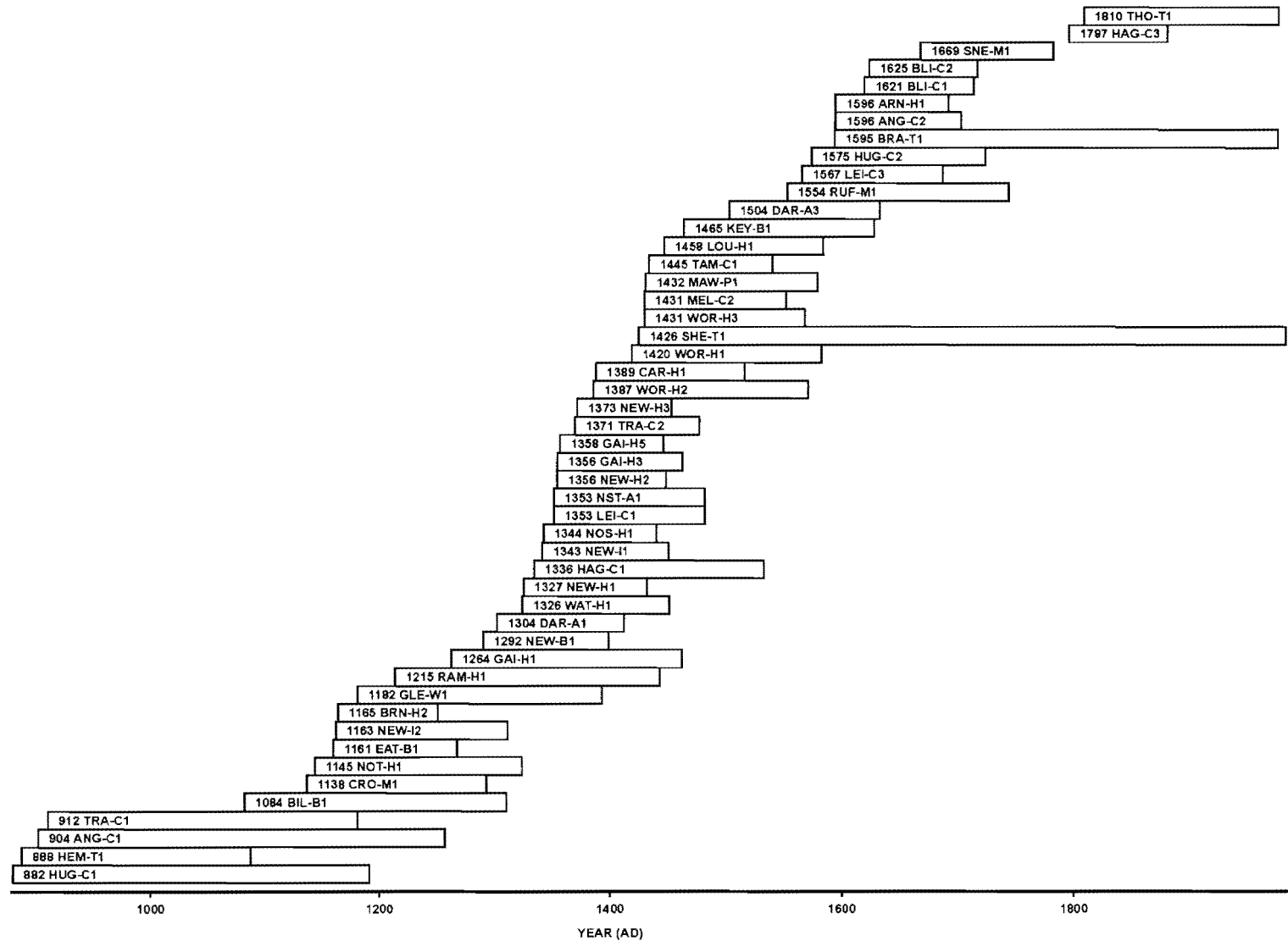
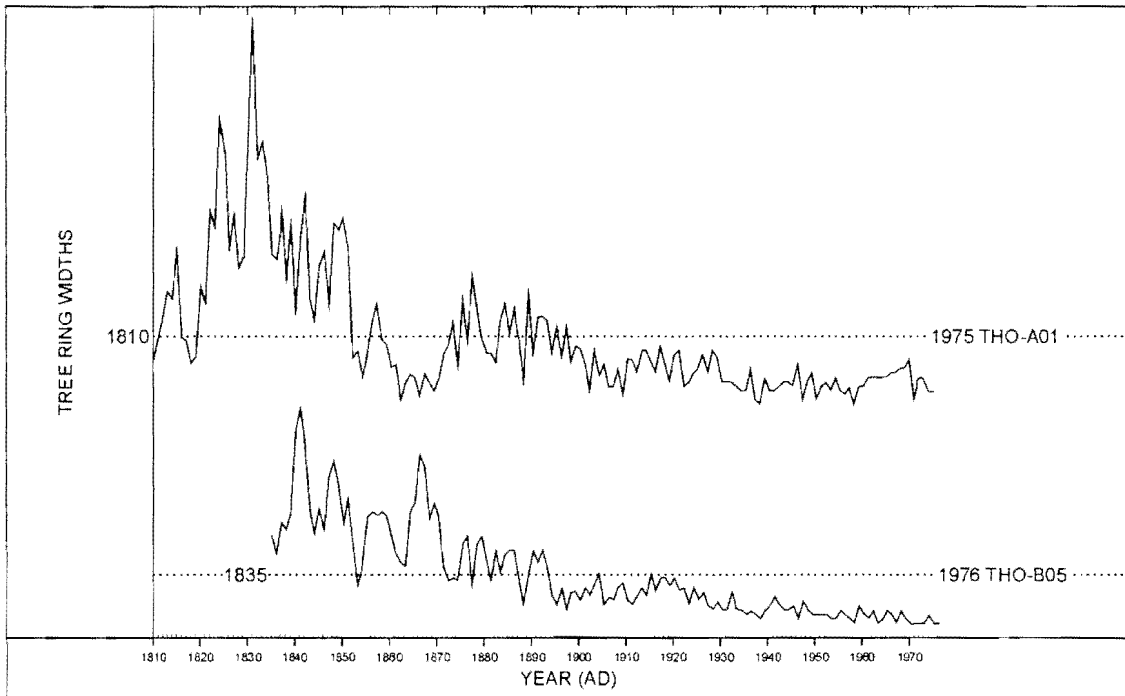


Fig. 6 Bar diagram showing the relative positions and dates of the first rings of the component site sequences in the East Midlands Master Dendrochronological Sequence, EM08/87



(a)



(b)

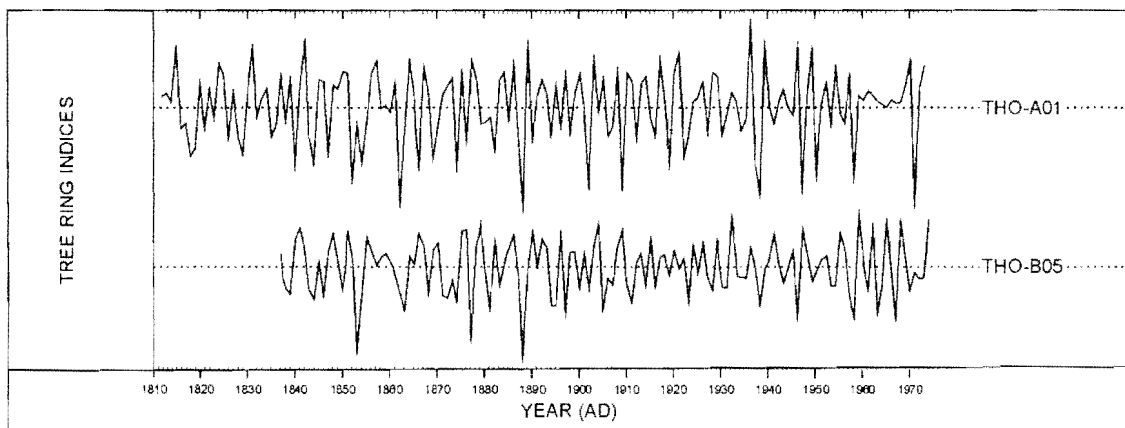


Fig 7. (a) The raw ring-widths of two samples, THO-A01 and THO-B05, whose felling dates are known. Here the ring widths are plotted vertically, one for each year, so that peaks represent wide rings and troughs narrow ones. Notice the growth-trends in each; on average the earlier rings of the young tree are wider than the later ones of the older tree in both sequences.

Fig 7. (b) The *Baillie-Pilcher* indices of the above widths. The growth-trends have been removed completely.

## REFERENCES

- Baillie, M G L, and Pilcher, J R, 1973, A simple cross-dating program for tree-ring research, *Tree-Ring Bulletin*, **33**, 7-14
- English Heritage, 1998 *Dendrochronology; Guidelines on Producing and Interpreting Dendrochronological Dates*, London
- Hillam, J, Morgan, R A, and Tyers, I, 1987, Sapwood estimates and the dating of short ring sequences, *Applications of tree-ring studies*, BAR Int Ser, **3**, 165-85
- Howard, R E, Laxton, R R, Litton, C D, and Simpson, W G, 1984-95, Nottingham University Tree-Ring Dating Laboratory Results, *Vernacular Architecture*, **15-26**
- Hughes, M K, Milson, S J, and Legett, P A, 1981 Sapwood estimates in the interpretation of tree-ring dates, *J Archaeol Sci*, **8**, 381-90
- Laxon, R R, Litton, C D, and Zainodin, H J, 1988 An objective method for forming a master ring-width sequence, *P A C T*, **22**, 25-35
- Laxton, R R, and Litton, C D, 1988 *An East Midlands Master Chronology and its use for dating vernacular buildings*, University of Nottingham, Department of Archaeology Publication, Monograph Series III
- Laxton, R R, and Litton, C D, 1989 Construction of a Kent Master Dendrochronological Sequence for Oak, AD 1158 to 1540, *Medieval Archaeol*, **33**, 90-8
- Laxon, R R, Litton, C D, and Howard, R E, 2001 *Timber; Dendrochronology of Roof Timbers at Lincoln Cathedral*, English Heritage Research Transactions, **7**
- Litton, C D, and Zainodin, H J, 1991 Statistical models of Dendrochronology, *J Archaeol Sci*, **18**, 29-40
- Miles, D W H, 1997 The interpretation, presentation and use of tree-ring dates, *Vernacular Architecture*, **28**, 40-56
- Pearson, S, 1995 *The Medieval Houses of Kent, An Historical Analysis*, London
- Rackham, O, 1976 *Trees and Woodland in the British Landscape*, London